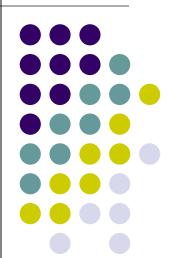
Computer Graphics (CS 543) Lecture 5a: Hierarchical 3D Models

Prof Emmanuel Agu

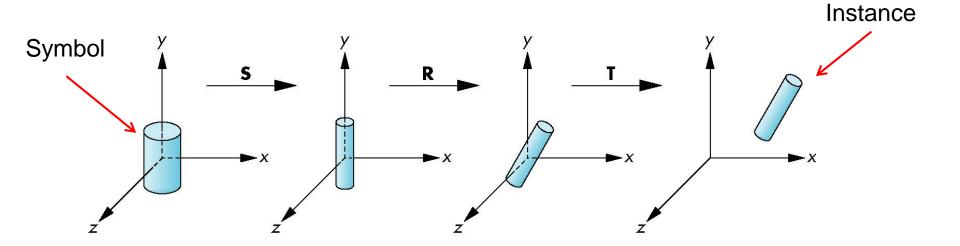
Computer Science Dept. Worcester Polytechnic Institute (WPI)



Instance Transformation



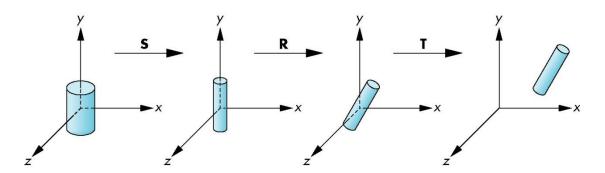
- Start with unique object (a symbol)
- Each appearance of object in model is an instance
 - Must scale, orient, position
 - Defines instance transformation



Symbol-Instance Table

Can store intances + instance transformations

Symbol	Scale	Rotate	Translate
1	s_x, s_y, s_z	$\theta_{x'} \theta_{y'} \theta_{z}$	d_{x}, d_{y}, d_{z}
2	•	_	
3			
1			
1			

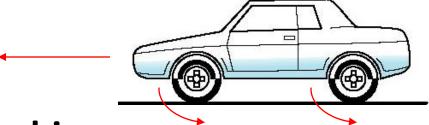




Problems with Symbol-Instance Table



- Symbol-instance table does not show relationships between parts of model
- Consider model of car
 - Chassis (body) + 4 identical wheels
 - Two symbols



- Relationships:
 - Wheels connected to chassis
 - Chassis motion determined by rotational speed of wheels



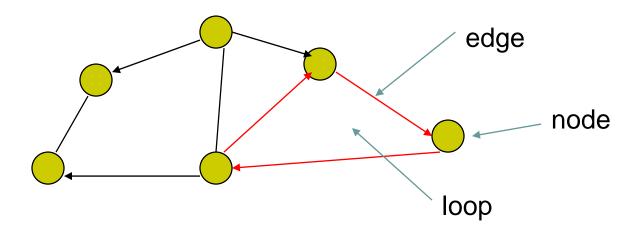


```
car(speed)
{
    chassis()
    wheel(right_front);
    wheel(left_front);
    wheel(right_rear);
    wheel(left_rear);
}
Left front
wheel
```

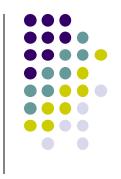
- Fails to show relationships between parts
- Explore graph representation

Graphs

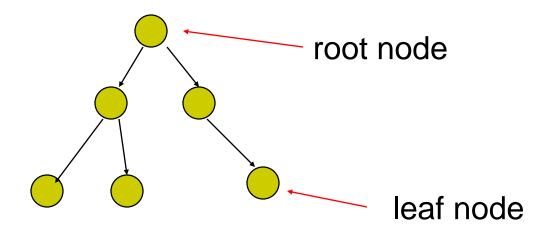
- Set of nodes + edges (links)
- Edge connects a pair of nodes
 - Directed or undirected
- Cycle: directed path that is a loop



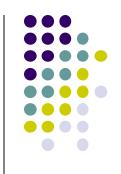
Tree

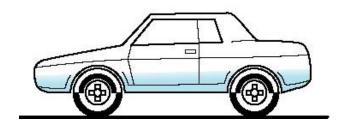


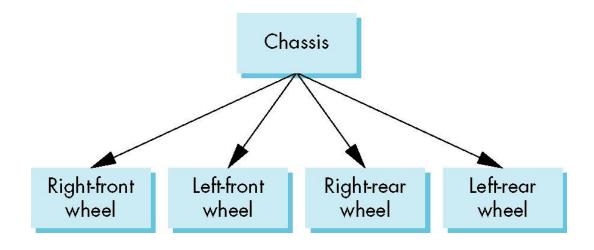
- Graph in which each node (except root) has exactly one parent node
 - A parent may have multiple children
 - Leaf node: no children





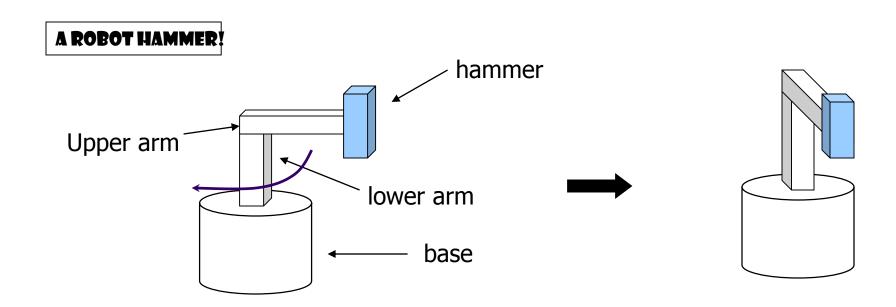




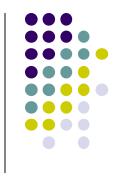


Hierarchical Transforms

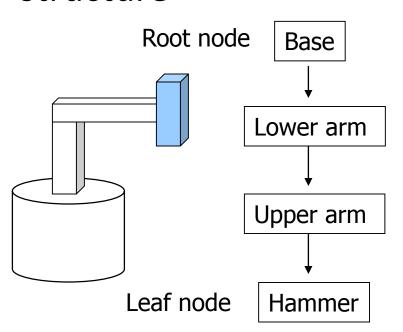
- Robot arm: Many small connected parts
- Attributes (position, orientation, etc) depend on each other







 Object dependency description using tree structure

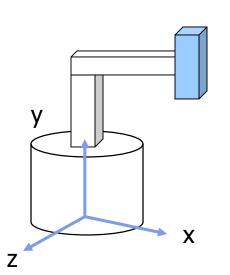


Object position and orientation can be affected by its parent, grand-parent grand-parent ... nodes

Hierarchical representation is known as a **Scene Graph**

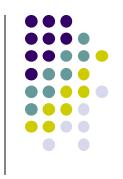
Transformations

- Two ways to specify transformations:
 - (1) Absolute transformation: each part transformed independently (relative to origin)



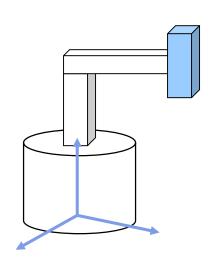
Translate the base by (5,0,0);
Translate the lower arm by (5,0,0);
Translate the upper arm by (5,0,0);
...

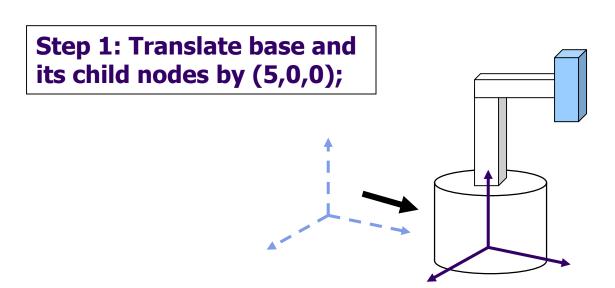
Relative Transformation



A better (and easier) way:

(2) Relative transformation: Specify transformation for each object relative to its parent

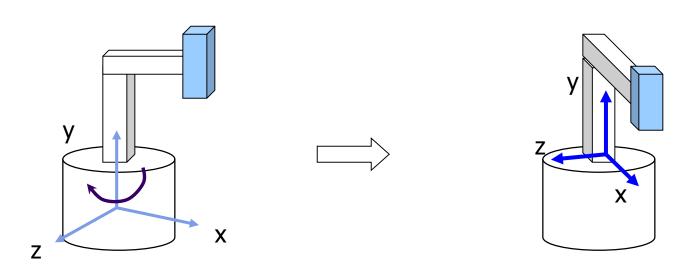




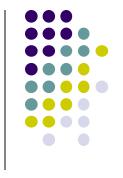




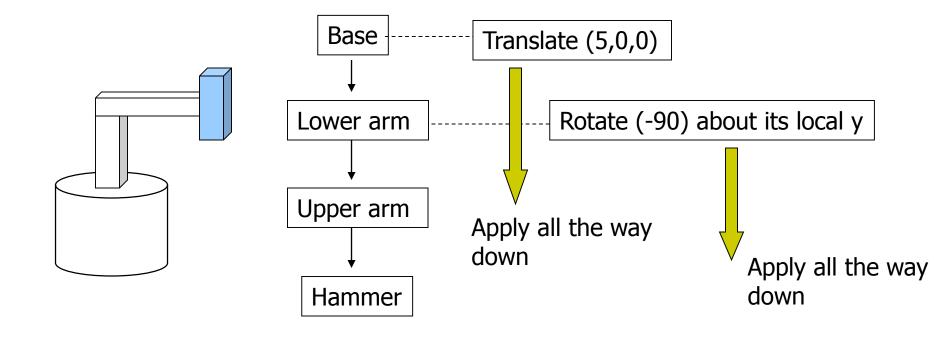
Step 2: Rotate the lower arm and all its descendants relative to the base's local y axis by -90 degree



Relative Transformation



Relative transformation using scene graph



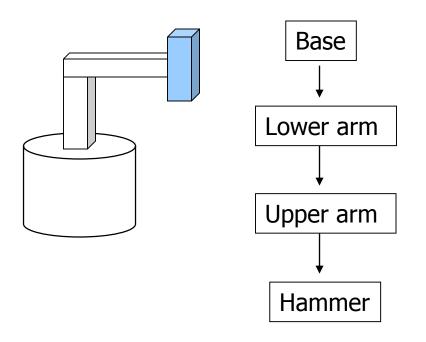
Hierarchical Transforms Using OpenGL



Translate base and all its descendants by (5,0,0)

Rotate lower arm and its descendants by -90 degree about

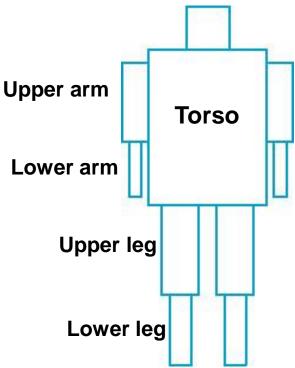
local y



```
ctm = LoadIdentity();
... // setup your camera
ctm = ctm * Translatef(5,0,0);
Draw_base();
ctm = ctm * Rotatef(-90, 0, 1, 0);
Draw_lower _arm();
Draw_upper_arm();
Draw_hammer();
```

Hierarchical Modeling

- For large objects with many parts, need to transform groups of objects
- Need better tools

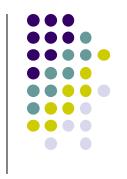


Hierarchical Modeling



- Previous CTM had 1 level
- Hierarchical modeling: extend CTM to stack with multiple levels using linked list
- Manipulate stack levels using 2 operations
 - pushMatrix
 - popMatrix

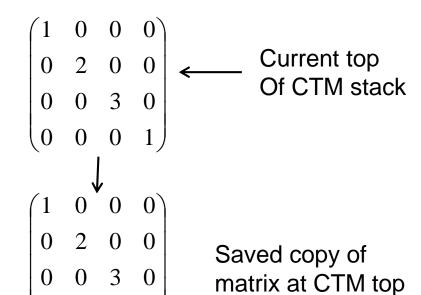
PushMatrix



- PushMatrix(): Save current modelview matrix (CTM) in stack
- Positions 1 & 2 in linked list are same after PushMatrix

Before PushMatrix

After PushMatrix

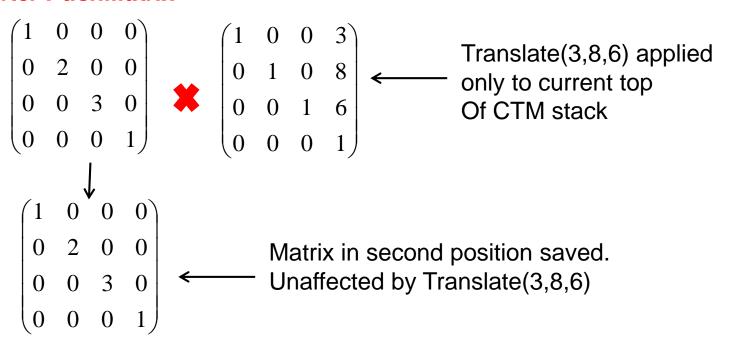


PushMatrix



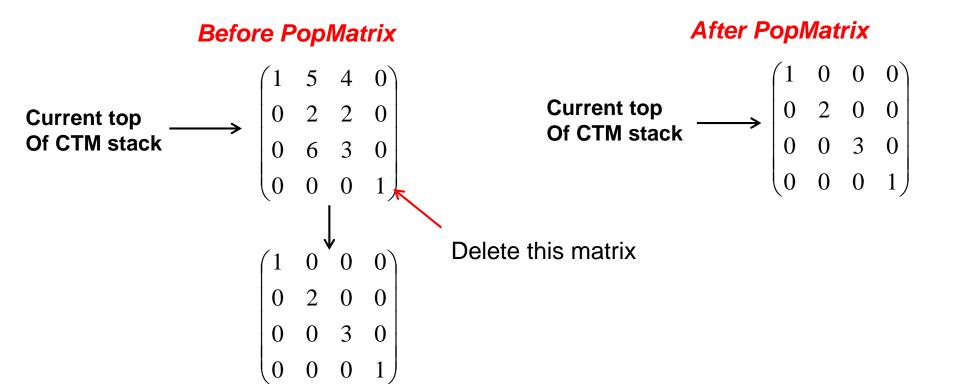
- Subsequent Rotate, Scale, Translate affect only top matrix
- E.g. ctm = ctm * Translate (3,8,6)

After PushMatrix



PopMatrix

 PopMatrix(): Delete position 1 matrix, position 2 matrix becomes top



Modelview Matrix Code Stack glLoadIdentity(); $I * M_1 = M_1$ glTranslatef(0.0, 0.0, -15.0); Processing in code order M_1 glPushMatrix(); //Copy of M₁ placed on top. $M_1^*M_2$ glScalef(1.0, 2.0, 1.0); $M_1 * M_2$ glutWireCube(5.0); //No change. glPopMatrix(); M_1 //Back to before the push statement! glTranslatef(0.0, 7.0, 0.0); M_1*M_3 glutWireSphere(2.0, 10, 8); M_1*M_3 //No change.

Figure 4.19: Transitions of the modelview matrix stack.

PopMatrix and PushMatrix Illustration



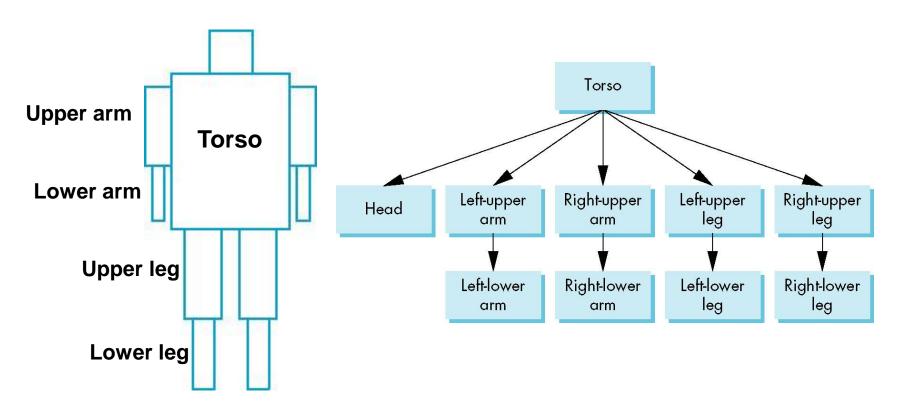
- Note: Diagram uses old glTranslate, glScale, etc commands
- We want same behavior though

Apply matrix at top of CTM to vertices of object created

Ref: Computer Graphics Through OpenGL by Guha

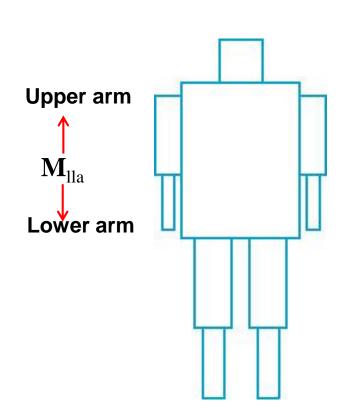






Building the Model

- Draw each part as a function
 - torso()
 - left_upper_arm(), etc
- Transform Matrices: transform of node wrt its parent
 - \mathbf{M}_{lla} positions left lower arm with respect to left upper arm
- Stack based traversal (push, pop)





Draw Humanoid using Stack

Torso



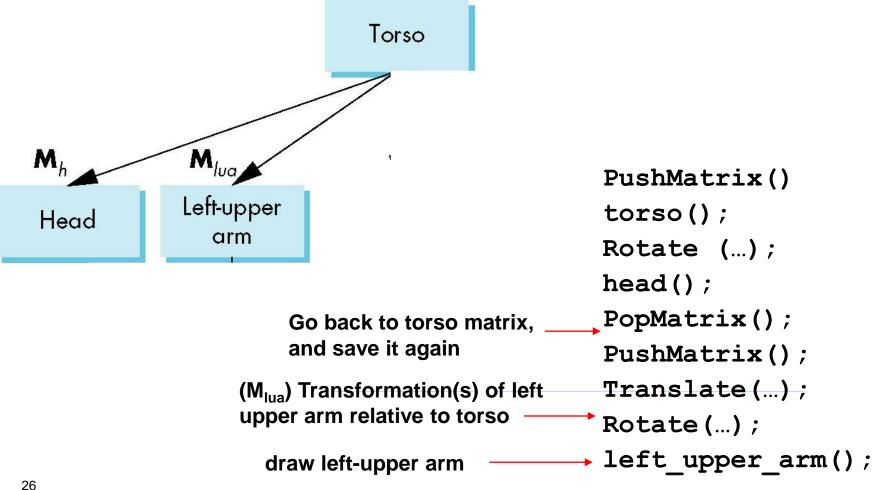


```
Torso
               figure() {
Head
                   PushMatrix()
                   torso();
                                               (M<sub>h</sub>) Transformation of head
                   Rotate (...); ←
                                               Relative to torso
                   head();
                                              draw head
```

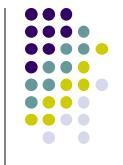


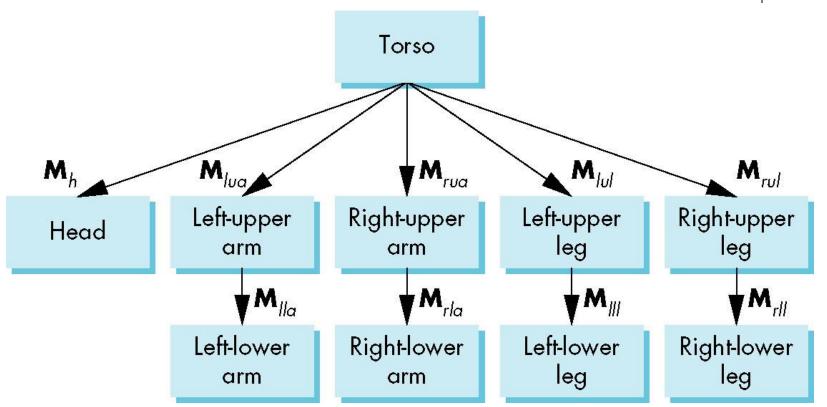
// rest of code()

Draw Humanoid using Stack



Complete Humanoid Tree with Matrices

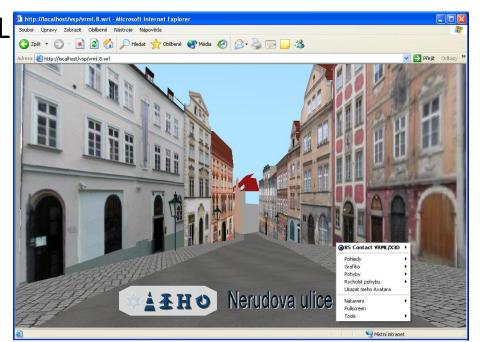




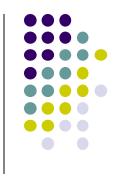
Scene graph of Humanoid Robot

VRML

- Scene graph introduced by SGI Open Inventor
- Used in many graphics applications (Maya, etc)
- <u>Virtual Reality Markup Language</u>
 - Scene graph representation of virtual worlds on Web
 - Scene parts can be distributed across multiple web servers
 - Implemented using OpenGL







References

 Angel and Shreiner, Interactive Computer Graphics (6th edition), Chapter 8