



**CS 563 Advanced Topics in  
Computer Graphics**  
*Triangular Meshes*

by Scott Ingram



# Rendering Goals

- Ultimate goal is to achieve photo realism when rendering objects
  - May be painful to build an model by using primitive shapes: spheres, planes, cones, torii, etc.
  - One solution... compose the model using a number of tessellated 2d shapes.

# Triangular Meshes

- The 2D tessellated shapes most commonly used are triangles.
  - Advantages
    - Artist/Programmer tools for creating editing models
    - Simplifies math, allows for faster rendering
    - Hardware support for triangle mesh processing
  - Mesh Sources
    - Artist/Programmer created
    - Physically 'sourced'
      - Derived from laser scans
      - Derived from image scans
      - Derived Mechanically

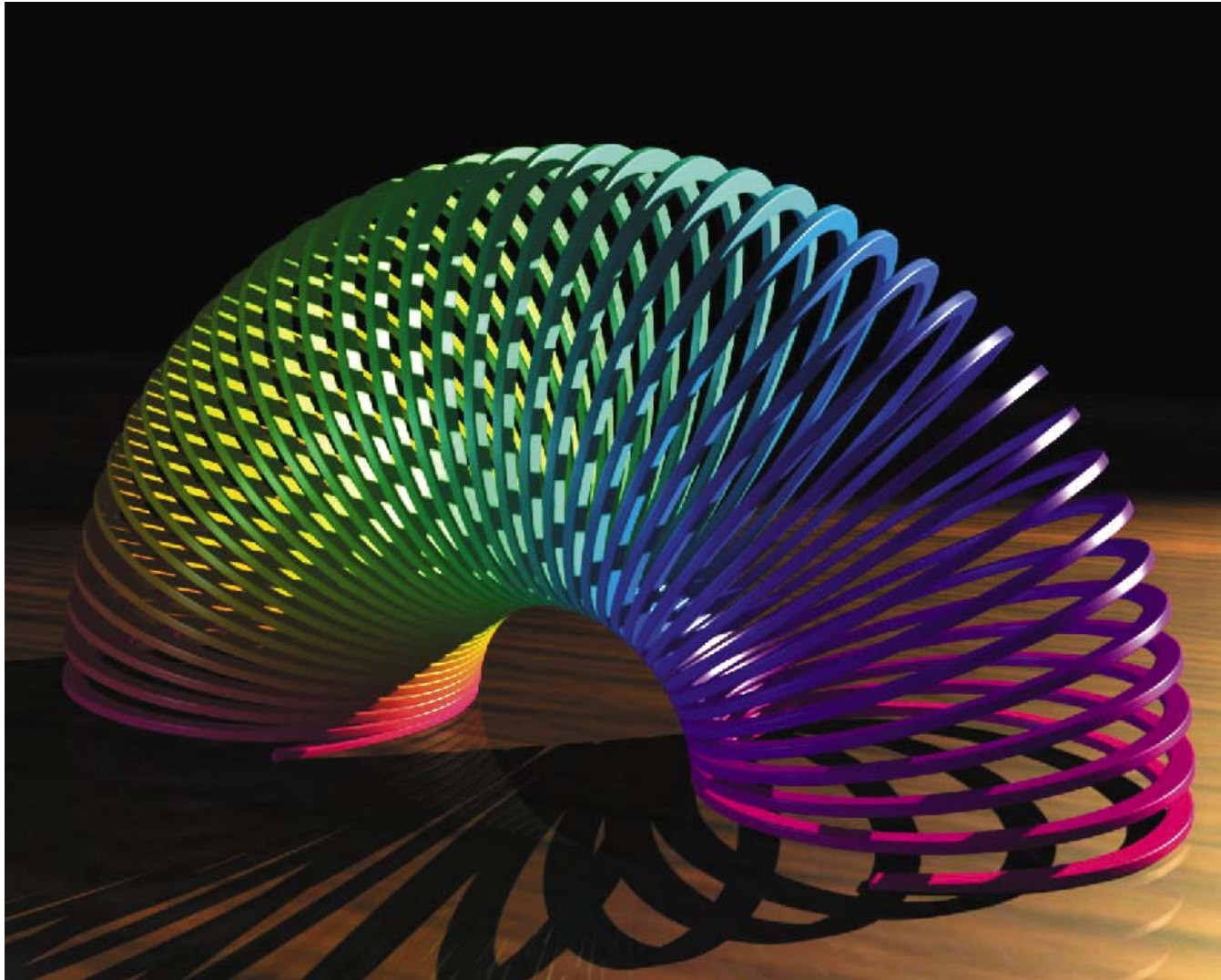
# Mesh Sources

- Artist Derived: Artists uses Maya/Zbrush package to model real or imaginary object. Exports design to .ply file (or some other format) for use in a renderer



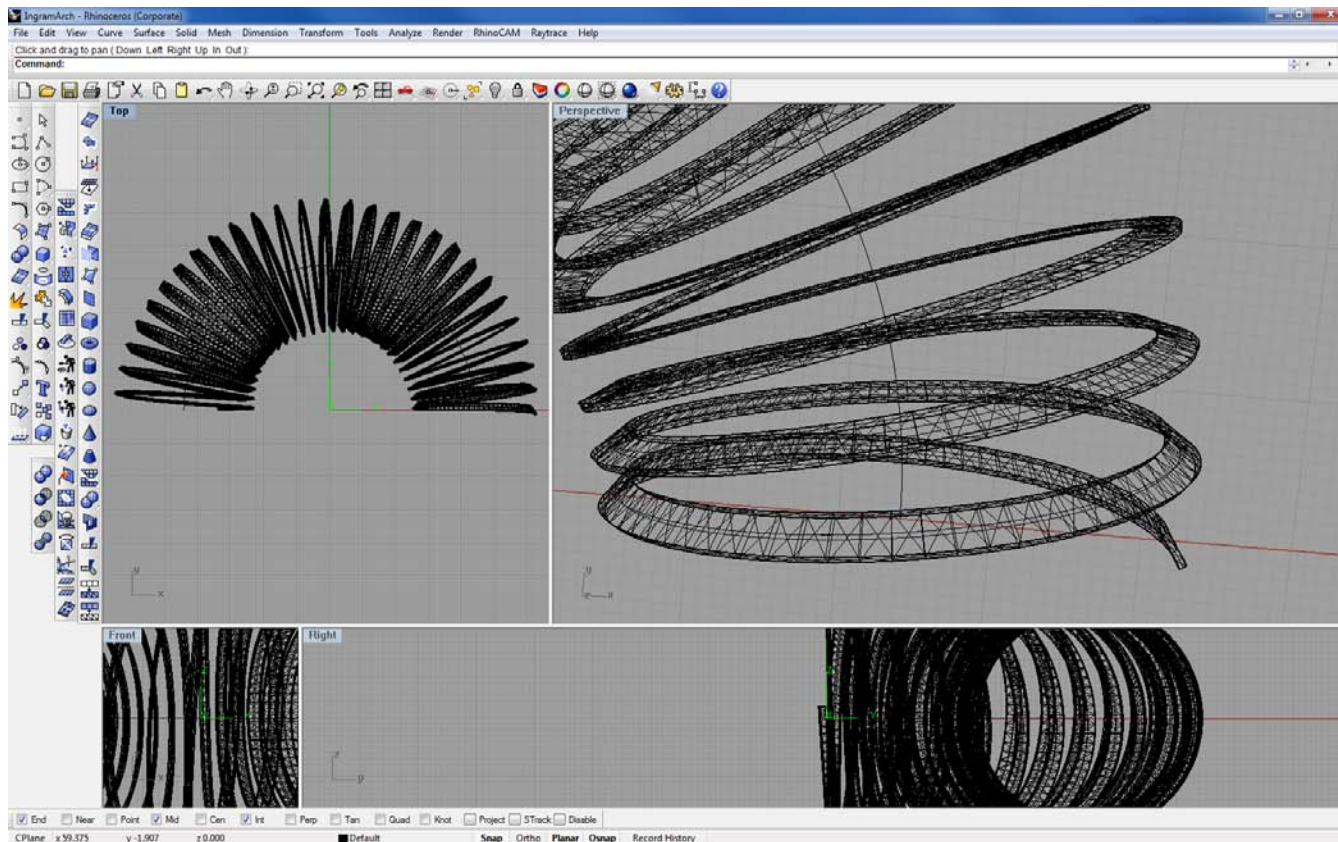
# Mesh Sources

- Rainbow Arch by Steve Agland (p304, Figure16.11)

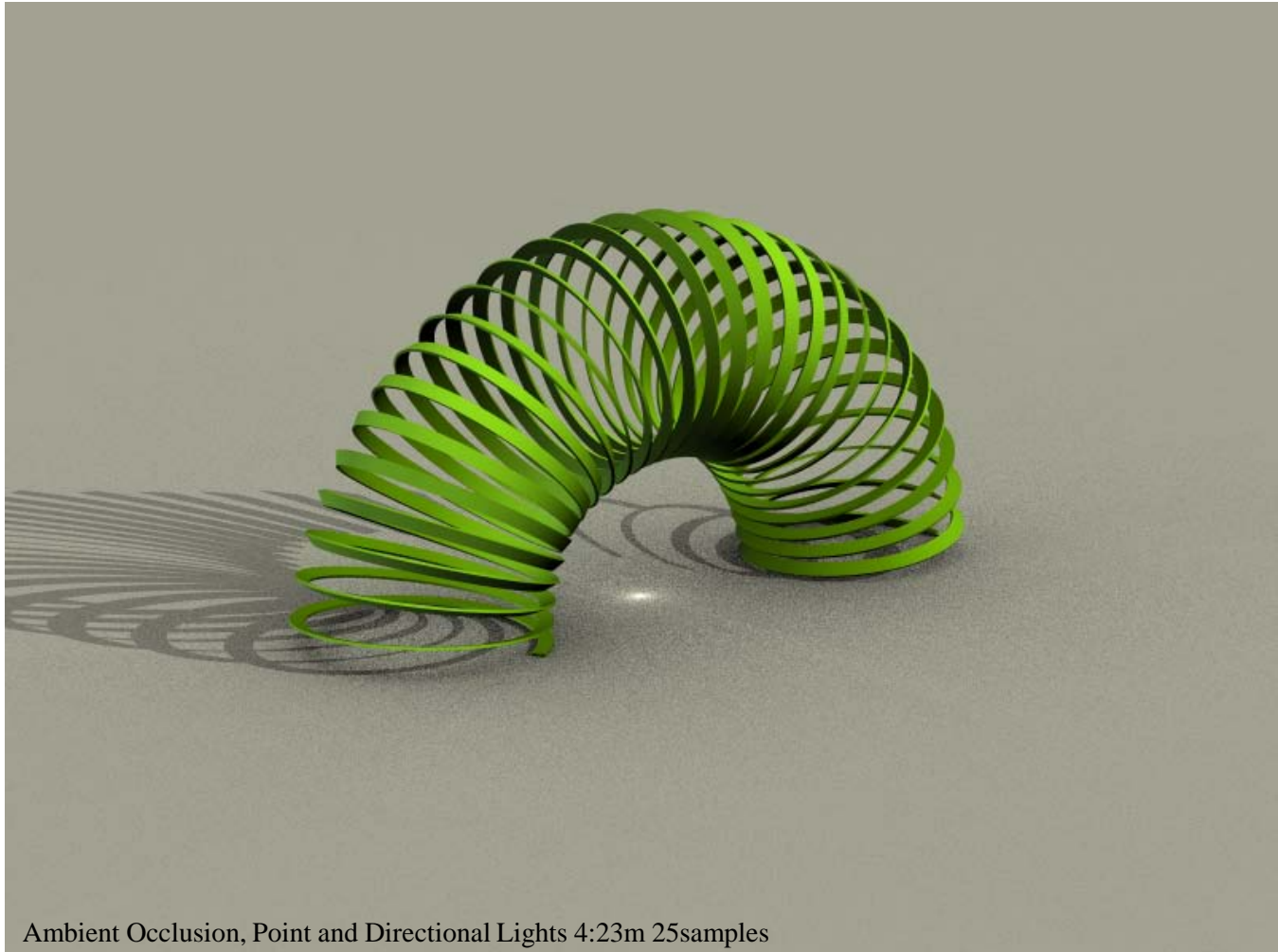


# Mesh Sources

- Reproduction of Arch
  - Create arch line
  - Create Helix along arch line
  - Create sweep cross section
  - Sweep cross section along Helix path
  - Convert to Tri - Mesh, Export to .ply file (element vertex 81940)



- Crude Reproduction



Ambient Occlusion, Point and Directional Lights 4:23m 25samples

# Mesh Sources

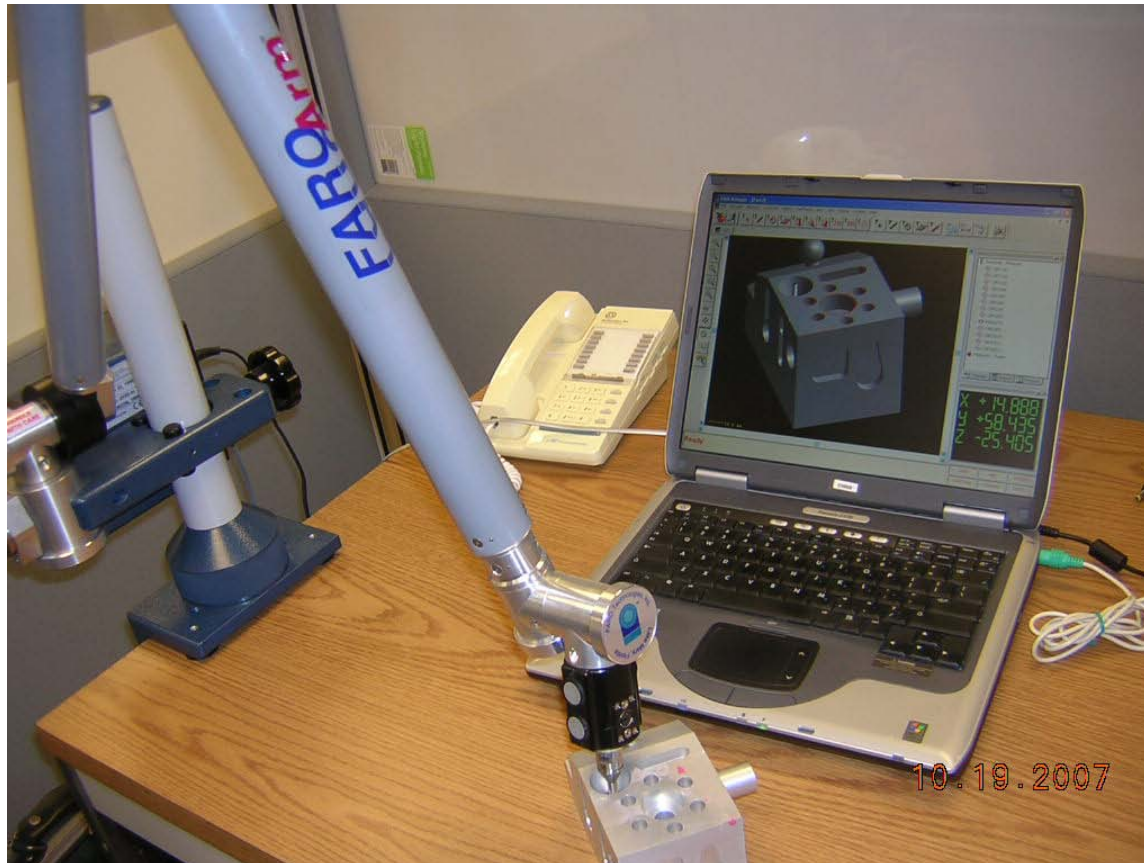
- Laser Scanned: hand held, or mounted





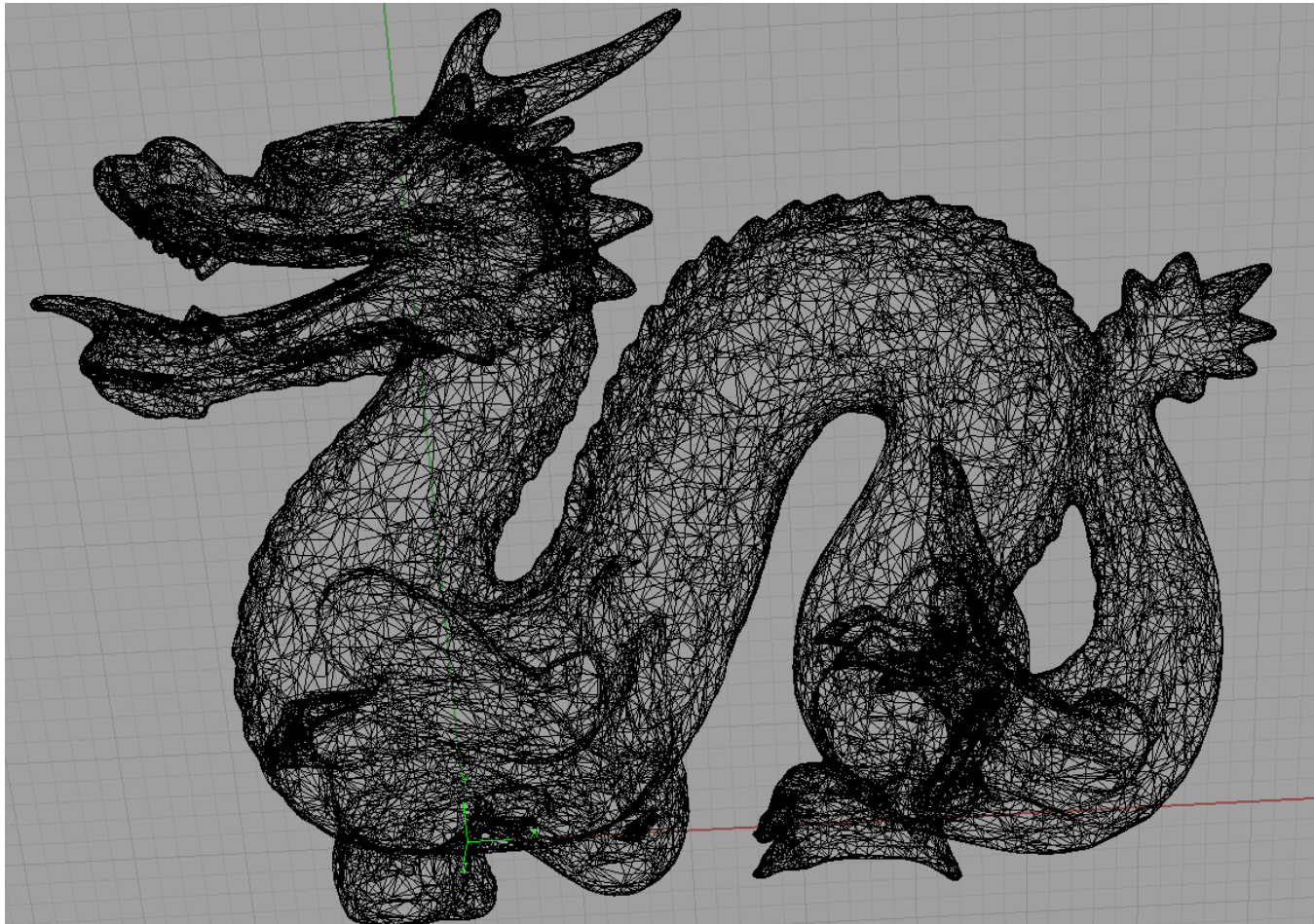
# Mesh Sources

- Mechanical: User directs an articulated arm to record points of interest: <http://www.faro.com/FaroArm/Home.htm>



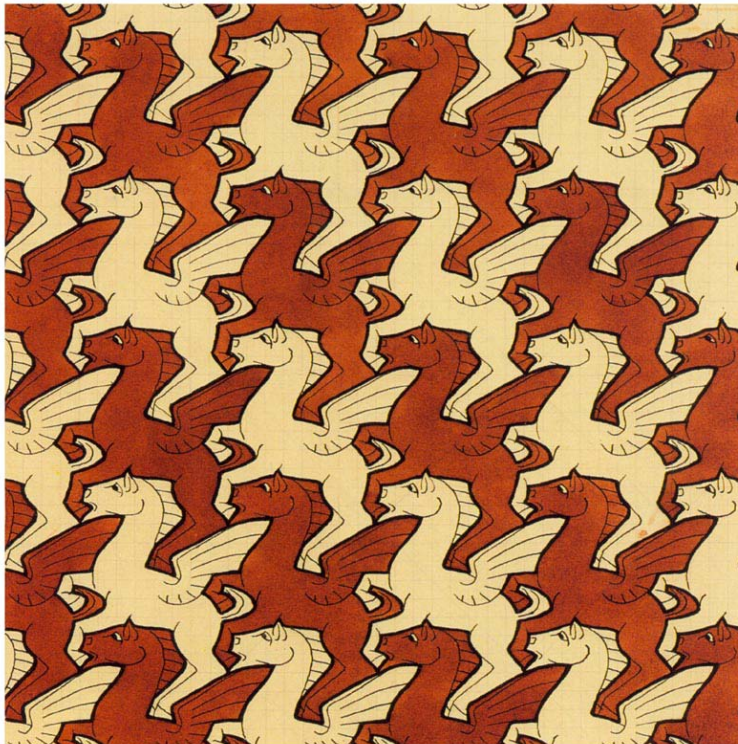
# Triangular Meshes

- Increase # of triangles.... increase the realism of the model



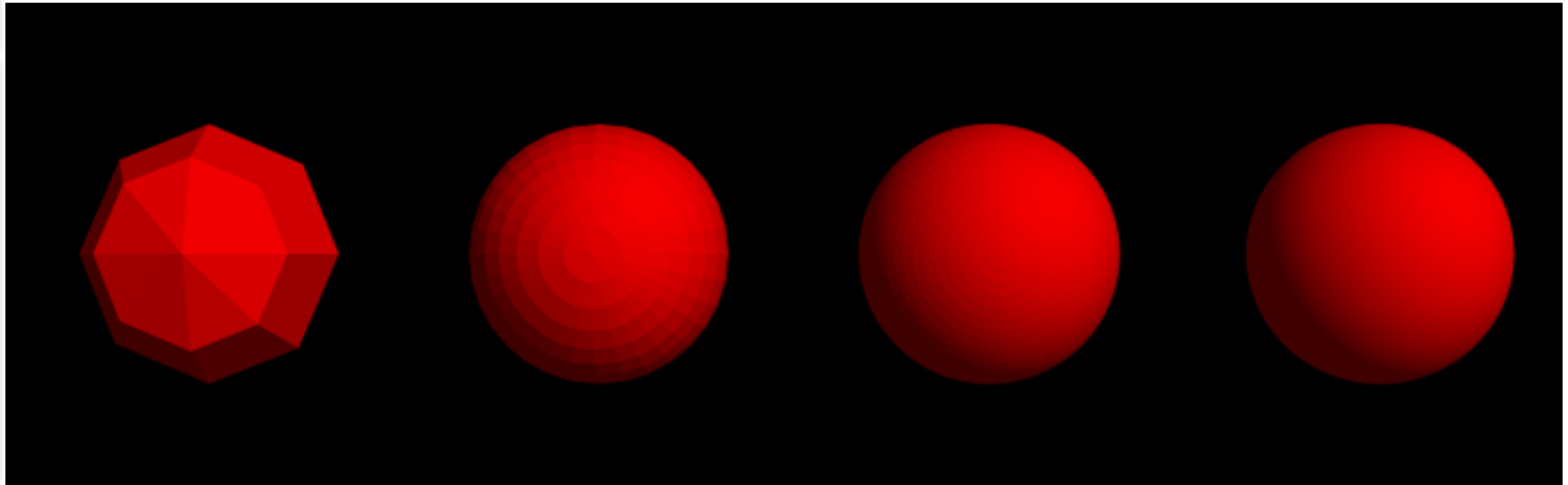
# Tessellation

- Tessellation (a.k.a tiling)
  - Repetition of a shape
  - No overlaps , no gaps
  - Also know as tiling
  - In 2D....



# Tessellating a Sphere

- Example: Sphere Tessellation



- $m=8, n=4$                        $m=32, n=16$                        $m=64, n=32$                        $m=128, n=64$
- $m = \#$  in azimuth direction
- $n = \#$  in polar direction

# Tessellating a Sphere (cont)

- tessellate\_flat\_sphere (author provided code)

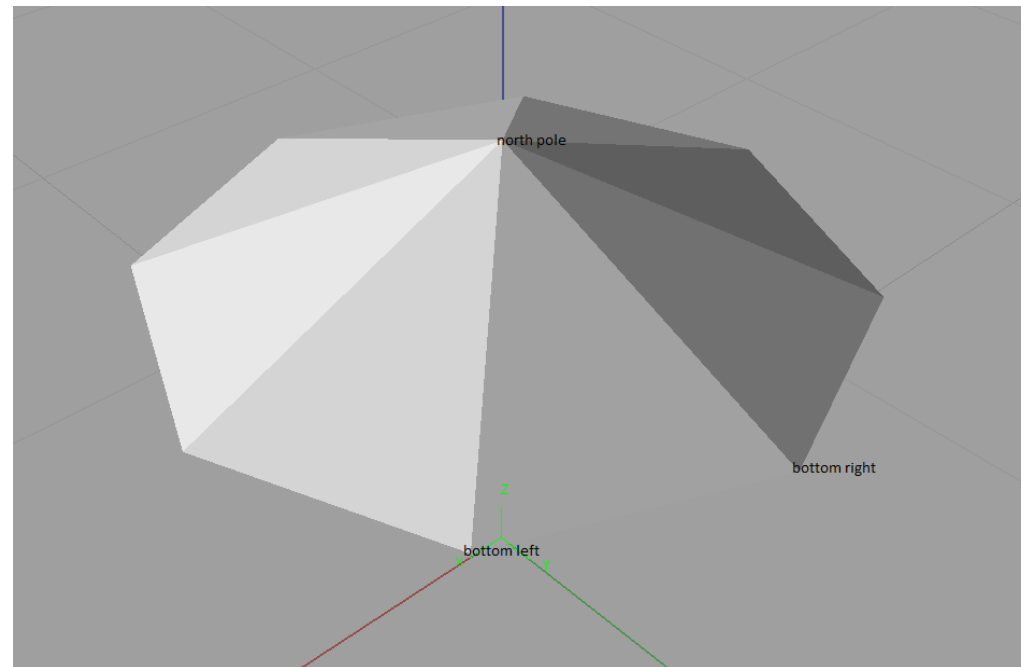
```
//Sphere Tessellation Pseudo Code
```

```
pick 'North Pole' point  
pick 'South Pole' point
```

```
//For triangles touching North Pole....  
for (0 -> m-1)  
    generate bottom left point  
    generate bottom right point  
    generate triangle (north pole, bot lft pnt, bot rgt pnt)
```

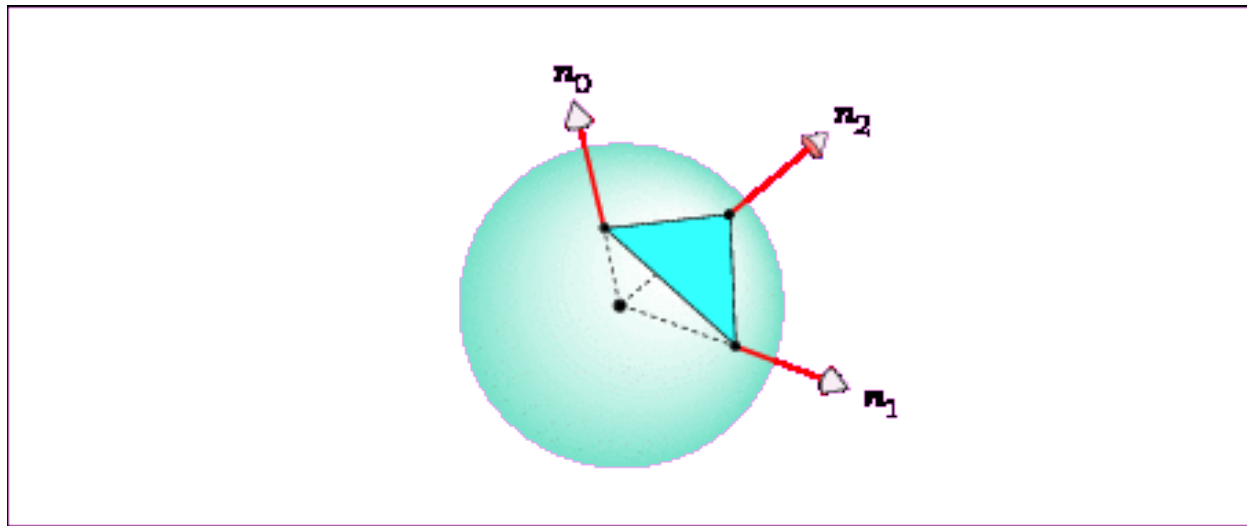
```
//For triangles touching South Pole....  
for (0 -> m-1)  
    generate top left point  
    generate top right point  
    generate triangle (south pole, top lft pnt, top rgt pnt)
```

```
//For 'stuff' in the middle  
for (0 -> n-2)  
    for (0 -> m-1)  
        //first triangle  
            generate bottom left  
            generate bottom right  
            generate top left  
        //second triangle  
            generate top right  
            generate top left  
            generate bottom right
```



# Tessellating a Sphere (cont)

- It would be nice to be able to vary shading across the triangle

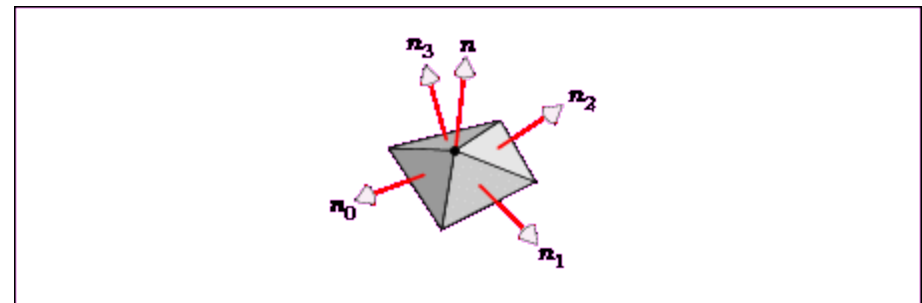
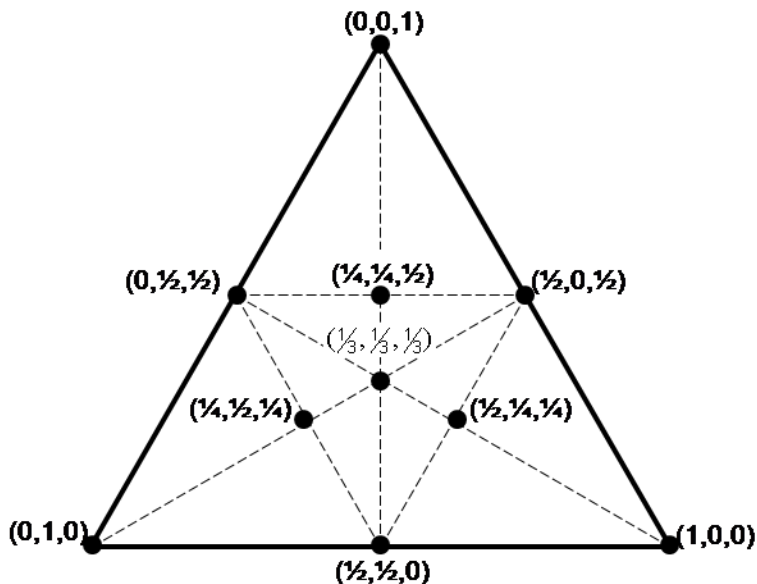


- The  $n_0$ ,  $n_1$ ,  $n_2$  normals of the sphere differ
- Gives the appearance of curvature rather than flat facets

# Smooth Shading

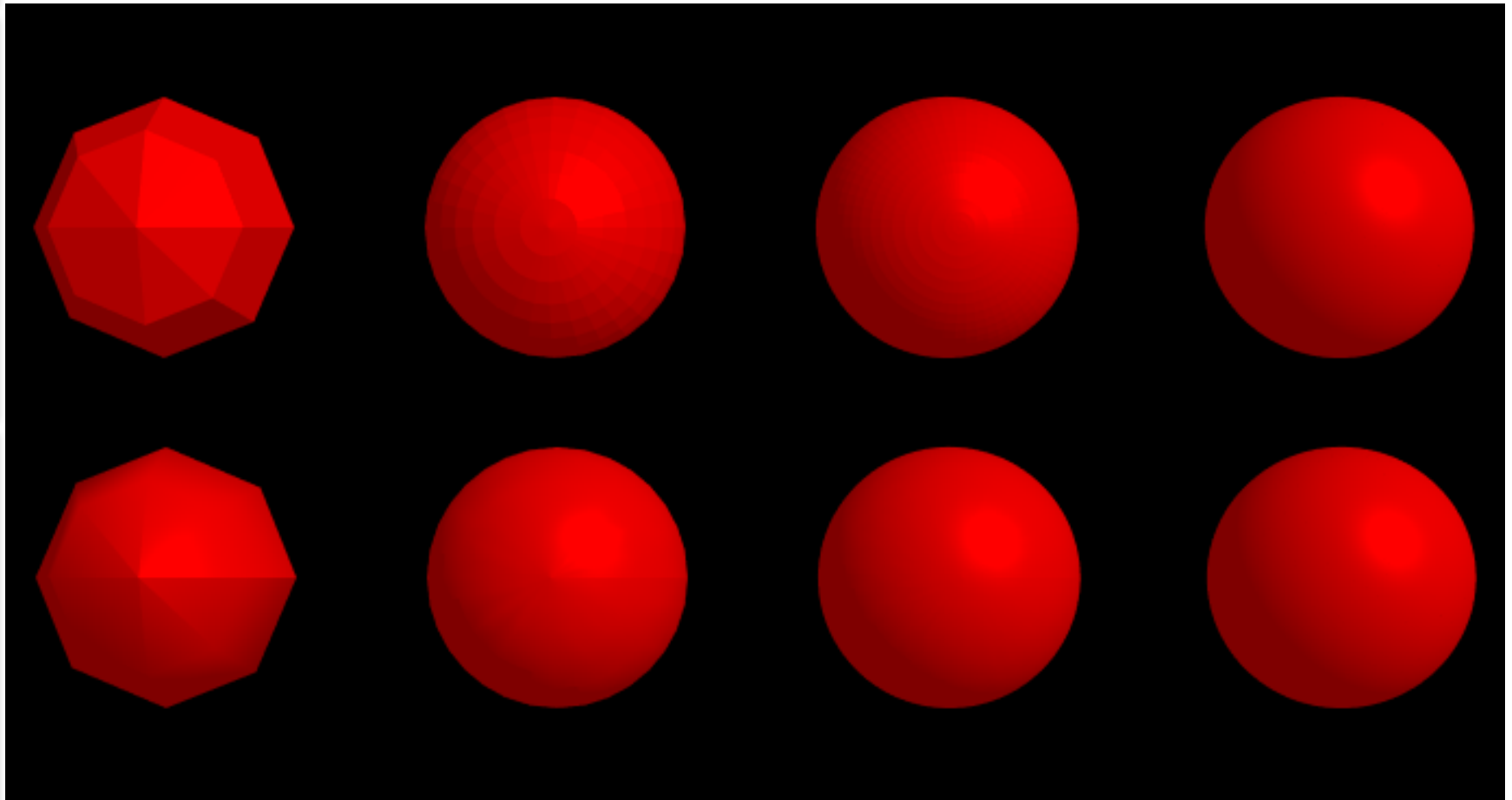
- Interpolate the normals on the interior of the triangle.
- Continuous shading makes the triangles edges disappear
- Silhouette outline still maintains flat appearance
- Use Barycentric coordinates and interpolate

$$n = \frac{1}{3}n_0 + \frac{1}{3}n_1 + \frac{1}{3}n_2$$



## Smooth Shading(cont)

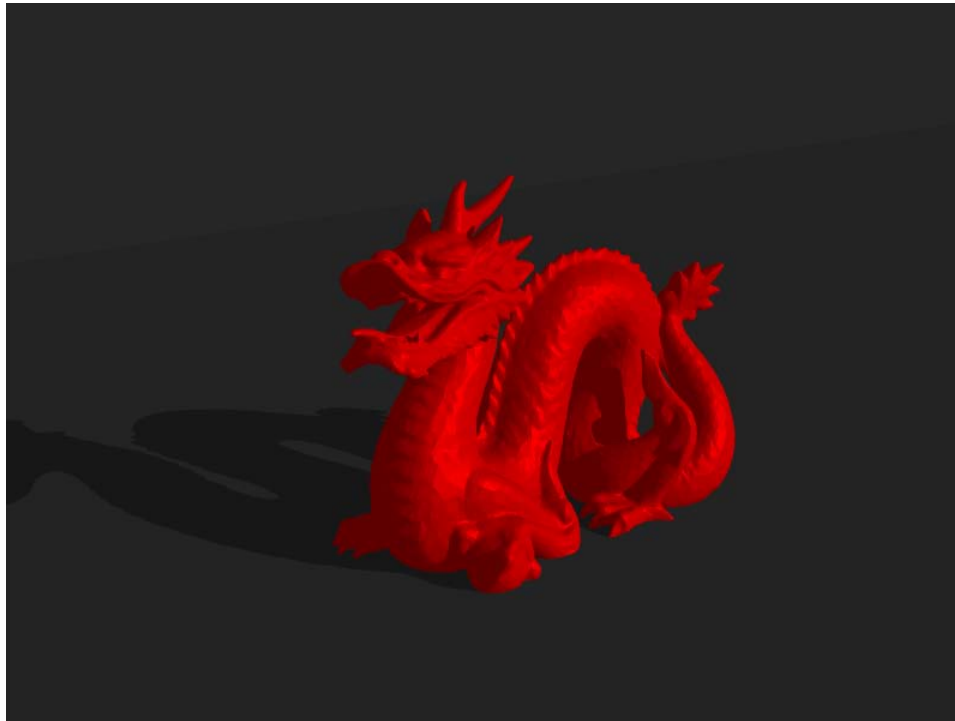
- Flat versus Smooth shading





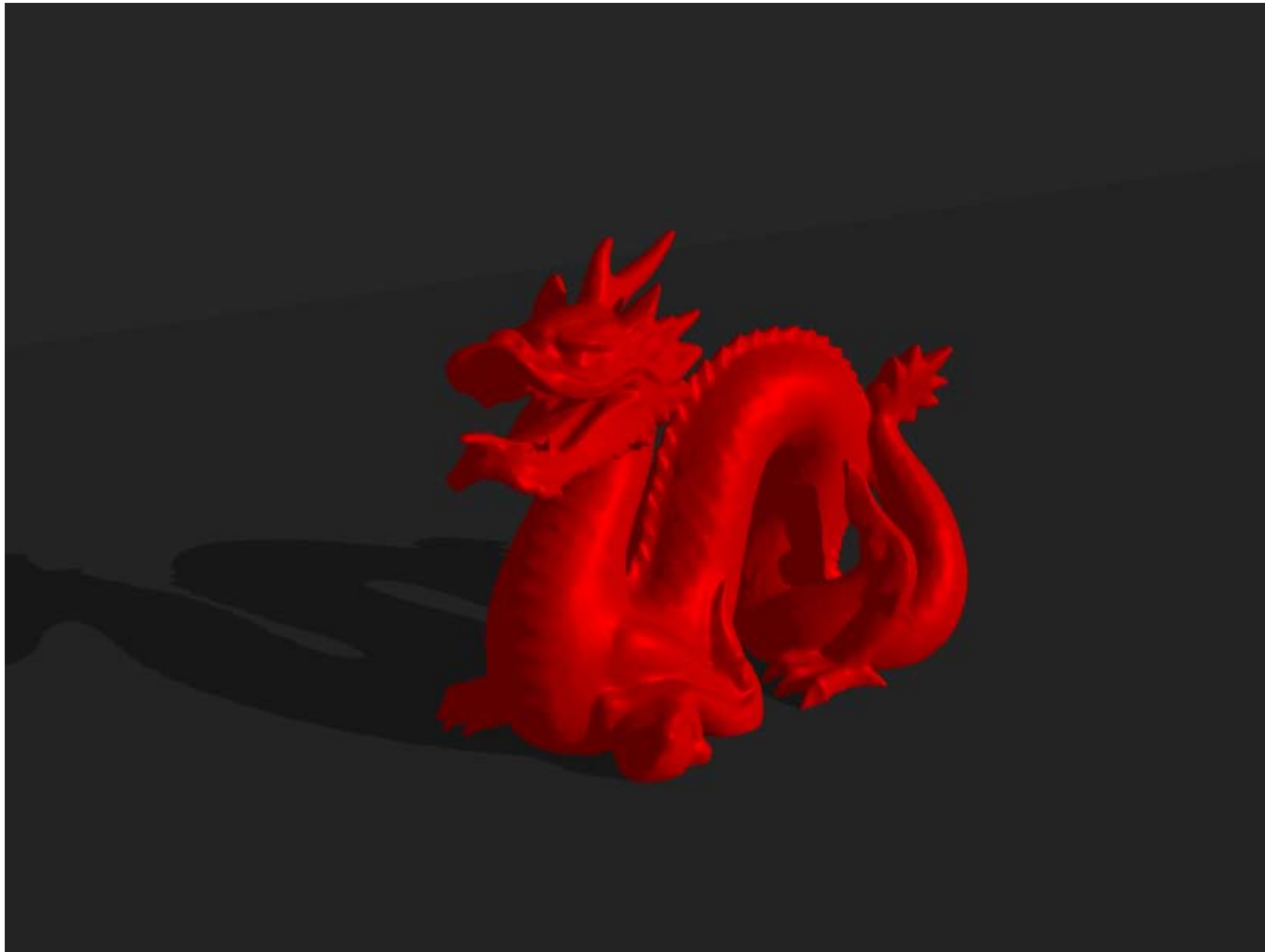
# Smooth Shading(cont)

- Smooth Shading requires storage of the additional normals and as such requires more memory (?).
  - Performance impact with Spheres, not noticed
  - Performance impact with Dragon, also unnoticed 51s for flat, 52 seconds for smooth. Both cases ~36,668k memory used.



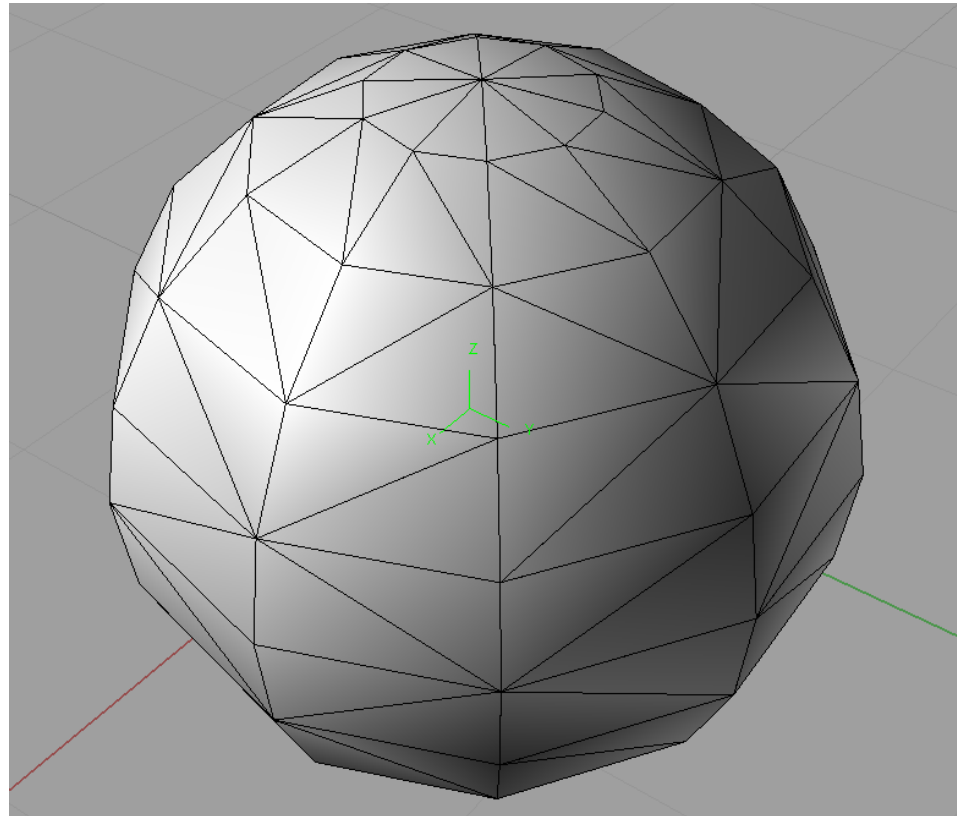
# Smooth Shading(cont)

- Smooth shaded dragon



# Mesh Data Structure

- Large Meshes = Memory hogs ('xyzrgb\_statuette' = 185MB)
- A single vertex is shared by adjacent triangles (average of 6 for closed mesh)
- Save coordinates and normal for each vertex once

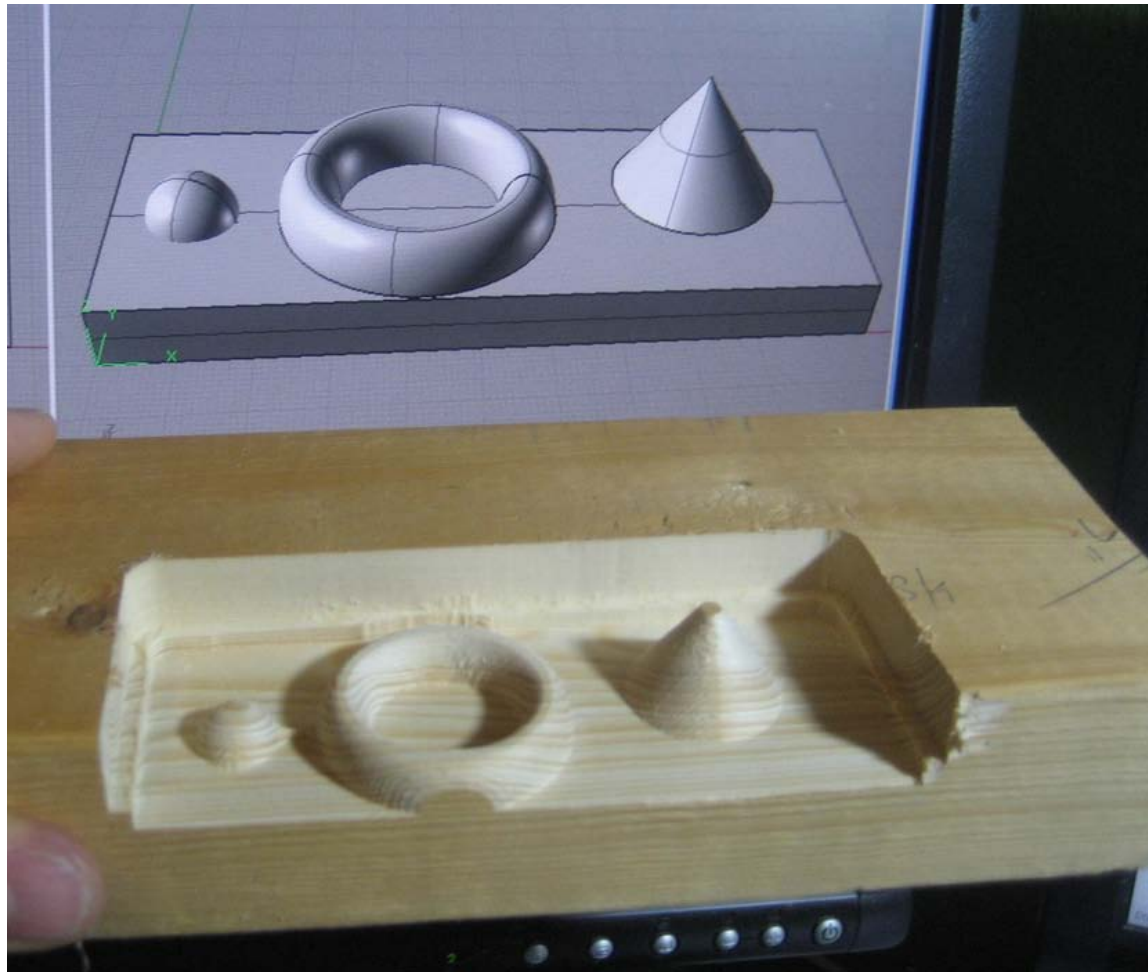


- Sample PLY file

```
ply
format ascii 1.0
comment made by anonymous
comment this file is a cube
element vertex 8
property float32 x
property float32 y
property float32 z
element face 6
property list uint8 int32 vertex_index
end_header
0 0 0
0 0 1
0 1 1
0 1 0
1 0 0
1 0 1
1 1 1
1 1 0
4 0 1 2 3
4 7 6 5 4
4 0 4 5 1
4 1 5 6 2
4 2 6 7 3
4 3 7 4 0
```

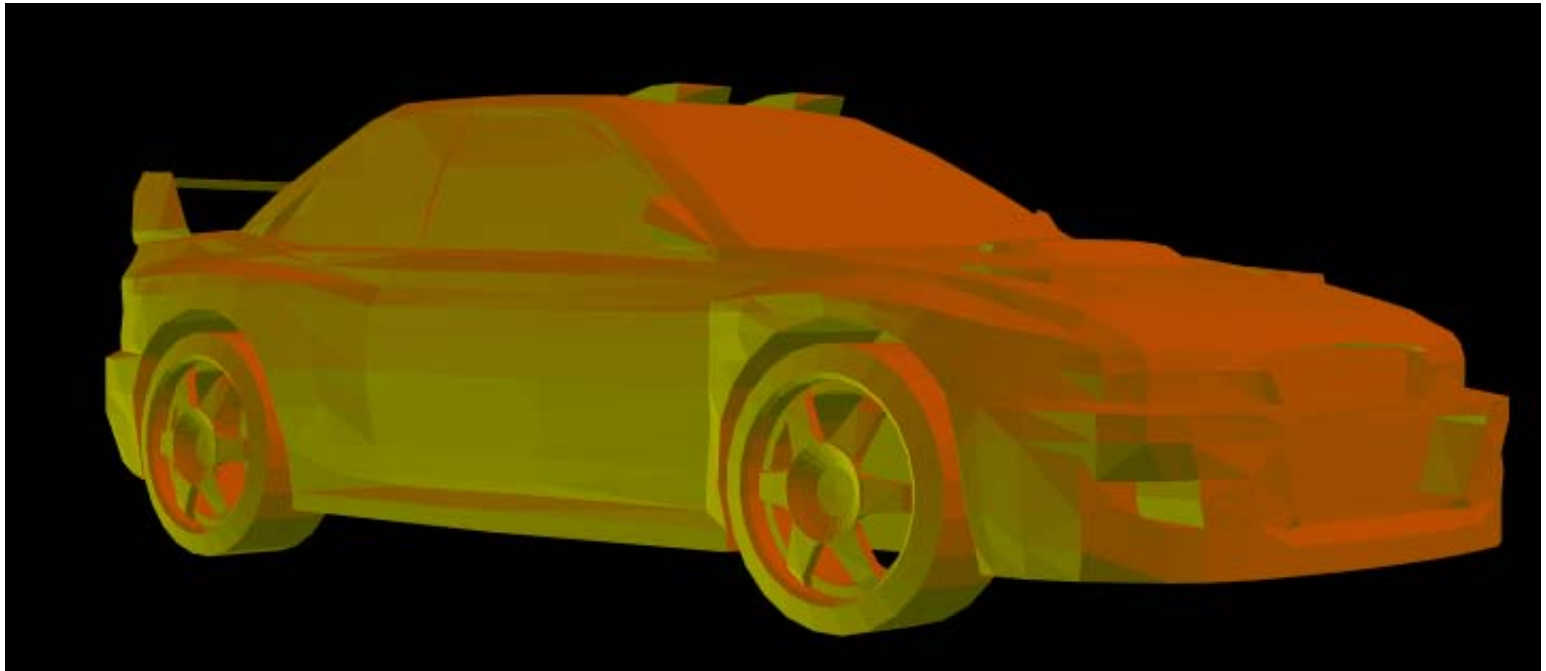
# Mesh Resources

- Rhino3d: Popular (?) CAD/CAM package for Industrial, Architectural, Jewelry, etc. Various 3rd-party plug ins are available for car modeling, virtual clay modeling, 3d prototyping, CNC tool paths ...



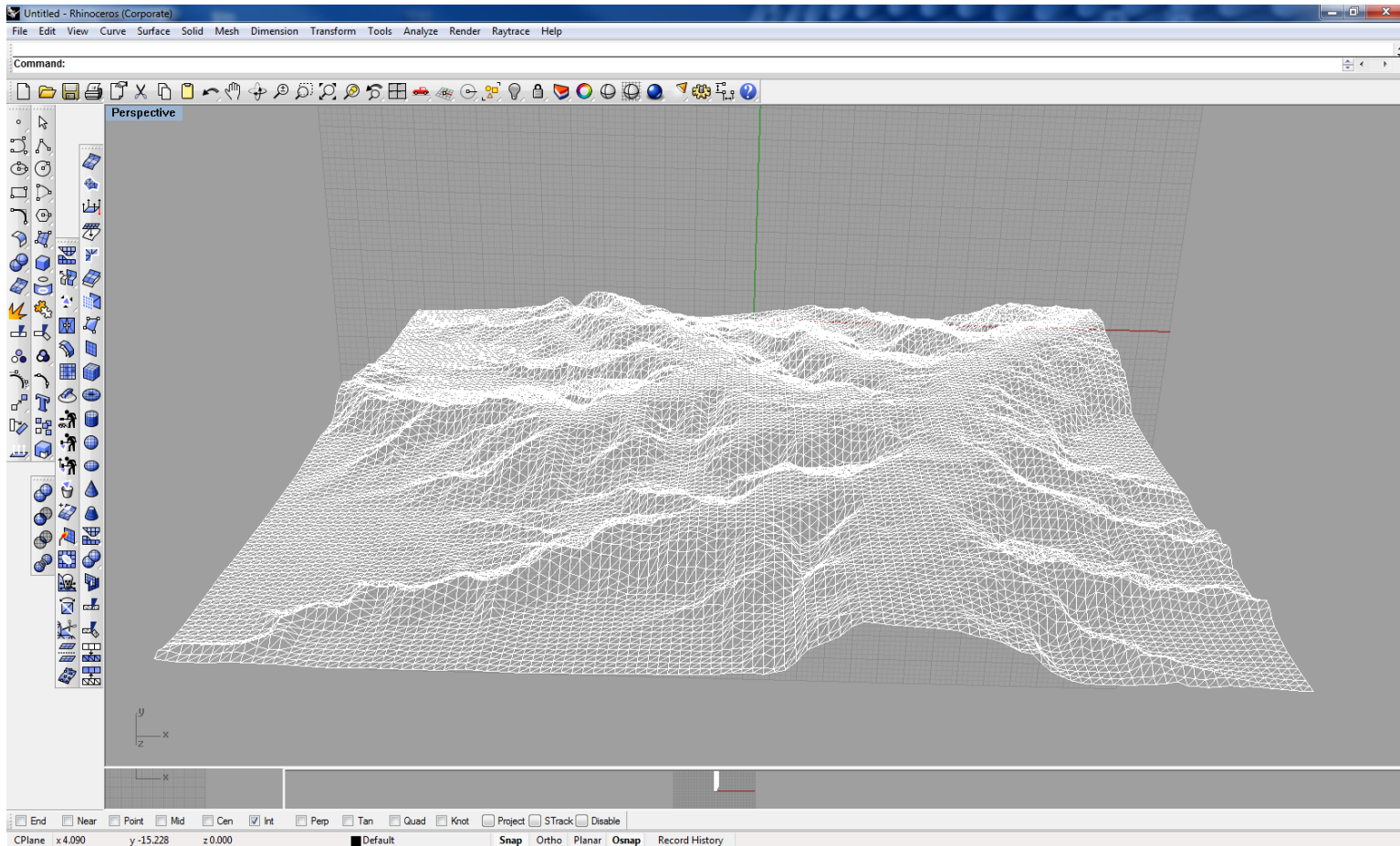
# Mesh Resources

- Rhino3d:
  - Allows import of many different model formats: 3dm, igs, vda, dwg, dxf, 3ds, lwo, stl, obj, *ply*, skp
  - Example: Imported .lwo model from <http://dmi.chez-alice.fr/models1.html> exported as .ply file and then rendered



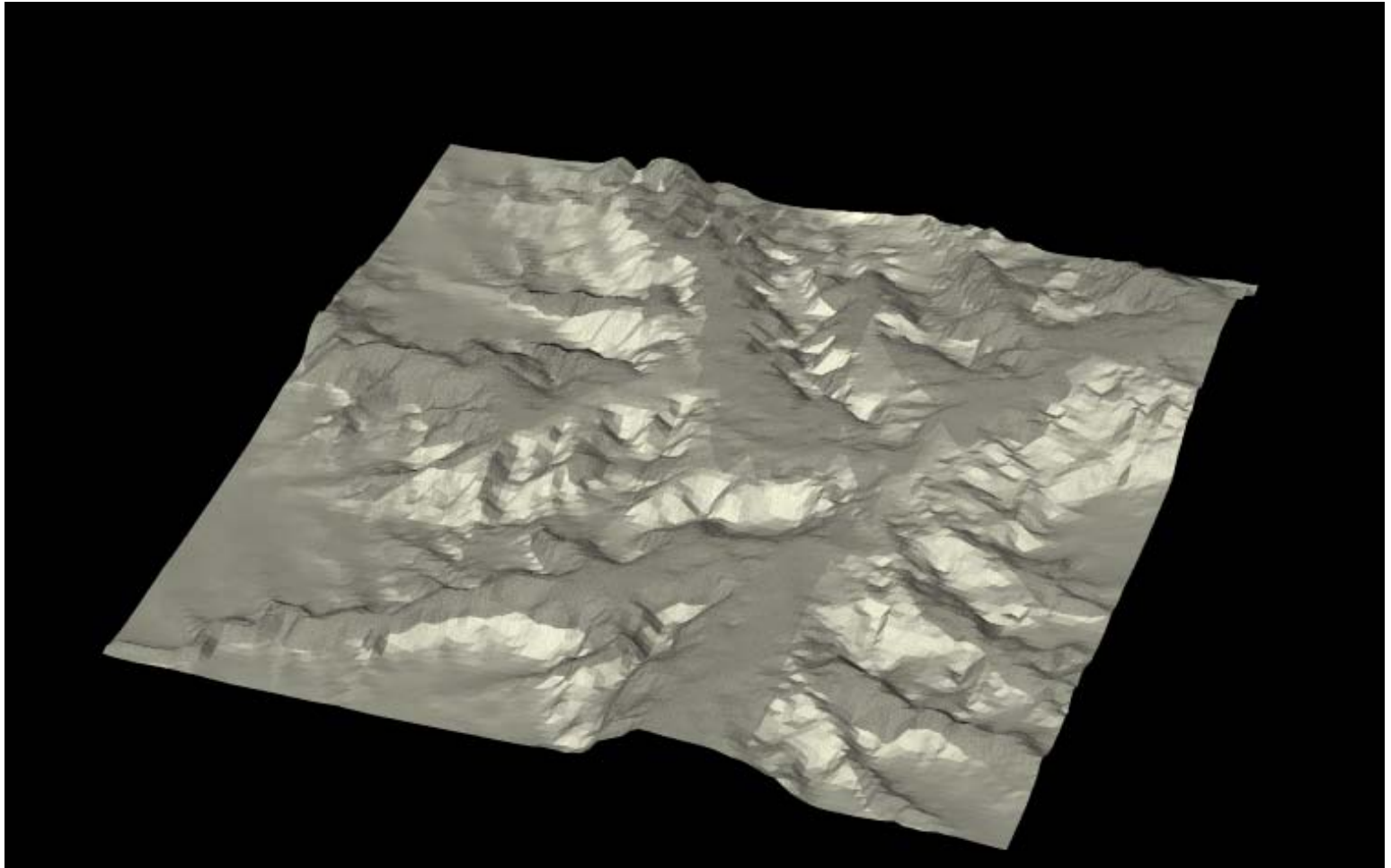
# Mesh Resources

- Google Sketchup Model (from <http://sketchup.google.com/3dwarehouse/>):
  - Import .skp model into Rhino3D (or other package)
  - Scale model if needed (reverse axis)



# Mesh Resources

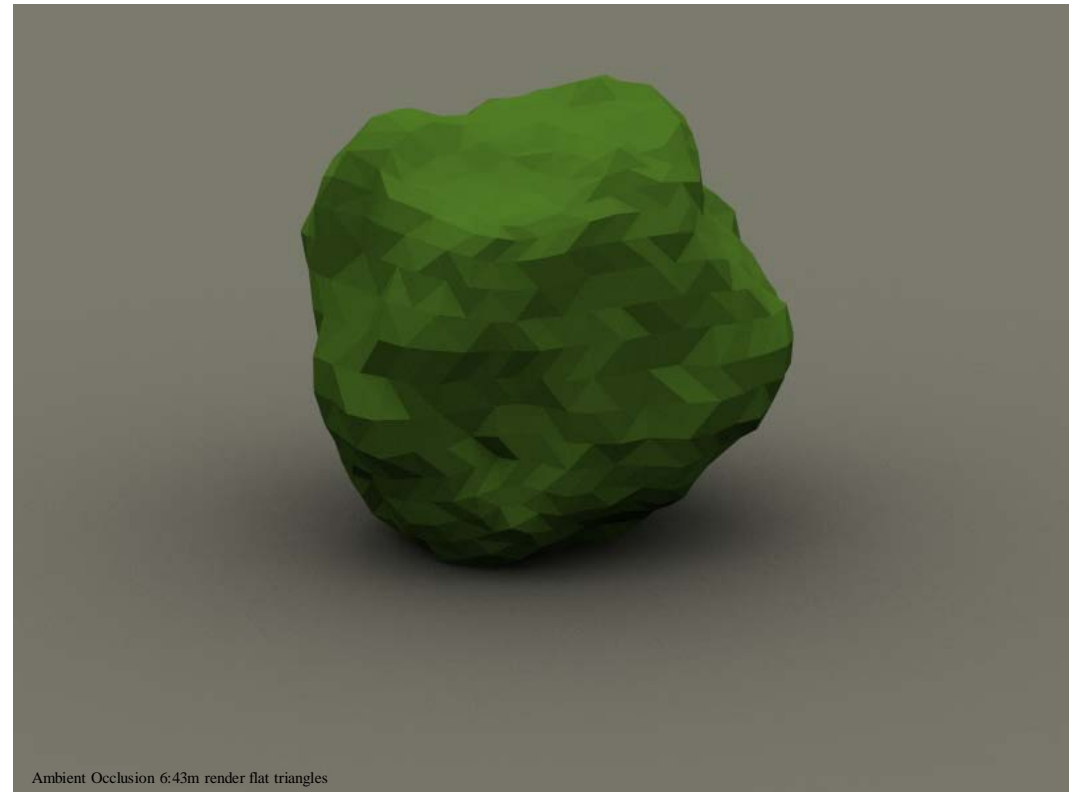
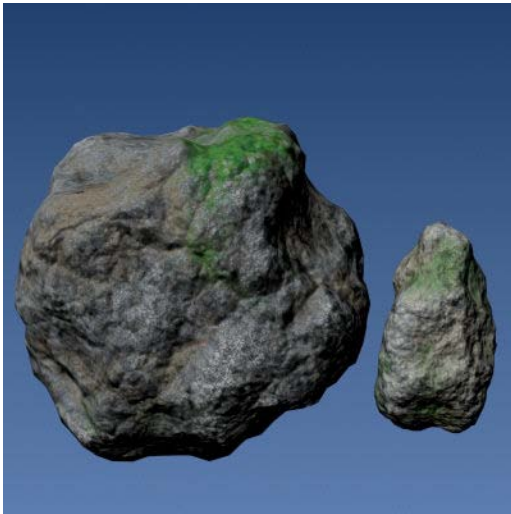
- Export to .ply format, property list uchar uint vertex\_index => property list uchar uint vertex\_indices





# Mesh Resources

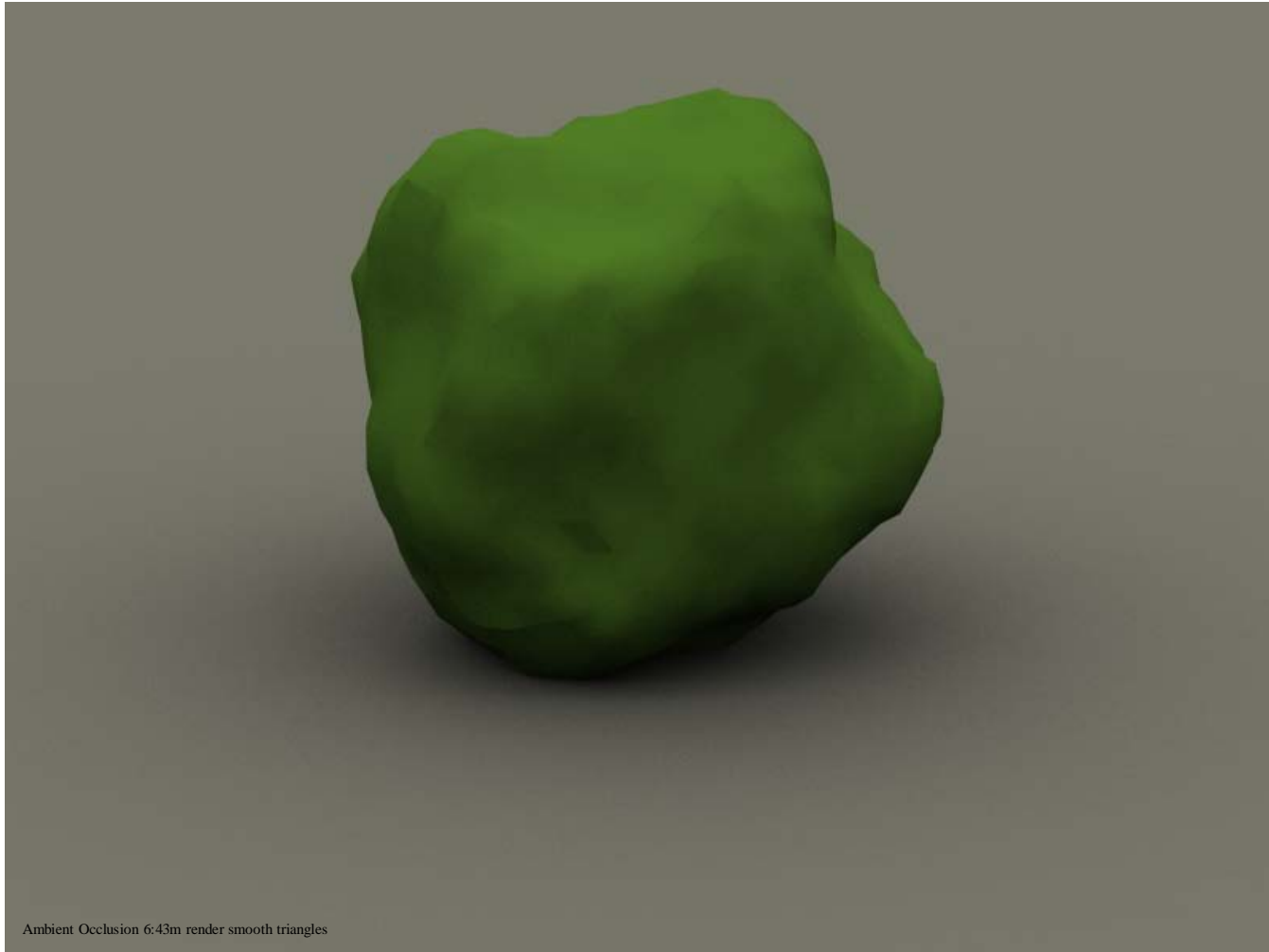
- TurboSquid (<http://www.turbosquid.com/>) is a 3d Marketplace that provides artists an outlet for selling models. Some free models exist on the site...



Ambient Occlusion 6:43m render flat triangles

# Mesh Resources

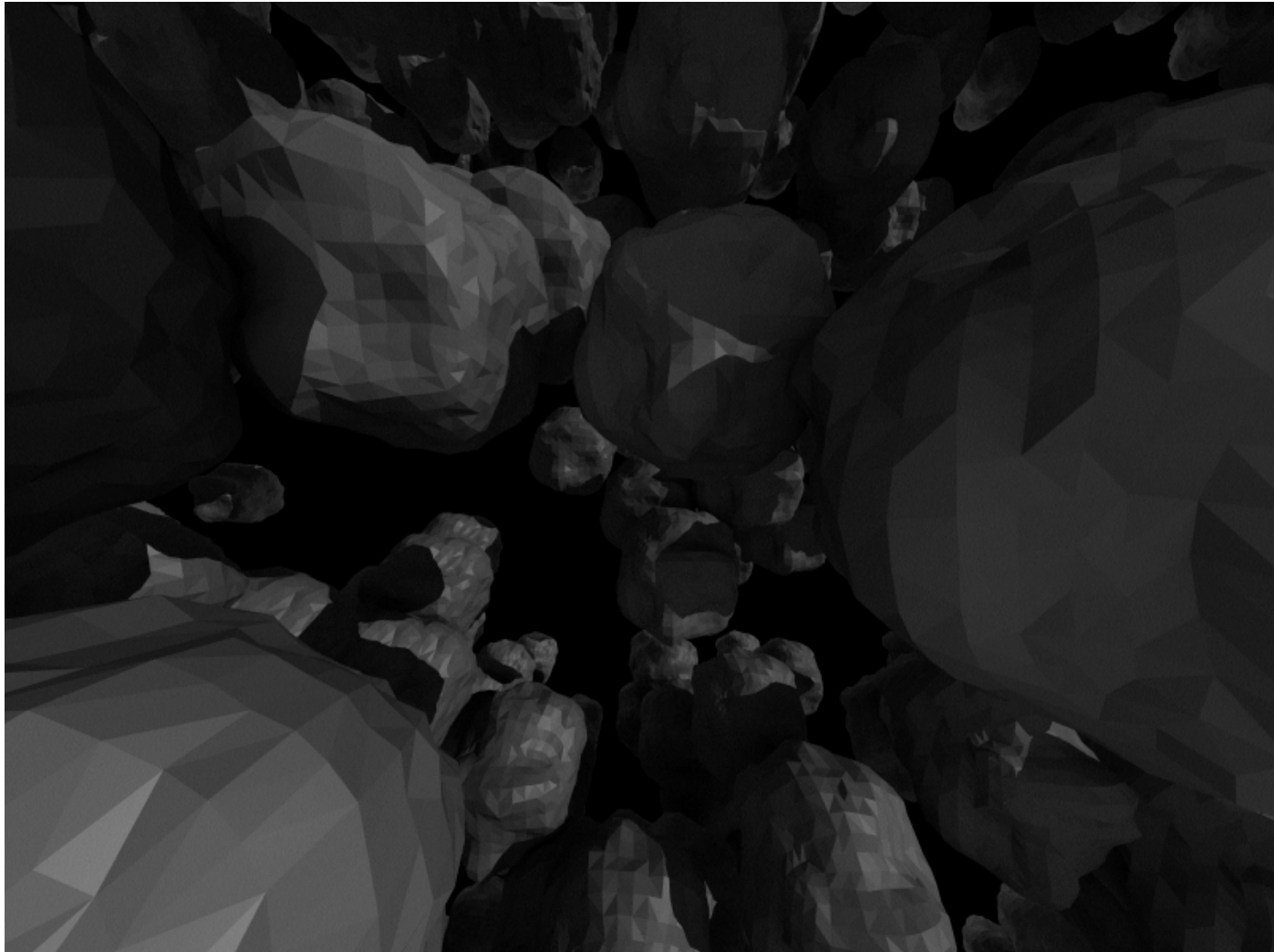
- w/smooth shaded triangles



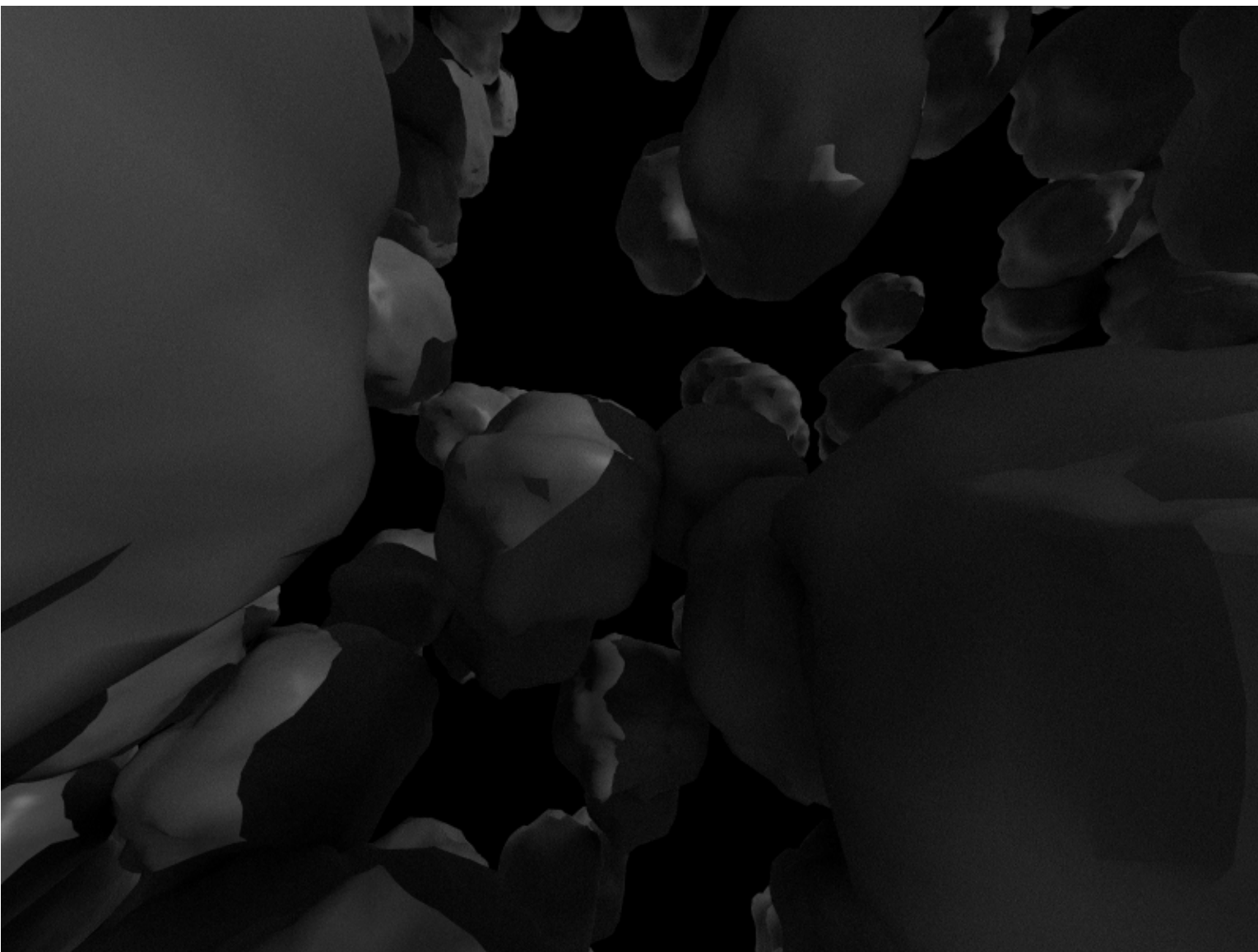
Ambient Occlusion 6:43m render smooth triangles

# Hierarchical Grids

- Hierarchical Grids: Create instances that contain some number of an object. Why?  
Example : Asteroid Field.... (7 hour render time, 4.5M memory used, 1 Stone 4.1M)



# Hierarchical Grids



# Mesh Resources

- Vehicles:

<http://dmi.chez-alice.fr/models1.html>

[http://www.planit3d.com/source/meshes\\_files/vehicles01.htm](http://www.planit3d.com/source/meshes_files/vehicles01.htm)

<http://www.3dtotal.com/pages/meshes/meshvehicles.php>

- Human Forms:

[http://www.3dtotal.com/pages/meshes/meshhuman\\_a.php](http://www.3dtotal.com/pages/meshes/meshhuman_a.php)

- Furniture, Architecture:

<http://archive3d.net/>

<http://www.3dmodelfree.com/>

- Space :

<http://hayabusa.sci.isas.jaxa.jp/shape.pl>

[http://www.nasa.gov/multimedia/3d\\_resources/3d-models-gallery.html](http://www.nasa.gov/multimedia/3d_resources/3d-models-gallery.html)<http://space.jpl.nasa.gov/models/>

- Various:

[http://www.cc.gatech.edu/projects/large\\_models/](http://www.cc.gatech.edu/projects/large_models/)

## References

- Suffern, Kevin (2007). Ray Tracing from the Ground Up. p. 473-490
- <http://www.3dm3.com/visits/1096>
- <http://www.iqcmm.com/>
- <http://www.zcorp.com>