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# The SMV language

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#### **Abstract:**

This document describes the current state of the input language used by the SMV model checker.

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# **SMV** language overview

The SMV language can be divided roughly into three parts - the definitional language, the structural language, and the language of expressions. The definitional part of the language declares signals and their relationship to each other. It includes type declarations and assignments. The structural part of the language combines definitional components. It provides language constructs for defining modules and structured data types, and for instantiating them. It also provides constructor loops, for describing regularly structured systems, and a collection of conditional structures that make describing complicated state transition tables easier. Finally, expressions in SMV are very similar to expressions in other languages, both hardware description languages and programming languages. For this reason, expressions will be discussed last, as any expressions appearing in discussions of other parts of the language should be self explanatory.

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# Data types and type declarations

A type declaration is of the form

<signal> : <type>;

where <signal> is the name of a signal and <type> is the set of values that the signal may take.

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### Boolean, enumerated and subrange types

The simple types are *boolean*, *enumerated* and *subrange*. The type `boolean' is simply an abbreviation for the set {0,1}. Thus,

foo : boolean;

declares a signal named ``foo", which can take on the value 0 or 1. An enumerated type is a set of symbols. For example,

bar : {ready, willing, able};

declares a signal named ``bar", which can take one of the symbolic values ``ready", ``willing" or ``able". A type can also be a subrange of the integers. For example,

count : 0..7;

declares a signal ``count" which can take any value inclusively in the range from 0 to 7. Numeric values in type declarations may also be expressions, consisting of numeric constants, and the numeric operators +, -, \*, /, mod, <<, >> and \*\* (see section 9).

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## **Arrays**

An array of signals is declared in the following way:

```
<signal> : array <x>...<y> of <type>;
```

This declares a collection of signals of type <type>, with subscripts running from <x> to <y>. For example, the declaration

```
zip : array 2..0 of boolean;
```

is equivalent to declaring.

```
zip[2] : boolean;
zip[1] : boolean;
zip[0] : boolean;
```

An element of an array can be referenced by adding a subscript in square brackets. The subscript must evaluate to an integer in the declared range of the array.

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## **Multidimensional arrays**

Arrays of arrays can also be declared. For example,

```
matrix : array 0..1 of array 2..0 of boolean;
is equivalent to

matrix[0] : array [2..0] of boolean;
matrix[1] : array [2..0] of boolean;
```

The boolean signals declared in this way are

```
matrix[0][0] matrix[0][1] matrix[0][2] matrix[1][0] matrix[1][1]
```

There is no fixed limit to the number of dimensions of an array declared in this way.

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### **Generic arrays**

Note that an array in SMV is not really a data type. It is simply a collection of signals with similar names. This means that it is possible to declare an ``array" whose elements have different types, by simply declaring the elements individually. For example:

```
state[0] : {ready, willing};
state[1] : {ready, willing, able};
state[2] : {ready, willing, able, exhausted};
```

See section <u>10.10</u>, however, for a discussion on the consequences of such a declaration for array references in expressions.

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#### **Structure**

A structure is a collection of signals that are referred to by symbolic names, rather than numeric subscripts. A structure declarion has this form:

```
foo : struct {
    c1 : type1;
    c2 : type2;
    ...
    cn : typen;
}
where c1...cn are symbolic names. This declaration is exactly equivalent to the declarations:
foo.c1 : type1;
foo.c2 : type1;
...
foo.cn : type1;
```

That is, like an array, a structure is simply a collection of signals with similar names.

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# Signals and assignments

A value of a signal is an infinite sequence of values of a given type. For example,

0;1;0;1;...

is a sequence of type boolean (of course, it is also an integer sequence). Normally, we interpreted this sequence as being a sequence of values occurring over time, although this interpretation is not necessary.

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### **Operations on signals**

An operator is applied to a signal value one element at a time. For example, the operator ~ stands for logical ``not". Thus if

```
foo = 0;1;0;1;...

~foo = 1;0;1;0;...
```

That is, it is the result of applying logical ``not" to each element of the sequence. Similarly, & stands for logical ``and". Thus, if

```
foo = 0;1;0;1;...
and bar = 0;0;1;1;...
then
foo & bar = 0;0;0;1;...
```

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then

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## **Assignments**

An assignment is of the form

```
<signal> := <expr>;
```

where <expr> is an expression that combines other signals using operators like ~ and &. Unlike an assignent in a typical ``procedural" language, this assignment means exactly what it says: that <signal> is equal to <expr>. So for example, suppose we make the assignment

```
zip := foo & bar;
```

If foo and bar are as above, then

$$zip = 0;0;0;1;...$$

The assignments in an SMV program are interpreted as equations holding *simultaneously*. That is, the fact that two assignments occur in sequence in a program is not interpreted to mean that they are to hold sequentially. Thus, for example, if these assignments appear in a program:

```
y := x + 1;

z := y + 1;
```

then we have (at all times) z = x + 2.

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## Unit delay assignments - the "next" operator

A special operator is provided for describing *recurrences*. Recurrences are circular or recursive systems of equations, and are the way that sequential systems are described in SMV.

If x is a signal, then next(x) is, intuitively, the "next" value of x. More precisely, the *i*th value of next(x) is equal to the (i+1)st value of x. Thus, for example, if

$$x = 0, 1, 2, 3, ...$$

then

$$next(x) = 1, 2, 3, 4, ...$$

By assigning a value to the "next" value of a signal, we can define a sequential machine. For example, assuming x and y are boolean signals,

$$next(x) := y ^ x;$$

defines a signal x which ``flips" each time the signal y is true (the ^ operator stands for ``exclusive or"). By definiton, the ``next" value of x is equal to  $(y ^ x)$ , which is equal to x if y is false and  $\sim x$  if y is true. Note, however, that the above assignment does not tell us the initial value of x. Thus, we obtain a different sequence depending on whether x starts at 0 or 1. We can determine this initial value by assigning

$$init(x) := 0;$$

In this case, if we had

$$y = 0;1;0;1;...$$

we would get

$$x = 0;0;1;1;0;0;1;1;...$$

On the other hand, if we assigned

$$init(x) := 1;$$

we would obtain the sequence

$$x = 1;1;0;0;1;1;0;0;...$$

Unit delay assignments - the ``next" operator

As another example, to declare a signal x that maintains a running sum of the values of a signal y, we would say

$$init(x) := 0;$$
  
 $next(x) := x + y;$ 



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#### State machines

Here is an example of a small finite state machine, expressed in SMV. It starts in a state ``idle" and waits for a signal ``start" to be asserted. On the next cycle, it changes to a state ``cyc1", then to state ``cyc2", then returns to ``idle". In state ``cyc2", it asserts a signal ``done":

```
start,done : boolean;
state : {idle,cyc1,cyc2};

next(state) :=
   switch(state){
    idle: start ? cyc1 : idle;
      cyc1: cyc2;
      cyc2: idle;
   };

done := (state = cyc2);
```

This illustrates two forms of conditional expressions in SMV. The ``switch" operator evaluates its argument ``state", then chooses the first expression in the curly brackets that is tagged with that value. Thus, if state = cyc1, then the value of the switch expression is cyc2. There is also a simpler form of conditional expression, that appears in the example as

```
start ? cyc1 : idle

If ``start" is true, this evaluates to ``cyc1", else to ``idle".
```

The above state machine can be expressed more `procedurally' using the structural conditional constructs described in the next section. We would write:

```
default done := 0;
in switch(state){
  idle:
    if start then next(state) := cyc1;
    cyc1:
      next(state) := cyc2;
    cyc2:
      next(state) := cyc2;
      done := 1;
}
```

This style of expression is semantically equivalent to the previous one, but can be much more readable for large complex state machines. The conditional constructs are only syntactic however, and can always be viewed as an abbreviation for a collection of simple assignment statements.

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# Rules for assignments

An SMV program amounts simply to a system of simultaneous equations, with a set of unknowns that are the declared signals. With an arbitrary set of equations, there is, of course, no guarantee that a solution exists, or that the solution is unique. Examples of systems that have no solutions are

```
x := x + 1;
next(x) := x + 1;
next(x) := x - 1;
```

An example of a system with many solutions is

```
x := y;

y := x;
```

We avoid these difficulties by placing certain rules on the structure of assignments in a program. These rules guarantee that every program is ``executable". This means, among other things, that a schedule must exist for computing the elements of all the sequences. The rules for assignments are:

- The single assignment rule each signal may be assigned only once.
- The circular dependency rule a program may not have ``cycles" in its dependency graph that are not broken by delays.
- The single assignment rule
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## The single assignment rule

SMV follows a "single assignment" rule. This means that a given signal can be assigned only once in a program. Thus, we avoid the problem of conflicting definitions. The definition of "single assignment" is compicated somewhat by the "next" and "init" operators. The rule is this: one may either assign a value to x, or to next(x) and init(x), but not both. Thus, the following are legal:

x := foo;	next(x) := foo;	
init(x) := foo;	init(x) := foo;	
	next(x) := bar;	

while the following are illegal:

x := foo;	next(x) := foo;	
x := bar	next(x) := bar;	
x := foo;	x := foo;	
init(x) := bar;	next(x) := bar;	

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### The circular dependency rule

If we have the assignment

$$x := y;$$

then we say that x *depends on* y. A *combinational loop* is a cycle of dependencies that is unbroken by delays. For example, the assignments

$$x := y;$$
  
 $y := x;$ 

form a combinational loop. Although as equations, they may have a solution, there is no fixed order in which we can compute x and y, since the *i*th value of x depends on the *i*th value of y and vice versa.

To be more precise, an assignment of form

```
next(x) := <expr>;
```

introduces ``unit delay dependencies". There is a unit delay dependency from x to every signal refernced in < expr>. An assignment of the form

```
<signal> := <expr>;
```

introduces ``zero delay dependencies", in the same way. A combinational loop is a cycle of dependencies whose total delay is zero. Combinational loops are illegal in SMV.

Therefore, legal SMV programs have the following property: for any sequence values chosen for the unassigned (free) signals, there is at least one solution for the assigned signals. There may be multiple solutions in the case where a signal has an unassigned initial value, or the case of nondeterministic assignments (see below).

There are cases where a combinational loop `makes sense", in that there is always a solution of the equations. In this case, the order in which signals are evaluated may be conditional on the values of some signals. For example, take the following system:

$$x := c ? y : 0;$$
  
 $y := \sim c ? x : 1;$ 

If c is false, then we may first evaluate x, then y, obtaining x = 0, then y = 0. On the other hand, if c is true, we may first evaluate y, then x, obtaining y = 1, then x = 1. The existence of conditional schedules such as this is difficult to determine, since it may depend on certains states (or signal values) being ``unreachable''. For example, if we have

```
x := c ? y : 0;

y := d ? x : 1;
```

it may be the case that c and d are never true at the same time, in which case x and y can always be evaluated in some order. Loops of this kind do sometimes occur in hardware designs (especially in buses and ring-structured arbiters). It is possible that at a future time the definition of a combinational to could be relaxed in order to allow such definitons. Currently, however, combination loops are defined only in terms of syntactic dependencies.

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#### Range violations and unknown values

By definition, a signal's value is always in the range of its type. When a signal is assigned a value that is not an element of its declared type, the resulting value of the signal is not defined by the SMV semantics, except that it must be a value in the type of the signal.

Another way to view this is that any assignment

```
x := expr;
```

is treated as if it were a shorthand for:

```
x := (expr in TYPE) ? expr : TYPE;
```

where TYPE is the set of values in the type of signal x. This means that if the value of expr is not in the set TYPE, then the value of x is chosen nondeterministically from the set TYPE. See the next section for a discussion of nondeterministic choice.

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## Order of assignments and declarations

Because assignments are treated as a system of simultaneous equations (or inclusions), the order in which assignments appear in the program is irrelevant to the program's semantics. There may also be multiple type declarations for a given signal, provided they all agree on the type. Type declarations and assignments may appear in any order.

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# Nondeterministic assignments

Especially in the early stages of a design, a designer may not want to completely specify the value of a given signal. Incomplete specification may represent either a design choice yet to be made, incomplete information about the environment of a system, or a deliberate abstraction made to simplify the verification of a system. For this purpose, SMV provides *nondeterministic* choice. A nondeterministic choice is represented by a set of values. If we make the assignment

```
signal := \{a,b,c,d\};
```

then the value of signal is chosen arbitrarily from the set {a,b,c,d}. As another example, suppose that in our previous state machine, we don't want to specify how many cycles will be spent in state ``cyc1". In this case, we could write:

```
next(state) :=
  switch(state) {
    idle: start ? cyc1 : idle;
    cyc1: {cyc1,cyc2};
    cyc2: idle;
};
```

Note that in case state = cyc1, the value of the switch expression is the set {cyc1,cyc2}. This means that the next value of ``state" may be either ``cyc1" or ``cyc2". In general, the mathematical meaning of the assignment

```
x := y;
```

where y is a set of values, is that x is *included in* the set y. Ordinary values are treated as sets of size one. Thus, properly speaking, an SMV program is a simultaneous set of inclusions, rather than equations.

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## Assignments to arrays of signals

Technically, each assignment is only to one signal. However, it is possible to write an assignment to an array element whose subscript is not a constant. This is treated as a collection of assignments to all the declared elements in the array. For example, suppose the x is declared as an array, as follows:

```
x : array 0...3 of boolean;
```

and suppose y is an expression involving a signal (i.e., not a constant expression). Then the statement:

```
next(x[y]) := expr;
```

is treated as an abreviation for the array of assignments:

```
if(y=0) next(x[0]) := expr;
if(y=1) next(x[1]) := expr;
if(y=2) next(x[2]) := expr;
if(y=3) next(x[3]) := expr;
```

This syntactic interpretation has two important consequences. First, although the "next" value of x is assigned, the subscript y is evaluated at the "current" time. This is in accordance with what we would expect to occur in a procedural language. Second, this statement effectively assigns all of the elements of the array. This means that, for example, the following is a violation of the single assignment rule:

```
x[0] := foo;
x[count + 1] := bar;
```

This makes sense, since it is not possible to determine statically whether 0 and count +1 refer to the same element of the array.

A practical note: if you want to make two assignments to variable indices in the same array, you can use use the ``default" construct (described below). That is, the following is legal:

```
default next(x[i]) := foo;
in next(x[j]) := bar;
```

In the case where i = j, the second assignment takes precedence, and thus there are no simultaneous assignments.

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## **Modules**

A *module* is a bundle of definitions (type declarations and assignments) that can be reused. Much like a subroutine, a module may have *formal parameters*. When creating an *instance* of the module, actual signals or expressions are plugged in for the formal parameters, thus linking the module instance into the program. Most often the formal parameters of a module are declared to be either inputs or outputs. Inputs are expected to be assigned outside the module, whereas outputs are expected to be assigned inside the module.

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#### **Module declarations**

As an example, suppose we want to construct a binary counter, by designing a counter ``bit", and then chaining the bits together to form a counter. In SMV, the counter bit might be declared as follows:

```
MODULE counter_bit(carry_in, clear, bit_out, carry_out)
{
   INPUT carry_in, clear : boolean;
   OUTPUT bit_out, carry_out : boolean;
   next(bit_out) := clear ? 0 : (carry_in ^ bit_out);
   carry_out := carry_in & bit_out;
}
```

The ``INPUT" and ``OUTPUT" declarations are specialized forms of type declarations, which also give the direction of signals being declared. These declarations must occur before any ordinary type declarations or assignments.

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#### **Instantiations**

To create a three-bit counter, we can now write, for example:

```
clear : boolean;
count : array 2..0 of boolean;
carry : array 3..0 of boolean;
bit0 : counter_bit(carry[0], clear, count[0], carry[1]);
bit1 : counter_bit(carry[1], clear, count[1], carry[2]);
bit2 : counter_bit(carry[2], clear, count[2], carry[3]);
```

Here, three *instances* of the module ``counter\_bit" are created. These instances have names ``bit0", ``bit1", ``bit2". Each instance is, in effect, a copy of the definitions in module ``counter\_bit". However, all the signal names referenced in the instance are prefixed with the instance name, so that they are unique to that instance. For example, the signals in module instance ``bit0" are:

```
bit0.carry_in
bit0.clear
bit0.bit_out
bit0.carry_out
```

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### Input and output declarations

The effect of the INPUT declaration is to make an assignment from the actual parameters to the corresponding formal parameters. Thus, in instance ``bit0", the declaration

```
INPUT carry_in, clear : boolean;
has the effect of assigning

bit0.carry_in := carry[0];
bit0.clear := clear;
```

Similarly, the effect of the OUTPUT declaration is to make an assignment from the formal parameters to the corresponding actual parameters. Thus, in instance ``bit0", the declaration

```
OUTPUT bit_out, carry_out : boolean;
has the effect of assigning

count[0] := bit0.bit_out;
carry[1] := bit0.carry_out;
```

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#### **Instance hierarchies**

Modules may, of course, contain instances of other modules, and so forth, provided the module references are not circular. So we can, for example, create three-bit counter module, as follows:

```
MODULE counter3(carry_in, clear, count, carry_out)
  INPUT carry_in, clear : boolean;
  OUTPUT count : array 2... of boolean;
  OUTPUT carry_out : boolean;
  carry: array 3...1 of boolean;
  bit0 : counter_bit(carry_in, clear, carry[0], carry[1]);
  bit1 : counter_bit(carry[1], clear, carry[1], carry[2]);
  bit2 : counter_bit(carry[2], clear, carry[2], carry[3]);
  carry_out := carry[3];
If we then instantiate this module with
        foo : counter(cin,clr,cnt,cout);
we will have, for example, an instance of counter_bit called foo.bit0, which defines signals
        foo.bit0.carry_in
        foo.bit0.clear
        foo.bit0.bit_out
        foo.bit0.carry_out
```

MODULE declarations may not appear inside other MODULE declarations, however. That is, all MODULE declarations must be in the outermost scope.

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### Structured data types

A module with only type declarations and no parameters or assignments acts like a structured data type. For example, to define a data structure ``hands" with fields ``left" and ``right", the following module might be defined:

```
MODULE hands()
{
  left, right : boolean;
}
```

An instance of this structured type can be created as follows:

```
party : hands();
```

This is exactly equivalent to

```
party.left, party.right : boolean;
```

The two fields of this record can be referenced as

```
party.left
party.right
```

In fact, any signal belonging to a module instance can be referenced directly by name in this way. Normally, however, it is recommended that only inputs and outputs be referenced.

An array of a given structured type may be created in the same manner as an array of signals. For example,

```
foo : array 1..0 of hands();
which would be equivalent to

party[1].left, party[1].right : boolean;
party[0].left, party[0].right : boolean;
```

As with signals, multidimensional arrays may be created.

Next: Conditionals Up: Modules Previous: Structured data types

## **Defined types**

A type definition (typedef) is a special kind of module declaration with no parameters, and a slightly different syntax. The definition of `hands' above can equivalently be written as

```
typedef hands struct{
  left, right : boolean;
}
```

The general form of this declaration is

```
typedef <name> <type>
where <type> is any legal type specification.
```

Next: Simple conditionals Up: The SMV language Previous: Defined types

## **Conditionals**

Assignments or groups of assignments may be made conditional. This is especially useful when several assignments all depend on the same condition - it avoids repeating the conditional structure in each assignment.

- Simple conditionals
- Defaults
- Complex conditionals switch and case

Next: Defaults Up: Conditionals Previous: Conditionals

#### Simple conditionals

The basic conditional structure is

```
if(<condition>)
  <stmt1>
else
  <stmt2>
```

A ``statement" can be either an assignment, or a group of statements delimited by curly brackets.

The effect of the statement

```
if(c)
    x := foo;
else
    x := bar;
```

is exactly equivalent to

```
x := c ? foo : bar;
```

If x is assigned in the ``if" part, but not assigned in the ``else" part, then x is undefined when the condition is false. This means that x can take any value in its type. Similarly, if x is assigned in the ``else" part, but not in the ``if" part, then x is undefined when the condition is true. For example,

```
if(c)
    x := foo;
else
    y := bar;
```

is equivalent to

```
x := c ? foo : undefined;
y := c ? undefined : bar;
```

Mathematically, undefined is the set of all possible values.

If next(x) is assigned in one part of the conditional, but not the other, then

```
next(x) = x;
```

is the default. For example,

```
if(c)
    next(x) := foo;
else
    next(y) := bar;
is equivalent to

next(x) := c ? foo : x;
next(y) := c ? y : bar;
```

Conditionals are statements, and therefore can be nested inside conditionals. Groups of statements can also be nested inside conditionals. For example:

```
if(c)
{
    x := foo;
    if(d)
        next(y) := bar;
    else
        next(z) := bar;
}
else
    x := bar;
```

The ``else" part may be omitted, although this is hazardous. It can result in an ambiguity as to which ``if" a given ``else" corresponds to, if there are nested conditionals. Care should be take to use curly braces to disambiguate. Thus, instead of:

```
if(c)
    if(d)
        <stmt>
    else
        <stmt>
the prefered usage is:

if(c){
    if(d)
        <stmt>
    else
        <stmt>
    }
```

The effect of:

if(c)

Simple conditionals
<stmt>

is equivalent to:

if(c)
 <stmt>
else {}

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Next: Defaults Up: Conditionals Previous: Conditionals

Next: Complex conditionals - switch Up: Conditionals Previous: Simple conditionals

#### **Defaults**

The ``default" construct provides a way of automatically filling in the cases where a signal is undefined with a default value. The syntax is:

```
default
     <stmt1>
in
     <stmt2>
```

The effect of this statement is to use the assignments in <stmt1> in any cases in <stmt2> where the given signal is unassigned. For example,

```
default
    x := foo;
in
{
    if(c)
    {
        x := bar;
        next(y) := y + 1;
    }
    else
        next(y) := y + 2;
}
```

is equivalent to

```
next(y) := c ? y + 1 : y + 2;
 x := c ? bar : foo;
```

An assignment to next(x) may also appear in the default statement. The effect is again to insert the default assignment in any cases where next(x) is not defined. Default statements may be nested inside conditionals, and vice-versa, and groups of statements may appear in both the ``default" part and the ``in" part.

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Next: Constructor loops Up: Conditionals Previous: Defaults

#### Complex conditionals - switch and case

The complex conditionals are ``case" and ``switch". A ``case" statement has the form:

This statement is exactly equivalent to

```
if (<cond1>) <stmt1>
else if (<cond2>) <stmt2>
...
else if (<condn>) <stmtn>
[else <dfltstmt>]
```

Note this means that if all the conditions are false, and there is no default statement, then no assignments are made.

A ``switch" statement has the form:

This is exactly equivalent to:

```
case{
    <expr> in <case1> : <stmt1>
    <expr> in <case2> : <stmt2>
    ...
    <expr> in <casen> : <stmtn>
    [default : <dft1stmt>]
```

```
Complex conditionals - switch and case }
```

Note that the set inclusion operator ``in" is used instead of ``=". This means that each case may be a set of values rather than a single value. For example, if we want a counter that waits for a signal ``start", counts to seven, asserts a signal ``done", and resets, we might write:

```
default
  done := 0;
in
  switch(count){
    0 : if start then next(count) := 1;
    1..6 : next(count) := count + 1;
    7 : {
       next(count) := 0;
       done := 1;
    }
}
```

Next: Basic for-loops Up: The SMV language Previous: Complex conditionals - switch

# **Constructor loops**

A looping construct is provided for expressing regular structures more succinctly. Loops are simply unrolled by the compiler into the equivalent `in-line" code.

- Basic for-loops
- Creating arrays of instances
- Creating parameterized modules
- Chained constructor loops

Next: Creating arrays of instances Up: Constructor loops Previous: Constructor loops

#### **Basic for-loops**

For example,

```
for(i = 0; i < 3; i = i + 1){
   x[i] := i;
}</pre>
```

is in every way equivalent to

```
x[0] := 0;

x[1] := 1;

x[2] := 2;
```

The general form of the loop is

The loop is unrolled in the following way: initially, var is set to init. Then, while cond is true, stmt is instantiated, and var is set to next. The loop variable var may appear in stmt. Each occurrence of var is replaced by its current value.

Next: Creating parameterized modules Up: Constructor loops Previous: Basic for-loops

#### **Creating arrays of instances**

One important use of loops is to create arrays of module instances. For example, to create a three bit counter as an array of counter bits, we could write:

```
bits : array 2..0;
for(i = 0; i < 2; i = i + 1)
  bits[i] : counter_bit(carry[i],clear,count[i],carry[i+1]);</pre>
```

Note that bits is first declared as a generic array. Then the elements of the array are `filled in' inside the loop. In this way, each counter bit is connected to the appropriate signal, as a function of the loop index i.

Also note that module instances can be nested inside conditionals, provided that the condition evaluates to a constant at compile time. Since loops are unrolled at compile time, a loop index counts as a constant. Thus, for example, if we want to use a special module ``special\_bit" for bit 0 of the counter, we could write:

```
bits : array 2..0;

for(i = 0; i < 2; i = i + 1){
   if(i = 0)
      bits[i] : special_bit(carry[i],clear,count[i],carry[i+1]);
   else
      bits[i] : counter_bit(carry[i],clear,count[i],carry[i+1]);
}</pre>
```

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Next: Chained constructor loops Up: Constructor loops Previous: Creating arrays of instances

#### Creating parameterized modules

Compile time constants can also be passed as parameters to modules. This allows us to write a generic n-bit counter module, which takes n as a parameter:

```
MODULE nbit_counter(n,carry_in,clear,count,carry_out)
{
   INPUT carry_in, clear : boolean;
   OUTPUT count (n - 1)..0 : boolean;
   OUTPUT carry_out : boolean;

   bits : array (n - 1)..0;
   carry : array n .. 0 of boolean;

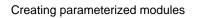
   for(i = 0; i < n; i = i + 1)
       bits[i] : counter_bit(carry[i],clear,count[i],carry[i+1]);

   carry_out := carry[n];
}</pre>
```

The ability to nest module instances inside conditionals even makes it possible to write recursively defined modules. For example, the following code builds an n-input ``or" gate as a balanced tree of 2-input ``or" gates:

```
MODULE or_n(n,inp,out)
{
    INPUT inp : array 0..(n - 1) of boolean;
    OUTPUT out : boolean;

    case{
        n = 1 : out := inp[0];
        n = 2 : or2(inp[0],inp[1],out);
        default: {
            x,y : boolean;
            or_n(n / 2, inp[0 .. (n / 2 - 1)], x);
            or_n(n - n / 2, inp[(n / 2) .. n], y);
            or_2(x,y,out);
        }
    }
}
```



Next: Expressions Up: Constructor loops Previous: Creating parameterized modules

#### **Chained constructor loops**

It is commonly necessary to select the first element of an array satisfying a certain condition, or to perform some other computation involving prioritizing an array. A looping construct called ``chain" is provided for this purpose. It acts exactly like a ``for" loop, except that the assignments in one iteration of the loop act as defaults for the assignments in subsequent iterations. This makes it possible to assign a signal in more than one iteration of the loop, with the later assignment taking priority over the earlier assignment.

For example, suppose we want to specify a `priority encoder', that inputs an array of signals, and outputs the index of the highest numbered signal that is true. Here is a priority encoder that inputs an array of boolean signals of size `n':

```
MODULE priority_n(n,inp,out)
{
   INPUT inp : array 0..(n - 1) of boolean;
   OUTPUT out : 0..(n-1);

   chain(i = 0; i < n; i = i + 1)
      if (inp[i]) out := i;
}</pre>
```

Depending on the contents of the array `inp", the signal `out" might be assigned many times in different iterations of the loop. In this case, the last assignment is given precedence.

The construct:

is in every way equivalent to:

```
default
  <stmt with i = 0>
in default
  <stmt with i = 1>
in default
  <stmt with i = 2>
in
  <stmt with i = 3>
```

Chained of	constructor	loops
------------	-------------	-------

Next: Parentheses and precedence Up: The SMV language Previous: Chained constructor loops

## **Expressions**

An ``expression" combines signals using a collection of operators. These operators include:

- boolean operators (``and", ``or", ``not" and ``xor"),
- conditional operators (``if-then-else", ``case" and ``switch")
- arithmetic operators (``+", ``-", ``\*", ``/", ``mod", and shifts)
- comparison operators (``=", ``<", ``>", ``>=", ``<=")
- set operators (union, integer subrange and inclusion)
- vector operators (concatenation, subrange)
- conversion operations (integer to bit vector and vice versa)

Since signals are sequences of values, all of these operators apply to the elements of a sequence one-by-one. Thus, if

$$x = x_1, x_2, x_3, \dots$$

$$y = y_1, y_2, y_3, \dots$$

and • is a binary operator, then

$$x \cdot y = (x_1 \cdot y_1), (x_2 \cdot y_2), (x_3 \cdot y_3), \dots$$

The following describes the various operators as they apply to individual values.

- Parentheses and precedence
- Integer constants
- Symbolic constants

#### Expressions

- Boolean operators
- Conditional operators (``if", ``case" and ``switch")
- Representing state machines using conditionals
- Arithmetic operators
- Comparison operators
- Set expressions
  - o The set inclusion operator
  - Extension of operators to sets
  - o Comprehension expressions

Next: Integer constants Up: Expressions Previous: Expressions

#### Parentheses and precedence

Parentheses ``()" may always be put around an expression, without changing its value. If parentheses are omitted, then the order of operators is determined by their priority. The operators are listed here in order of priority, from ``strongest binding" to ``weakest binding":

```
::
                    (concatenation)
                    (unary minus sign)
* , / , << , >>
                    (mult, div, left shift, right shift)
+,-
                    (add, subtract)
mod
                    (integer mod)
                    (set inclusion)
in
union
                    (set union)
                    (comparison operators)
=,~=,<,<=,>,>=
                    (not)
                    (and)
&
                    (or, exclusive or)
                    (iff)
<->
                    (implies)
->
                    (tuple separator)
                    (conditional)
?:
                    (integer subrange)
```

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Next: Symbolic constants Up: Expressions Previous: Parentheses and precedence

## Integer constants

Integer constants may appear in expressions, and are optionally signed decimal numbers in the range  $2^{-31}\dots(2^{31}-1)$ .

Next: Boolean operators Up: Expressions Previous: Integer constants

## Symbolic constants

Symbolic constants may be declared by including them in a type declaration, such as,

```
x : {ready, willing, able};
```

The three symbols ready, willing and able are treated as distinct constants, which are also distinct from all the integers. A given symbolic constant may not appear in two different types. For example,

```
x : {foo, bar, baz};
y : {red, green, foo};
```

is illegal, since foo appears in two distinct types. This restriction is made so that programs may be type checked.

Next: Conditional operators (`if", ``case" Up: Expressions Previous: Symbolic constants

#### **Boolean operators**

The boolean operators are ``&", for logical and, `` | " for logical or, ``~" for logical not, ``^" for exclusive or , ``->" for implies, and ``<->" for if-and-only-if (exclusive nor). The boolean values are 0 (false) and 1 (true).

The ``&" operator obeys the following laws:

If neither x nor y is a boolean value, then  $x \in y$  is undefined. (recall that an ``undefined' expression yields the set of all possible values, which in the case of a boolean expression is  $\{0,1\}$ ). In particular,

```
1 & undefined = undefined
0 & undefined = 0
```

That is, ``undefined" values behave like ``X" values in typical logic simulators. You can write an undefined value as simply  $\{0,1\}$ .

Also note that

$$1 \& 37 = 37$$
  
 $0 \& 37 = 0$   
 $37 \& 37 = undefined$ 

The other boolean operators behave similarly, obeying:

$$x \leftarrow y = \sim (x \land y)$$

Conditional operators (``if", ``case" and ``switch")

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Next: Representing state machines using Up: Expressions Previous: Boolean operators

## Conditional operators (``if", ``case" and ``switch")

The simple conditional operator has the form

```
x ? y : z
```

It yields y if x is 1 (true) and z if x is 0 (false). If x is not a boolean value, it yields undefined.

The complex conditionals are ``case" and ``switch". The expression

```
case{
   c1 : e1;
   c2 : e2;
   ...
   cn : en;
   [default : ed;]
}
```

is equivalent to

```
c1 ? e1 : c2 ? e2 : ... cn ? en : ed
```

if there is a default case, and otherwise

```
c1 ? e1 : c2 ? e2 : ... cn ? en : undefined
```

That is, if all the conditions c1...cn are false, and there is no default case, then the case expression is undefined.

The expression

```
switch(x){
  v1 : e1;
  v2 : e2;
  ...
  vn : en;
  [default : ed;]
}
```

is equivalent to

```
(x \text{ in } v1) ? e1 : (x \text{ in } v2) ? e2 : ... (x \text{ in } vn) ? en : ed if there is a default case, and otherwise
```

Conditional operators (``if", ``case" and ``switch")

```
(x in v1) ? e1 : (x in v2) ? e2 : ... (x in vn) ? en : undefined
```

That is, the switch expression finds the first set vi that contains the value x, and returns the corresponding ei. The vi can also be single values - these are treated as the set containing only the given value.

Next: Arithmetic operators Up: Expressions Previous: Conditional operators (``if", ``case"

## Representing state machines using conditionals

As an example, suppose we have a state machine with one boolean input ``choice", that starts in state ``idle", then depending on ``choice" goes to either state ``left" or ``right", and finally returns to state ``idle". Using a ``case" expression, we could write:

```
next(state) :=
  case{
    state = idle : choice ? left : right;
    default : idle;
};
```

The equivalent using a switch statement would be:

```
next(state) :=
  switch(state) {
    idle : choice ? left : right;
    default : idle;
  };
```

The values in a switch statement can also be "tuples" (lists of expressions separated by commas, see section on tuples). Using this notation, we can write the above state machine as

If we want to add outputs ``left\_enable" and ``right\_enable" to our state machine, to indicate that the state is ``left" and ``right" respectively, we can use a switch expression that returns a tuple. Thus:

Representing state machines using conditionals

This provides a fairly succint way of writing the truth table of a state machine, with current state and inputs on the left, and next state and outputs on the right.

Next: Comparison operators Up: Expressions Previous: Representing state machines using

#### **Arithmetic operators**

The arithmetic operators are

```
+ addition
- subtraction and unary minus sign
* multiplication
/ integer division
mod remainder of division
<< left shift
>> right shift
```

All results of arithmetic on integers are modulo  $2^{32}$ , in the range  $-2^{31} \dots (2^{31}-1)$ .

The operators ``\*", ``/" and ``mod" obey the law

$$y * (x/y) + (x mod y) = x$$

The remainder is *always* positive.

The expression ``x << y" is equivalent to ``x \*  $2^y$ ". Similarly, ``x >> y" is equivalent to ``x /  $2^y$ ".

Next: Set expressions Up: Expressions Previous: Arithmetic operators

#### **Comparison operators**

The comparision operators are

```
= equal
~= not equal
< less than
> greater than
<= less than or equal
>= greater than or equal
```

When applied to integers, all return boolean values. The ``equal" and ``not equal" operators may also be applied to symbolic constants. Any integer is considered not equal to any symbolic constant. The inequality operators are undefined if either operand is a symbolic constant.

Next: The set inclusion operator Up: Expressions Previous: Comparison operators

## **Set expressions**

A set is specified as a list of elements between curly brackets:

```
{ elem, ..., elem }
```

Note that a set cannot be empty - there must be at least one element. Each element can be one of the following:

- An expression x. In this case, the value of x is included in the set. Note that if x itself represents a set of values, then all elements of x are included.
- ullet A subrange x . . y, where x and y are integer valued expressions. In this case all elements in the subrange x . . y are included in the set.
- A guarded expression c ? e. In this case, the value of e is included in the set if the condition c is true.

The set x . . y can be abbreviated to x . . y.

Note that a set expression may represent the empty set in the case that all elements are guarded, and all the guard conditions are false. In this case the result of the set expression is undefined. Thus, for example:

```
{1 ? foo, 1 ? bar} = {foo,bar}
{1 ? foo, 0 ? bar} = {foo}
{0 ? foo, 0 ? bar} = undefined
```

The reason for this rule is that a set expression is interpreted (with one exception, below) to represent a non-deterministic choice between the values in the set. A choice between the empty set of values is not meaningful.

- The set inclusion operator
- Extension of operators to sets
- Comprehension expressions

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Next: The concatenation operator Up: The SMV language Previous: Comprehension expressions

# Vectors and vector operators

A vector is a fixed-length sequence of values. Various operations are allowed on vectors, including concatenation, test for equality, and binary arithmetic and logical operators, which treat a vector as a binary number. Note, however, that a vector itself is not a `first class' value in SMV. That is, it is not possible for the value of a signal to be a vector. However, syntactic shorthands are provided that make it possible to treat vectors as if they were first class values.

A vector x of n elements is denoted by a non-empty, comma-separated list of elements within square brackets:

$$[xn, \ldots, x1, x0]$$

The *n*th element can be extracted from a vector by the function nth, which takes a vector as its first argument, and an integer as its second argument. The function nth numbers the elements of the vector from zero on the right. So, for example,

$$nth([5,4,3,2,1,0], 2) = 2$$

- The concatenation operator
- Extension of operators to vectors
- Vector coersion operator
- Arithmetic on vectors
- Comparison operators on vectors
- Vector sets
- Coercion of scalars to vectors
- Explicit coercion operators
- Coercion of array variables to vectors
- Generic arrays and vector coersion
- Array subranges
- Assignments to vectors
- Assignments to arrays

#### Vectors and vector operators

- Vectors as inputs and outputs
- <u>Iteratively constructing vectors</u>
- Reduction operators
- Vectors as conditions

Next: Extension of operators to Up: <u>Vectors and vector operators</u> Previous: <u>Vectors and vector operators</u>

## The concatenation operator

A vector may also be constructed using the concatenation operator `::". As an example,

```
(0 :: 1 :: 1 :: 0)
```

is a vector of length 4. That is, the 4 boolean values in this expression are treated as vectors of length 1, and concatenated to produce a vector of length 4.

The concatenation operator is associative. Thus, for example,

```
((0 :: 1) :: (1 :: 0)) = (0 :: 1 :: 1 :: 0)
```

Next: Vector coersion operator Up: Vectors and vector operators Previous: The concatenation operator

#### **Extension of operators to vectors**

Logical operators extend to vectors in the obvious way, by applying them one-by-one to the elements of the vector. That is, if f is a unary operator, then

$$f[x,y] = [f(x),f(y)]$$

For example,

$$\sim$$
 [0,1,0] = [1,0,1]

Binary logical operators extend similarly. That is, if \* is a binary operator, then

$$[w,x] * [y,z] = [w*y, x*z]$$

For example,

$$[0,1] & [1,1] = [0,1]$$

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Next: Arithmetic on vectors Up: Vectors and vector operators Previous: Extension of operators to

#### **Vector coersion operator**

When combining vectors of different length with a binary operator, the shorter vector is prepended with a vector of zeros to make the vectors the same length. Thus, for example,

$$[a,b,c,d] * [e,f]$$

is equivalent to

$$[a,b,c,d] * [0,0,e,f]$$

In general, if x and z are booleans, then

$$(w :: x) * z = (w * 0) :: (x * z)$$
  
 $x * (y :: z) = (0 * y) :: (x * z)$ 

The exceptions to the above rule are

- the arithmetic operators,
- the comparison operators, and
- the conditional operator
- the union and ``in" (set inclusion) operators

These exceptions are described below.



Next: Comparison operators on vectors Up: Vectors and vector operators Previous: Vector coersion operator

#### **Arithmetic on vectors**

Arithmetic operators applied to vectors treat the vectors as unsigned binary numbers. As stated above, if the vectors are of unequal length, the shorter vector is prepended with a vector of zeros to make the lengths equal. Thus

$$[0,1,1,0] + [1,0]$$

is equivalent to

$$[0,1,1,0] + [0,0,1,0]$$

The arithmetic operator is then applied to the unsigned binary numbers represented by the two vectors, yielding an unsigned binary representation of the result, of the same length as the argument vectors. The operators are the same as they are on integers, except the result is modulo  $2^n$ , where n is the vector

length. The result is always negative (in the range  $\hat{0} \dots (2^n - 1)$ ). For example,

$$[0,1,1,0] + [0,0,1,0] = [1,0,0,0]$$

and

$$[1,1,1,0] + [0,0,1,0] = [0,0,0,0]$$

Note that, since the arithmetic is modular, it doesn't actually matter whether we look at it as signed or unsigned, except that extension is always by zeros. This extension by zeros implicitly treats vectors as unsigned numbers.

Next: Vector sets Up: Vectors and vector operators Previous: Arithmetic on vectors

#### Comparison operators on vectors

Comparison operators on vectors operate in the same manner as arithmetic operators: the shorter vector is prepended with zeros, and the resulting vectors are compared as *unsigned* binary numbers.

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Next: Coercion of scalars to Up: Vectors and vector operators Previous: Comparison operators on vectors

#### **Vector sets**

The ``union" operator can be applied to vectors, to produce a set of vectors. In particular, one can express a nondeterministic choice between the vectors [0,1] and [1,0] by writing either

$$[0,1]$$
 union  $[1,0]$ 

Note that the following is not legal, however:

As with other operators, vectors are padded with zeros to the same length before the union operator is applied. The ``in" operator may also be applied to vetor sets. In general:

```
[a,b] in ([c,d] union [e,f]) is equivalent to
```

$$([a,b] = [c,d]) | ([a,b] = [e,f])$$

Next: Explicit coercion operators Up: Vectors and vector operators Previous: Vector sets

#### Coercion of scalars to vectors

An integer expression is *coerced* to a vector expression whenever:

- it is combined with a vector by a binary operator or conditional, or
- it is assigned to a vector of signals

The length of the vector representation of an integer is 32 bits. The shorter of the two argument vectors is then padded with zeros before applying the operation.

$$[0,1,1] + 17$$

yields a 32 bit vector representation of the number 20.

Next: Coercion of array variables Up: Vectors and vector operators Previous: Coercion of scalars to

#### **Explicit coercion operators**

An vector expression may be explicitly coerced to a vector of a given length by applying the ``bin' function. The expression

causes the vector ``val" to be either shortened to length n, or padded with zeros to length n. If ``val" is an integer, is is first coerced to a 32 bit vector, and then truncated or padded. Thus, for example

$$bin(3,17) = [0,0,1]$$
  
 $bin(4,17) = [1,0,0,1]$ 

and

$$[0,1,1] + bin(4,17)$$

is equal to

$$[0,0,1,1]$$
  
+  $[1,0,0,1]$   
=  $[1,1,0,0]$ 

Note that coercing a negative integer to longer than 32 bits will not produce the intuitively correct result, since `bin" treats its argument as an unsigned number. The `sbin" operator is equivalent to `bin", except that it sign extends rather than zero extending. Thus, for example `sbin(64,-1)" is a string of 64 ones.

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#### Coercion of array variables to vectors

A reference to an array of signals without a subscript will be converted to a vector. For example, if x is declared in this way:

```
x : array 0...3 of boolean;
```

then the expression `x" is equivalent to

Note that the elements of x occur in the order given by the type declaration. Thus, for example, if x is declared in this way:

```
x : array 3...0 of boolean;
```

then the expression `x" is equivalent to

This has consequences when combining "big endian" and "little endian" arrays. For example, if we have

```
x : array 3..0 of boolean;
y : array 0..3 of boolean;
```

Then the expression x = y'' is equivalent to

```
(x[3] = y[0]) & (x[2] = y[1]) & (x[1] = y[2]) & (x[0] = y[3])
```

The only difference between big-endian and little-endian arrays is the order in which they are converted to vectors (which determines which element of the array is considered most significant and least significant).

Next: Array subranges Up: Vectors and vector operators Previous: Coercion of array variables

#### Generic arrays and vector coersion

Note that it is possible to declare an array of signals by individually declaring the elements of the array. This allows elements of an array to have different types, as in the earlier example:

```
state[0] : {ready, willing};
state[1] : {ready, willing, able};
state[2] : {ready, willing, able, exhausted};
```

However, the lack of an ``array" declaration means that there is no defined order for building a vector from these elements. Thus, the expression state cannot be coerced to a vector. To allow this, we can use a generic array declaration, as follows:

```
state : array 0..2;
```

This does not declare any signals, but it does determine how state should be converted to a vector.

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# **Array subranges**

A array variable may be explicitly coerced to a vector by specifying a subrange of bit indices. For example, the expression

is equivalent to

Similarly,

is equivalent to

Subranges may be used, for example, to extract bitfields, or to reverse the declared order bits in an array.

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# **Assignments to vectors**

Assignments may also be made to vectors of signals. When a value is assigned to a vector, the following rules apply:

- An integer value on the right hand side is first coerced to a 32 bit vector.
- A vector value on the right hand side is padded or truncated to the same length as the left hand side of the assignment.

For example,

$$[x,y] := [1,1,0];$$

is equivalent to

$$x := 1;$$
  
 $y := 0;$ 

That is, the leftmost (high order) bit is dropped to make the vectors the same length.

On the other hand

$$[x,y] := 1;$$

is equivalent to

$$x := 0;$$
  
 $y := 1;$ 

since the integer is coerced to a vector, and then truncated to length 2.

The assignment

$$[x,y,z] := [1,0];$$

is equivalent to

$$x := 0;$$
  
 $y := 1;$   
 $z := 0;$ 

since the vector on the right-hand-side is zero-extended.

Important note: A vector of signals may not be assigned a nondeterministic value.

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# **Assignments to arrays**

An unsubscripted array reference on the left hand side of an assignment is converted to a vector (see above). This means that the result of the assignment depends on whether the vector is `big-endian" or `little-endian". For example, if:

```
x : array 0...1 of boolean;
then
         x := [1,0];
is equivalent to
          [x[0],x[1]] := [1,0];
which is equivalent to
         x[0] := 1;
         x[1] := 0;
On the other hand, if:
         x : array 1..0 of boolean;
then
         x := [1,0];
is equivalent to
         [x[1],x[0]] := [1,0];
which is equivalent to
         x[1] := 1;
```

x[0] := 0;

Next: Iteratively constructing vectors Up: Vectors and vector operators Previous: Assignments to arrays

#### Vectors as inputs and outputs

The above rules regarding vector assignments have consequences when vectors are passed as parameters to modules. For example, suppose we have a module:

```
MODULE foo(x)
{
   INPUT x : array 1..0 of boolean;
   ...
}
```

Suppose we create an instance of `foo" as follows:

```
bar : foo(y);
```

This is equivalent to:

```
bar.x : array 1..0 of boolean;
bar.x := y;
```

The meaning of this depends on whether ``y" is big-endian or little endian. If ``y" is declared in the same order as ``bar.x":

```
y : array 1..0 of boolean;
```

then we have

```
bar.x[1] := y[1];
bar.x[0] := y[0];
```

On the other hand, if ``y" is in the opposite order:

```
y : array 0..1 of boolean;
```

then

```
bar.x[1] := y[0];
bar.x[0] := y[1];
```

That is, passing a "big-endian" array to a "little-endian" parameter, results in a reversal of the index order of the elements. What remains constant is the value as a binary number.

Note that as a result of the above rules for vector assignment, inputs may be truncated, or zero-extended. For example, if we instantiate ``foo" as follows:

```
bar : foo([0,1,0]);
the effect will be

bar.x[1] := 1;

bar.x[0] := 0;
```

since the vector [0,1,0] will be truncated to [1,0]. On the other hand,

```
bar : foo([1]);
will give us

bar.x[1] := 0;
bar.x[0] := 1;
```

since the integer 1 will be coerced to the vector [0,1].

The same remarks apply to outputs. That is, suppose we have a module

```
MODULE zip(y)
{
   OUTPUT y : array 1..0 of boolean;
   ...
}
```

An instance

```
bar : zip(x);
```

is equivalent to

```
bar.y : array 1..0 of boolean;
x := bar.y;
```

This means that if ``x" has length shorter than ``bar.y", then ``x" will get the low order bits of ``bar.y". Similarly, if ``x" is longer, then it will get ``bar.y" extended with zeros. If ``x" is an array declared in the opposite order to ``bar.y", then ``x" will get ``bar.y" reversed, and so on.

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# Iteratively constructing vectors

A vector may be constructed iteratively using the construction [f(i):i=1..r], where f(i) is some expression containing the parameter i, and l, r are integers. This expands to the vector [f(l), ..., f(r)]. For example, the expression:

$$[ i*i : i = 1..5 ]$$

is equivalent to:

On the other hand:

$$[ i*i : i = 5..1 ]$$

is equivalent to:

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#### **Reduction operators**

The associative operators :: (concatenation), &, |,  $^$ , +, \* and merge may be applied to vectors as ``reduction" operators . For example,

&[
$$w,x,y,z$$
]

is equivalent to

and so on. Reduction operators may be combined with the iterated vector constructor. For example, to compute the sum of the first five squares, we could write:

$$+[ i*i : i = 1..5]$$

Note that for the non-commutative operator ::, the order of the range specification matters. For example

$$::[i*i:i=1..5]$$

produces [1, 4, 9, 16, 25], while

$$::[ i*i : i = 5..1]$$

produces [25,16,9,4,1]. Also note that using :: as a reduction operator makes it possible to construct a vector by repeating a pattern. For example,

$$::[[0,1]:i=1..3]$$

is equivalent to [0,1,0,1,0,1].

Reduction operators do not coerce their arguments to vectors. A reduction operator applied to a scalar operand has no effect. Thus, +3 = 3 (and not 2, fortunately!).

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#### **Vectors as conditions**

If a vector appears as the condition in a conditional expression or statement, then the logical ``or" of the elements of the vector is taken as the condition. Thus, for example,

$$[x,y,z]$$
 ? foo : bar is equivalent to 
$$(x \mid y \mid z)$$
 ? foo : bar

In particular, this means that when a bit vector is used as a condition, it is considered to be true if and only if it is non-zero.

Next: Temporal formulas Up: The SMV language Previous: Vectors as conditions

# **Assertions**

An *assertion* is a condition that must hold true in every possible execution of the program. Assertions in SMV are written in a "linear time" temporal logic, that makes it possible to succinctly state propositions about the relation of events in time.

- Temporal formulas
- The assert declaration
- <u>Using...Prove declarations</u>

Next: The assert declaration Up: Assertions Previous: Assertions

# **Temporal formulas**

Temporal formulas may contain all of the usual expression operator of SMV, plus the temporal operators G, F, X and U. The meanings of these operators are as follows:

- X p is true at time t if p is true at time t + 1.
- ullet G p is true at time t if p is true at all times  $t' \geq t$ .
- ullet F p is true at time t if p is true at some time  $t' \geq t$ .
- ullet p U q is true at time t if q is true at some time  $t' \geq t$ , and for all times < t' but  $\geq t$ , p is true.

A temporal formula is true for a given exectution of the program if it is true at the initial time (t = 0).



Next: Using...Prove declarations Up: Assertions Previous: Temporal formulas

#### The assert declaration

A declaration of the form

```
assert p;
```

where p is a temporal formula, means that every execution of the program must satisfy the formula p. An execution that does not satisfy the formula is called a *failure* of the program.

An assertion may be given a name. For example:

```
foo : assert p;
```

This does not change the semantics of the program, but provides an identifier ``foo" for refering to the given assertion. The code

```
foo : assert p;
foo : assert q;
```

is equivalent to

```
foo: assert p & q;
```

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#### **Using...Prove declarations**

A using...prove declaration tells the verification system to use one assertion as an assumption when verifying another. A declaration of the form

```
using foo prove bar;
```

where foo and bar are identifiers for assertions, tells the verification system to use assertion foo as an assumption when proving assertion bar. A list of assumptions may also be used:

```
using a1,a2,...,an prove bar;
```

Such a "proof" may not contain circular chains of reasoning. Thus, for example,

```
using foo prove bar; using bar prove foo;
```

is illegal.

Next: The refinement relation Up: The SMV language Previous: Using...Prove declarations

# Refinements

N.B. This section is incomplete and under construction

The mechanism of ``refinement" in SMV allows one model to represent the behavior of a design simultaneously at many levels of abstraction. It also allows one to verify in a compositional manner that each level of the design is a correct implementation of the level above.

The basic object in the refinement system is a ``layer''. A layer is a named collection of assignments. For example:

```
layer P : {
  x := y + z;
  next(z) := x;
}
```

represents a layer named P, which contains assignments to signals x and z. Within a layer the single assignment rule applies. That is, any given signal may be assigned only once. However, a signal may be assigned in more than one layer.

One layer may be declared to ``refine" another. The syntax for this declaration is:

```
P refines O;
```

where P and Q are names of layers. If P refines Q, then an assignment to any signal s in P supercedes the corresponding assignment to s in Q. For example, suppose that layer Q is defined as follows:

```
layer Q : {
  y := z;
  next(z) := 2 * y;
}
```

The net functional effect of these declarations is equivalent to:

```
x := y + z;

y := z;

next(z) := x;
```

That is, the assignment to z in P supercedes the assignment to z in Q, because P refines Q. Any assignment that is superceded in this way becomes a part of the specification. That is, in our example, every trace of the system must be consistent with

$$next(z) := 2 * y$$

at all times. This proposition is given the name  $\z$ /Q", meaning  $\$  the assignment to signal z in layer Q". Note that the property z//Q is true in the case of our example, since at all times

$$x = y+z = z+z = 2*z$$

Thus, we can infer that every trace of our system is also a trace of the system consisting only of the layer Q. Put another way, our system satisfies specification Q (and also, trivially, specification P).

- The refinement relation
  - o Circular assignments
- Compositional verification
- The <u>using</u>...<u>prove</u> declaration
- Abstract signals



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Next: Circular assignments Up: Refinements Previous: Refinements

#### The refinement relation

The refinement relation between layers is by definition transitive. Thus if we have:

P refines Q; Q refines R;

then by implication

P refines R;

The refinement relation may not be circular. Thus

P refines P

is an error. The *implementation* of a signal is the assignment to that signal whose layer is minimal with respect to the refinement relation. If no unique minimal assignment to a signal exists, the program is in error.

• Circular assignments

Next: The using...prove declaration Up: Refinements Previous: Circular assignments

#### **Compositional verification**

In order to verify a given assignment x//P, where x is a signal and P is layer, it is allowed to use any other assignment y//Q as an assumption (with one proviso, below). The syntax for this is:

```
using x//P prove y//Q;
```

In this case, x//P is referred to as the ``assumption" and y//Q as the ``guarantee". The one restriction on the use of this statement is that if x and y are identical, then P must refine Q. Other than this, any use is allowed, including circularities. For example, it is legitimate to write:

```
using x//P prove y//P;
using y//P prove x//P;
```

As a example, suppose we have:

```
layer P : {
    x := 0;
    y := 0;
}
layer Q : {
    init(x) := 0;
    next(x) := y;
    y := x;
}
Q refines P;
using x//P prove y//P;
using y//P prove x//P;
```

That is, in essence, the ``using" declarations say that in order to prove that x is always zero, we can assume that y is always zero, and vice versa.

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# The using...prove declaration

This declaration has the form form

```
using
  p_1, p_2, ..., p_k
prove
  q_1, q_2, ..., q_m
```

where  $p_1$ ,  $p_2$ , ...,  $p_k$  and  $q_1$ ,  $q_2$ , ...,  $q_m$  are properties. The meaning of the declaration is that properties p\_1, p\_2, ..., p\_k are to be taken as assumptions when proving the properties q\_1, q\_2, ..., q\_m.

If assumptions are not declared for a given property, then that property inherits the assumptions of its parent. For example, if we wish to assume property foo when proving bar.a, bar.b and bar.c, it is sufficient to declare

```
using foo prove bar;
```

If there is no declaration of assumptions for bar.a, then it will inherit the assumption of foo from its parent, bar. Note, however, that if we include the declaration

```
using baz prove bar.a;
```

then only property baz is used to prove bar.a.

Similarly, if we wish to assume a collection of properties foo.a, foo.b and foo.c when proving a property bar, it is sufficient to declare:

```
using bar prove foo;
```

It is allowed to use several assignments to the same signal as assumptions. For example:

```
using x//P1, x//P2 prove y//P
```

In this case, the conjunction of the two assumptions is used.

Next: Syntax Up: Refinements Previous: The using...prove declaration

# **Abstract signals**

In some cases, it may be necessary to introduce auxiliary signals that are used as part of the specification, or part of the proof, but do not belong to the system being verified. Such signals are introduced by the keyword abstract, as follows:

abstract <signal> : <type>

The implementation of a non-abstract signal may not depend on an abstract signal.

Next: Lexical tokens Up: The SMV language Previous: Abstract signals

# **Syntax**

This section gives a BNF grammar for the SMV language.

- Lexical tokens
- Identifiers
- Expressions
- Types
- Statements
- Module definitions
- Programs

Next: Identifiers Up: Syntax Previous: Syntax

#### Lexical tokens

A program is a sequence of *lexical tokens*, optionally separated by *whitespace*. A token is either an *atom*, a number, or any of the various keywords and punctation symbols that appear in typewriter font in the grammar expressions that follow.

#### An atom is

- A string consisting of alphanumeric characters and the characters, and the characters ``\$" and ``\_", beginning with an alphabetic character, or
- A string containing any character except the space character, delimited by an initial backslash (``
   \ ") and a final space character. The delimiters do not count as part of the atom.

As an example ``foo\_123" is an atom. It is exactly equivalent to `` \ foo\_123" (note the terminating

space character). Using backslash and space as delimiters allows any character (including backslash, but excluding space) to be included in an atom.

A number is a string of digits. Whitespace is any string of space characters, tab characters and newline characters.

Next: Expressions Up: Syntax Previous: Lexical tokens

#### **Identifiers**

The grammar rules for an *identifier* is as follows:

Next: Types Up: Syntax Previous: Identifiers

# **Expressions**

The grammar rules for an *expression* are, in order of precedence, from high to low (note € stands for the empty string):

	_		
expr::		id	
			number
			{ atom,,atom }
	1		expr :: expr
	I		[- + * &   ^] expr
			expr ** expr
expr	1		expr [* / << >>]
			expr [+ -] expr
	I		expr mod expr
			expr in expr
			expr union expr
[=  = < <= > >=] expr	I		expr
			~ expr
			expr & expr
			expr [  ^] expr
	I		expr <-> expr
			expr -> expr
			expr ? expr : expr
			expr expr
			( expr )

```
[ expr,...,expr ]

| [ expr,...,expr : atom =
expr .. expr ]

| bin ( expr , expr )

All operators of the same precedence except ``?:" associate to the left. For example, a / b * c is parsed as
(a / b) * c. The ternary ``?:" associates to the right. Thus

a ? b : c ? d : e
is parsed as

a ? b : (c ? d : e)
```

Next: Statements Up: Syntax Previous: Expressions

# **Types**

The grammar rules for types are:

type::		boolean
	1	expr expr
	1	{ atom, , atom }
	1	array expr expr of type
	1	atom ( expr,,expr )

Next: Module definitions Up: Syntax Previous: Types

#### **Statements**

The grammar rules for statements are:

```
stmt::
                                                      lhstup : type ;
                                                            lhs [:=|<-] expr;
                                                            { block }
                                                            if ( expr ) stmt
                                                            case { cblk }
                                                            switch ( tuple ) { cblk }
                                                             [for|chain] ( atom = expr ;
                                        atom = expr) stmt
expr ;
lhs::
                                      id
                                                            next ( id )
                                                             (lhstup)
                                            \epsilon
lhstup::
                                                             lhs
                                                             lhstup lhs
block::
                                    stmt
                                                            block stmt
cblk::
                                     expr : stmt
                                                            cblk expr : stmt
```

Next: Programs Up: Syntax Previous: Statements

# **Module definitions**

The grammar rules for module definitions are:

block }	module::		module atom ( params ) {
params::		ε	atom
			params , atom

Next: Extension of operators to Up: Set expressions Previous: Set expressions

#### The set inclusion operator

There is one operator for testings sets: the set inclusion operator ``in". The expression ``x in y" returns true if the value x is contained in the set y. The ``in" operator obeys the following law:

$$(x in {y,z}) = ((x in y) | (x in z))$$

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#### **Extension of operators to sets**

Most of the operators extend to sets, in a way which is consistent with the interpretation of sets as independent nondeterministic choices. Generally, a unary operator f obeys the law

$$f\{x,y\} = \{f(x),f(y)\}$$

Thus, for example,

$$-(2..3) = (-2..-3)$$

and

$$\sim \{0,1\} = \{1,0\}$$

For a binary operator \*, we have

$$\{x,y\}$$
 \* z =  $\{x$  \* z, y \* z $\}$   
x \*  $\{y,z\}$  =  $\{x$  \* y, x \* z $\}$ 

For example,

$$3 + \{4,5\} = \{7,8\}$$

and

$$0 \& \{0,1\} = 0$$
  
 $1 \& \{0,1\} = \{0,1\}$ 

(which are actually special cases of the laws given above for ``and").

This behavior of sets is somewhat counterintuitive when the equality operator is applied to sets. For example, the result of

$$\{a,b\} = \{a,b\}$$

is not equal to 1 (true). The way to understand this is to think of each set as representing an arbitrary choice among its elements. Thus, the result of the above expression is the set  $\{0,1\}$ , since we may choose equal elements or we may choose unequal elements.

The exception to the above rule is the ``in" operator, which compares a value and a set of values. In this case, only the left represents a nondeterministic choice. That is:

Extension of operators to sets

$$\{x,y\}$$
 in  $z = \{x \text{ in } z, y \text{ in } z\}$ 

However, as stated previously,

$$x in \{y,z\} = (x in y) | (x in z)$$

[N.B. This makes ``in" the only operator in the language which is not monotonic with respect to set containment. The ``in" operator is only monotonic in its left argument. A formal verification system that relies on monotonicity (such as ternary symbolic simulation) should allow only constant sets on the right hand side of ``in".]



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#### **Comprehension expressions**

A set may be built iteratively using the construction  $\{f(i):i=x..y\}$ , where f(i) is some expression containing the parameter i, and x, y are integer constants. This expands to the set  $\{f(1), \ldots, f(r)\}$ . For example, the expression:

$$\{ i*i : i = 1..5 \}$$

is equivalent to the set:

The form  $\{f(i) : i = x..y, c(i)\}$  represents the set of all f(i), for i = x..y such that condition c(i) is true. That is,

$$\{f(i) : i = x..y, c(i)\} = \{c(x) ? f(x), ..., c(y) ? f(y)\}$$

For example,

$$\{ i : i = 1..5, i \mod 2 = 1 \} = \{1,3,5\}$$

Or, for example, if y is of type array 1..5 of boolean, then

```
\{ i : i = 1..5, y[i] \}
```

represents the set of all indices i such that element i of array y is true. Note that in this case, if none of the elements of y is true, the result is undefined. This provides a straightforward way to describe a nondeterministic arbiter. In addition, the contruct provides a way to describe a nondeterministic choice among all the number in a given range *except* a specified number:

$$x := \{i : i \text{ in } 1..5, i \sim= j\};$$

 $\dots -2^{31} \dots (2^{31}-1)^{\frac{1}{2}}$ 

N.B. Unsigned arithmetic on integers of arbitrary precision can be performed on bit vectors, however. See section on vectors.

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#### **Circular assignments**

A circularity error occurs if there is a cycle of zero-delay assignments amongst the union of all assignments in all layers. Thus for example, the following program:

```
layer Q : {
   x := y;
}
layer P : {
   y := x;
   next(x) := y;
}
P refines Q;
```

is erroneous, even though it is functionally equivalent to the non-circular program:

```
y := x;

next(x) := y;
```