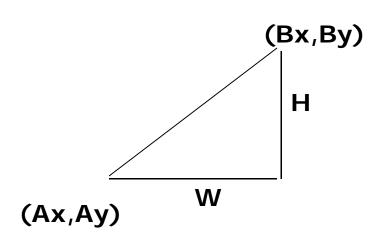


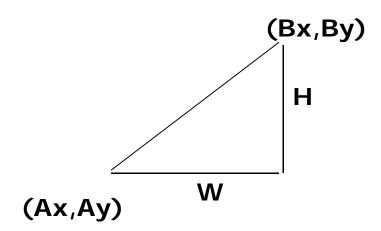
Recall: Bresenham's Line-Drawing Algorithm

- Problem: Given endpoints (Ax, Ay) and (Bx, By) of line, determine intervening pixels
- First make two simplifying assumptions (remove later):
 - (Ax < Bx) and
 - (0 < m < 1)
- Define
 - Width W = Bx Ax
 - Height H = By Ay





Recall: Bresenham's Line-Drawing Algorithm



- Based on assumptions (Ax < Bx) and (0 < m < 1)
 - W, H are +ve
 - H < W
- Increment x by +1, y incr by +1 or stays same
- Midpoint algorithm determines which happens

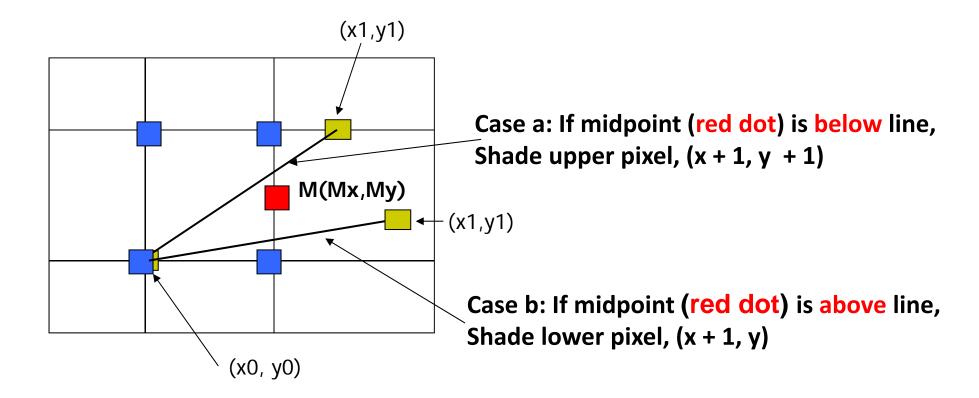


Recall: Bresenham's Line-Drawing Algorithm

What Pixels to turn on or off?

Consider pixel midpoint $M(Mx, My) = (x + 1, y + \frac{1}{2})$

Build equation of actual line, compare to midpoint

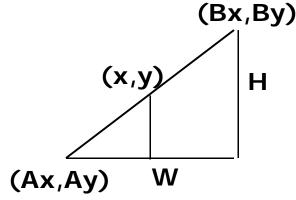


Build Equation of the Line



Using similar triangles:

$$\frac{y - Ay}{x - Ax} = \frac{H}{W}$$



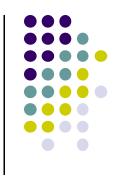
$$H(x - Ax) = W(y - Ay)$$
$$-W(y - Ay) + H(x - Ax) = 0$$

- Above is equation of line from (Ax, Ay) to (Bx, By)
- Thus, any point (x,y) that lies on ideal line makes eqn = 0
- Double expression (to avoid floats later), and call it F(x,y)

$$F(x,y) = -2W(y - Ay) + 2H(x - Ax)$$



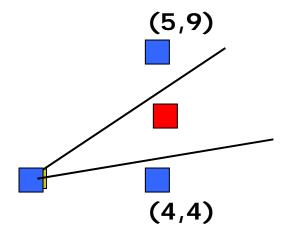
- So, F(x,y) = -2W(y Ay) + 2H(x Ax)
- Algorithm, If:
 - F(x, y) < 0, (x, y) above line
 - F(x, y) > 0, (x, y) below line
- Hint: F(x, y) = 0 is on line
- Increase y keeping x constant, F(x, y) becomes more negative

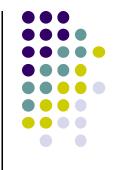


• Example: to find line segment between (3, 7) and (9, 11)

$$F(x,y) = -2W(y - Ay) + 2H(x - Ax)$$
$$= (-12)(y - 7) + (8)(x - 3)$$

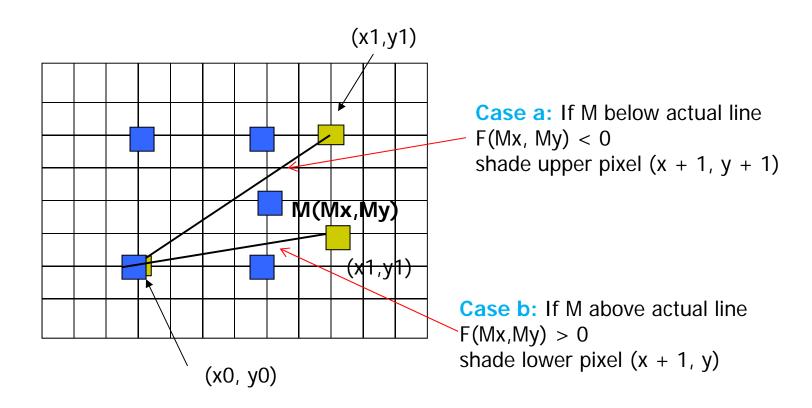
- For points on line. E.g. (7, 29/3), F(x, y) = 0
- A = (4, 4) lies below line since F = 44
- B = (5, 9) lies above line since F = -8



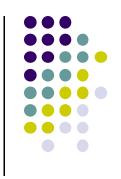


What Pixels to turn on or off?

Consider pixel midpoint $M(Mx, My) = (x0 + 1, Y0 + \frac{1}{2})$







Initially, midpoint
$$M = (Ax + 1, Ay + \frac{1}{2})$$

$$F(Mx, My) = -2W(y - Ay) + 2H(x - Ax)$$

i.e.
$$F(Ax + 1, Ay + \frac{1}{2}) = 2H - W$$

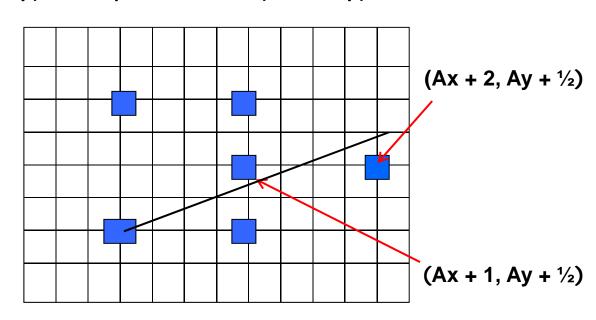
Can compute F(x,y) for next midpoint incrementally

If we increment to (x + 1, y), compute new F(Mx,My)

$$F(Mx, My) += 2H$$

i.e.
$$F(Ax + 2, Ay + \frac{1}{2})$$

- $F(Ax + 1, Ay + \frac{1}{2})$
= 2H



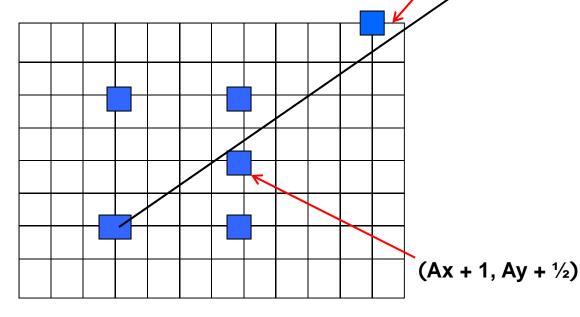




If we increment to (x + 1, y + 1)F(Mx, My) += 2(H - W)

(Ax + 2, Ay + 3/2)

i.e.
$$F(Ax + 2, Ay + 3/2) - F(Ax + 1, Ay + \frac{1}{2}) = 2(H - W)$$





Recall: F is equation of line



- Final words: we developed algorithm with restrictions
 0 < m < 1 and Ax < Bx
- Can add code to remove restrictions
 - When Ax > Bx (swap and draw)
 - Lines having m > 1 (interchange x with y)
 - Lines with m < 0 (step x++, decrement y not incr)
 - Horizontal and vertical lines (pretest a.x = b.x and skip tests)

Computer Graphics CS 4731 Lecture 25 Polygon Filling & Antialiasing

Prof Emmanuel Agu

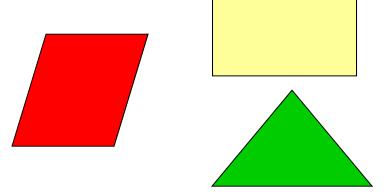
Computer Science Dept. Worcester Polytechnic Institute (WPI)



Defining and Filling Regions of Pixels



- Methods of defining region
 - Pixel-defined: specifies pixels in color or geometric range
 - Symbolic: provides property pixels in region must have
 - Examples of symbolic:
 - Closeness to some pixel
 - Within circle of radius R
 - Within a specified polygon





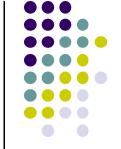


- Definition: Region R is the set of all pixels having color C that are connected to a given pixel S
- 4-adjacent: pixels that lie next to each other horizontally or vertically, NOT diagonally
- 8-adjacent: pixels that lie next to each other horizontally, vertically OR diagonally
- **4-connected:** if there is unbroken path of 4-adjacent pixels connecting them
- 8-connected: unbroken path of 8-adjacent pixels connecting them





- Recursive algorithm
- Starts from initial pixel of color, intColor
- Recursively set 4-connected neighbors to newColor
- Flood-Fill: floods region with newColor
- Basic idea:
 - start at "seed" pixel (x, y)
 - If (x, y) has color intColor, change it to newColor
 - Do same recursively for all 4 neighbors



Recursive Flood-Fill Algorithm

Note: getPixel(x,y) used to interrogate pixel color at (x, y)

```
void floodFill(short x, short y, short intColor)
{
   if(getPixel(x, y) == intColor)
       setPixel(x, y);
       floodFill(x - 1, y, intColor); // left pixel
       floodFill(x + 1, y, intColor); // right pixel
       floodFill(x, y + 1, intColor); // down pixel
       floodFill(x, y - 1, intColor); // up pixel
```

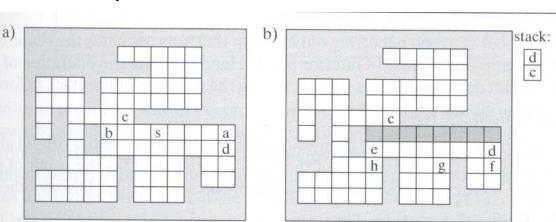
Recursive Flood-Fill Algorithm



- Recursive flood-fill is blind
- Some pixels retested several times
- Region coherence is likelihood that an interior pixel mostly likely adjacent to another interior pixel
- Coherence can be used to improve algorithm performance
- A run: group of adjacent pixels lying on same scanline
- Fill runs(adjacent, on same scan line) of pixels

Region Filling Using Coherence

Example: start at s, initial seed



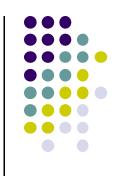
stack:



Pseudocode:

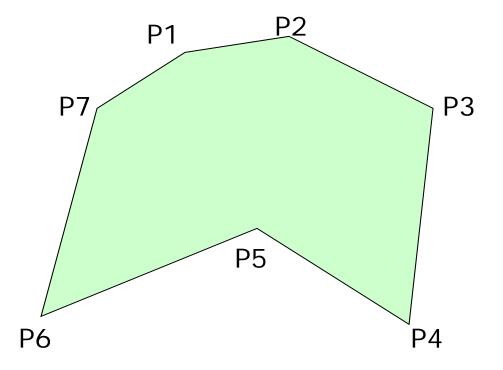
Push address of seed pixel onto stack
while(stack is not empty)
{
 Pop stack to provide next seed
 Fill in run defined by seed
 In row above find reachable interior runs
 Push address of their rightmost pixels
 Do same for row below current run

Note: algorithm most efficient if there is **span coherence** (pixels on scanline have same value) and **scan-line coherence** (consecutive scanlines similar)



Filling Polygon-Defined Regions

Problem: Region defined polygon with vertices
 Pi = (Xi, Yi), for i = 1...N, specifying sequence of P's vertices

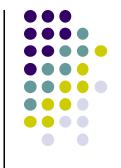




Filling Polygon-Defined Regions

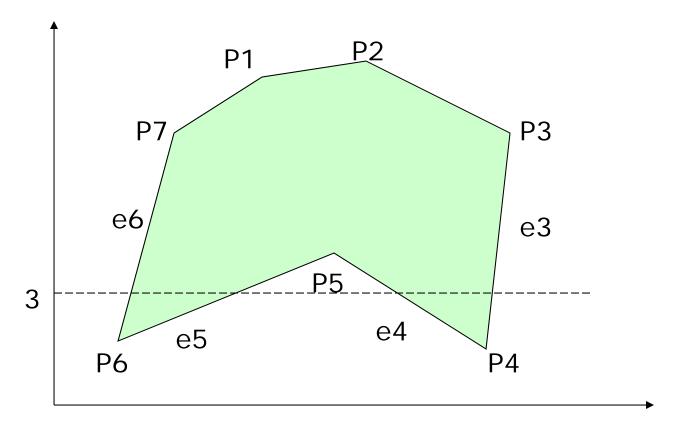
- **Solution:** Progress through frame buffer scan line by scan line, filling in appropriate portions of each line
- Filled portions defined by intersection of scan line and polygon edges
- Runs lying between edges inside P are filled
- Pseudocode:

```
for(each scan Line L)
{
   Find intersections of L with all edges of P
   Sort the intersections by increasing x-value
   Fill pixel runs between all pairs of intersections
}
```



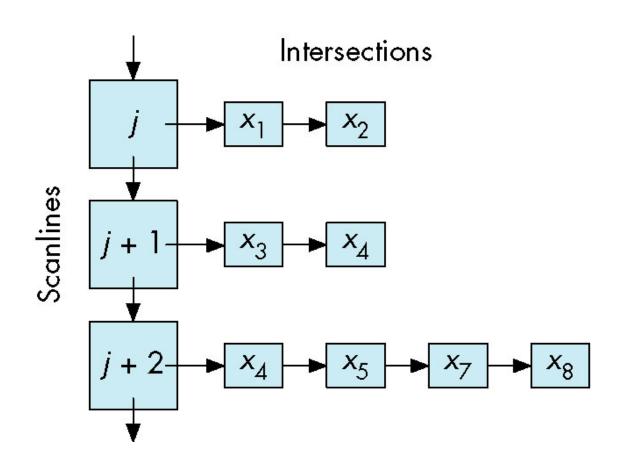
Filling Polygon-Defined Regions

- Example: scan line y = 3 intersects 4 edges e3, e4, e5, e6
- Sort x values of intersections and fill runs in pairs
- Note: at each intersection, inside-outside (parity), or vice versa





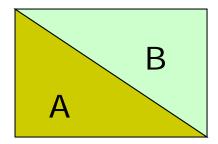








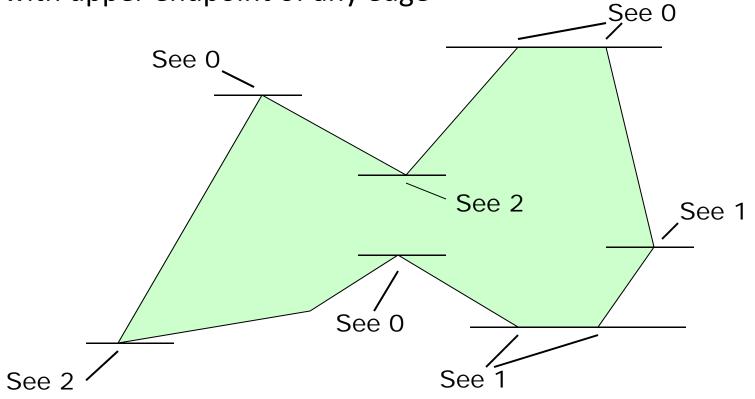
- Problem: What if two polygons A, B share an edge?
- Algorithm behavior could result in:
 - setting edge first in one color and the another
 - Drawing edge twice too bright
- Make Rule: when two polygons share edge, each polygon owns its left and bottom edges
- E.g. below draw shared edge with color of polygon B







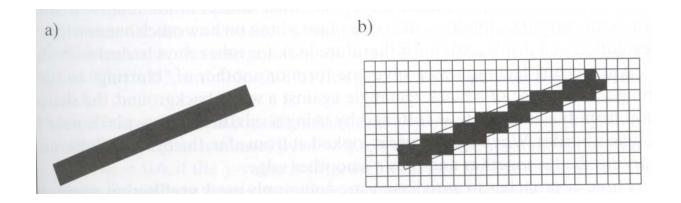
- Problem: How to handle cases where scan line intersects with polygon endpoints to avoid wrong parity?
- Solution: Discard intersections with horizontal edges and with upper endpoint of any edge







- Raster displays have pixels as rectangles
- Aliasing: Discrete nature of pixels introduces "jaggies"



Antialiasing



- Aliasing effects:
 - Distant objects may disappear entirely
 - Objects can blink on and off in animations
- Antialiasing techniques involve some form of blurring to reduce contrast, smoothen image
- Three antialiasing techniques:
 - Prefiltering
 - Postfiltering
 - Supersampling

References



- Hill and Kelley, chapter 11
- Angel and Shreiner, Interactive Computer Graphics, 6th edition