



# Introduction to Computer Graphics with WebGL

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# Computer Viewing Positioning the Camera

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# Objectives

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- Introduce the mathematics of projection
- Introduce WebGL viewing functions in MV.js
- Look at alternate viewing APIs



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# From the Beginning

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- In the beginning:
  - fixed function pipeline
  - Model-View and Projection Transformation
  - Predefined frames: model, object, camera, clip, ndc, window
- After deprecation
  - pipeline with programmable shaders
  - no transformations
  - clip, ndc window frames
- MV.js reintroduces original capabilities



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# Computer Viewing

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- There are three aspects of the viewing process, all of which are implemented in the pipeline,
  - Positioning the camera
    - Setting the model-view matrix
  - Selecting a lens
    - Setting the projection matrix
  - Clipping
    - Setting the view volume



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# The WebGL Camera

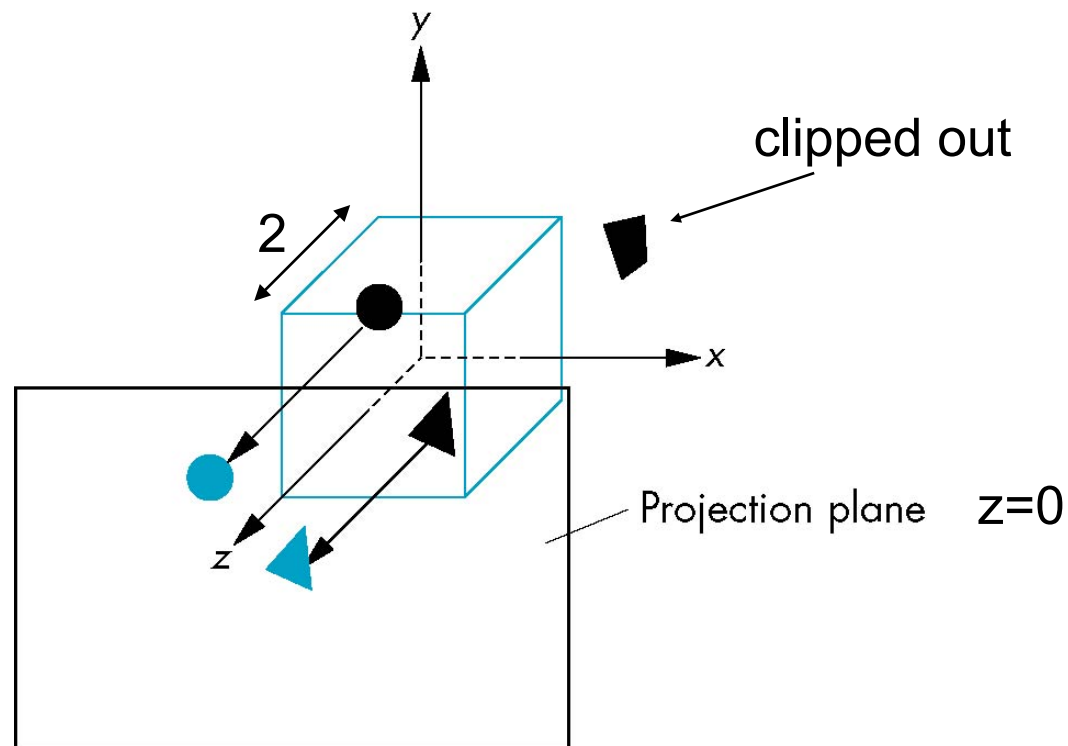
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- In WebGL, initially the object and camera frames are the same
  - Default model-view matrix is an identity
- The camera is located at origin and points in the negative z direction
- WebGL also specifies a default view volume that is a cube with sides of length 2 centered at the origin
  - Default projection matrix is an identity



# Default Projection

Default projection is orthogonal





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# Moving the Camera Frame

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- If we want to visualize objects with both positive and negative z values we can either
  - Move the camera in the positive z direction
    - Translate the camera frame
  - Move the objects in the negative z direction
    - Translate the world frame
- Both of these views are equivalent and are determined by the model-view matrix
  - Want a translation (`translate(0.0, 0.0, -d);`)
  - $d > 0$



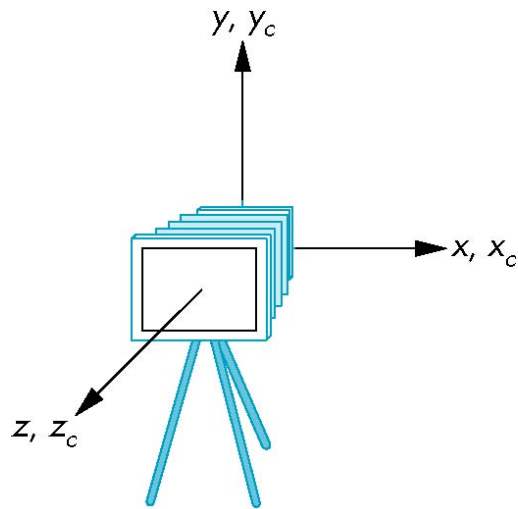


# Moving Camera back from Origin

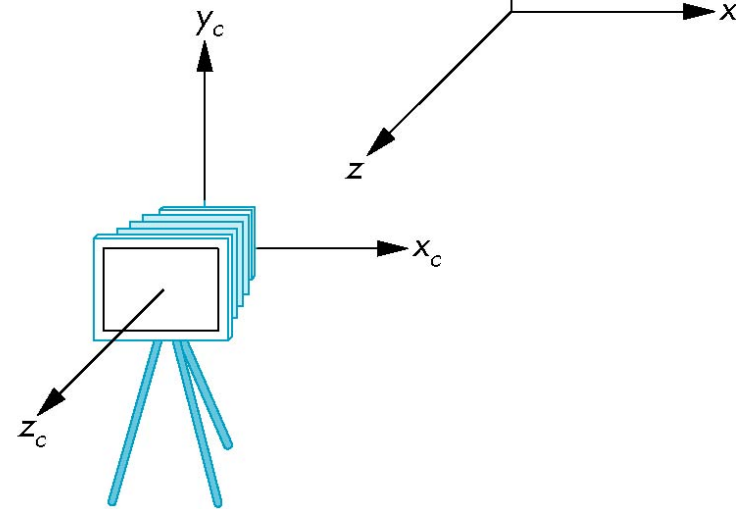
frames after translation by  $-d$

$$d > 0$$

default frames



(a)

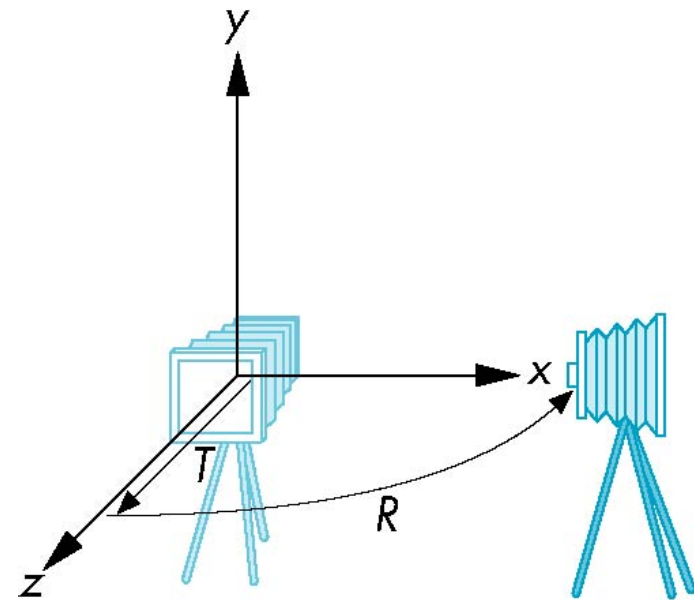


(b)



# Moving the Camera

- We can move the camera to any desired position by a sequence of rotations and translations
- Example: side view
  - Rotate the camera
  - Move it away from origin
  - Model-view matrix  $C = TR$





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# WebGL code

- Remember that last transformation specified is first to be applied

```
// Using MV.js
```

```
var t = translate (0.0, 0.0, -d);  
var ry = rotateY(90.0);  
var m = mult(t, ry);
```

or

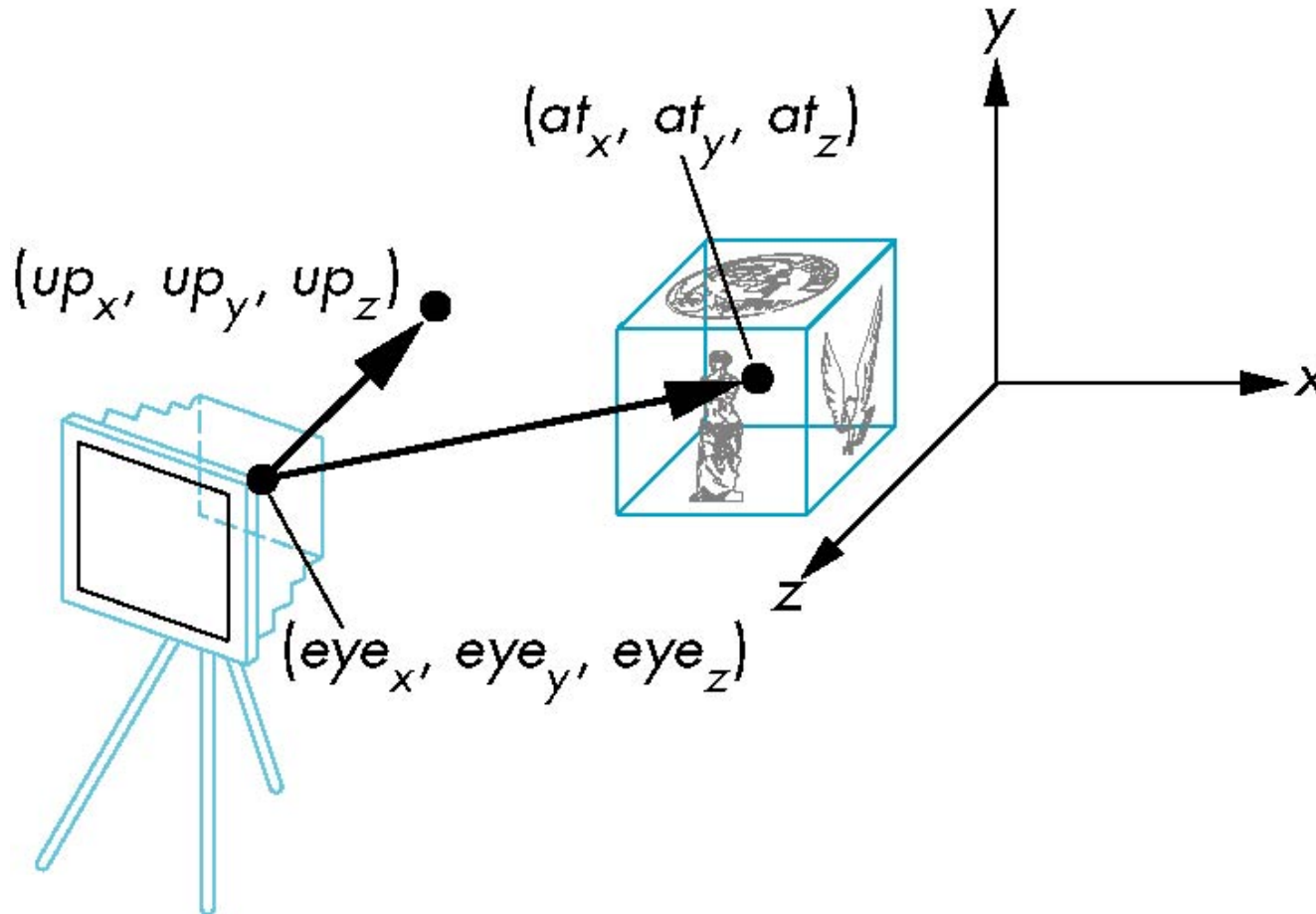
```
var m = mult(translate (0.0, 0.0, -d),  
            rotateY(90.0));
```



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# lookAt

LookAt(eye, at, up)





# The lookAt Function

- The GLU library contained the function `gluLookAt` to form the required modelview matrix through a simple interface
- Note the need for setting an up direction
- Replaced by `lookAt()` in `MV.js`
  - Can concatenate with modeling transformations
- Example: isometric view of cube aligned with axes

```
var eye = vec3(1.0, 1.0, 1.0);  
var at  = vec3(0.0, 0.0, 0.0);  
var up  = vec3(0.0, 1.0, 0.0);
```

```
var mv = LookAt(eye, at, up);
```



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# Other Viewing APIs

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- The LookAt function is only one possible API for positioning the camera
- Others include
  - View reference point, view plane normal, view up (PHIGS, GKS-3D)
  - Yaw, pitch, roll
  - Elevation, azimuth, twist
  - Direction angles