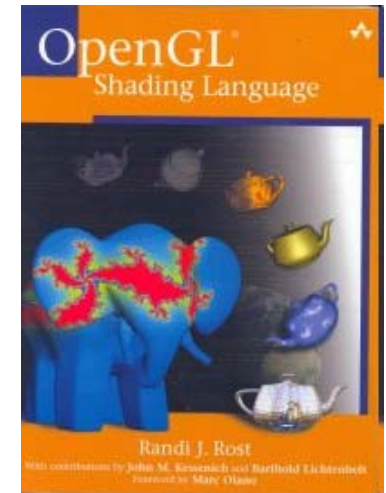
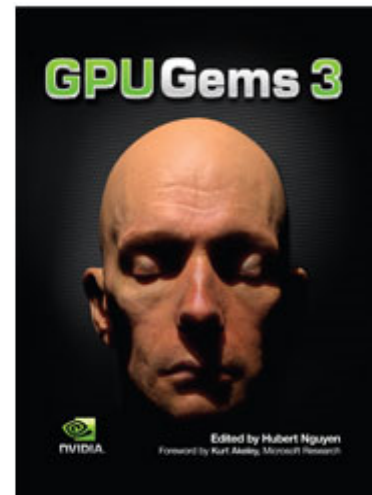
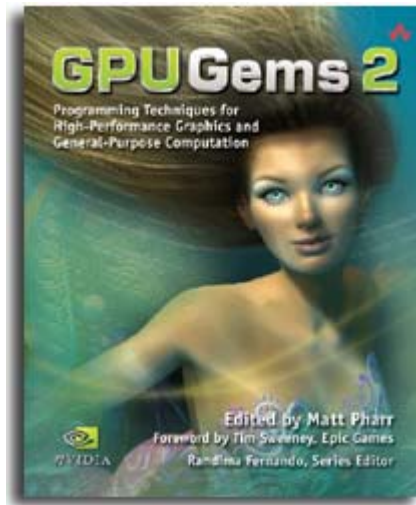
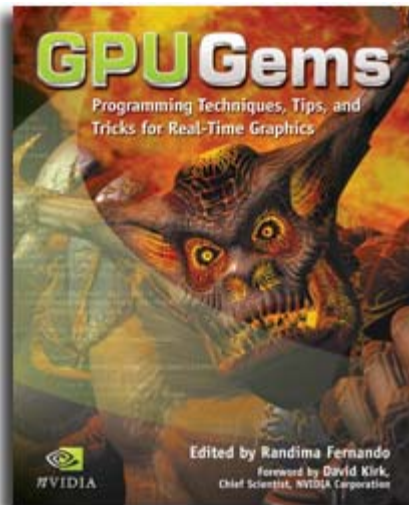


Introduction to Programming Mapping Techniques On The GPU



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[images courtesy of Nvidia and Addison-Wesley]

Motivation

Why do we need and want mapping?

- Realism
- Ease of Capture vs. Manual Creation
- GPUs are Texture Optimized (Texture = Efficient Storage)

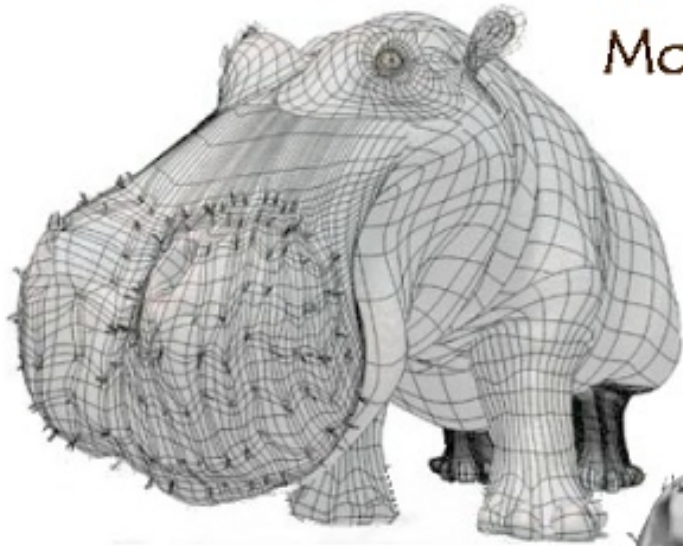


Solid Color Metal



**Metal Using
Mapping Techniques**

Quest for Visual Realism



Model

Model + Shading



Model + Shading
+ Textures

At what point
do things start
looking real?



For more info on the computer artwork of Jeremy Birn
see <http://www.3drender.com/jbirn/productions.html>

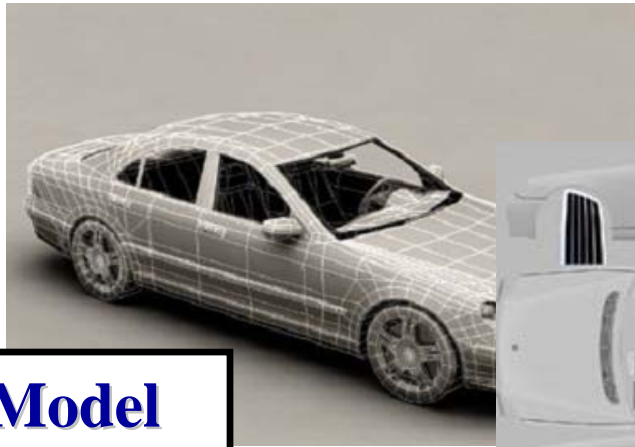


Talk Overview

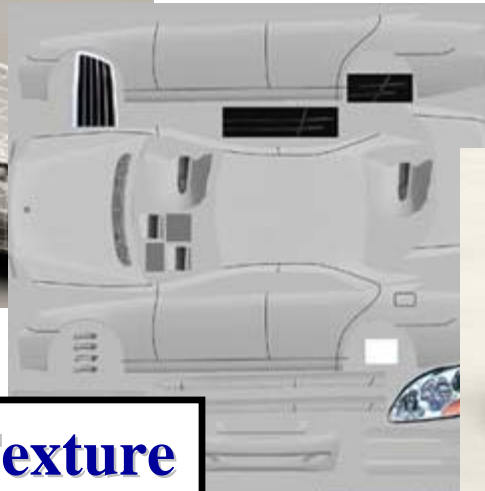
- **Review Basic Texturing**
- **Environment Mapping**
- **Bump Mapping**
- **Displacement Mapping**

Texture Mapping

**Main Idea: Use an image to apply color to the pixels
Produce by geometry of an object.[Catmull 74]**



Model



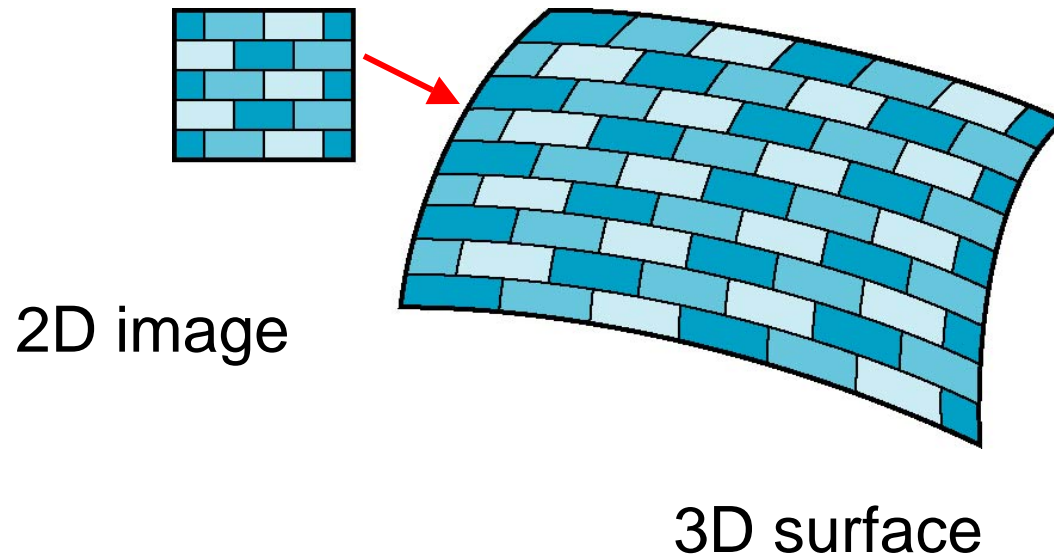
Texture



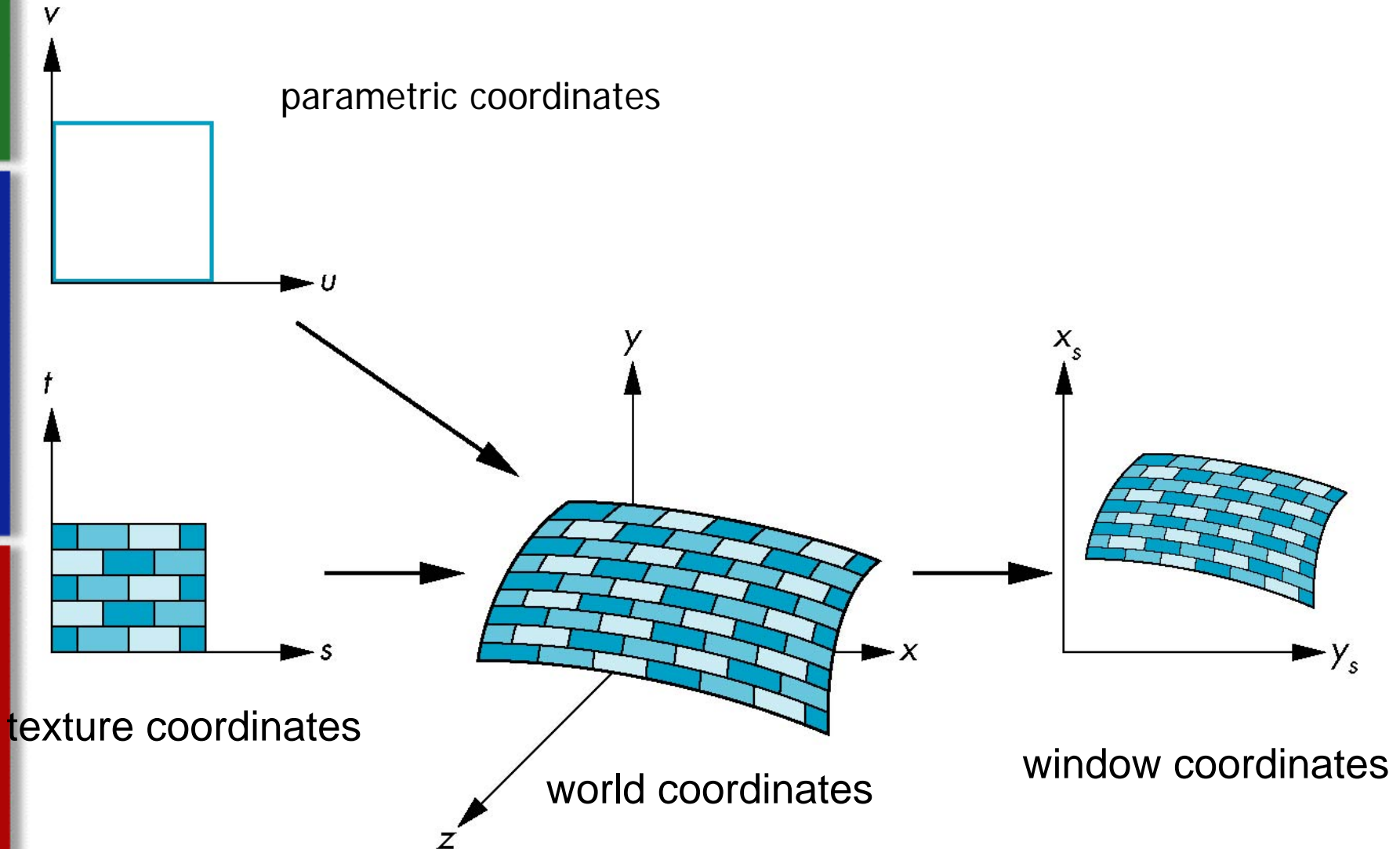
Render

Is it simple?

- Idea is simple---map an image to a surface---there are 3 or 4 coordinate systems involved



Texture Mapping



Mapping Functions

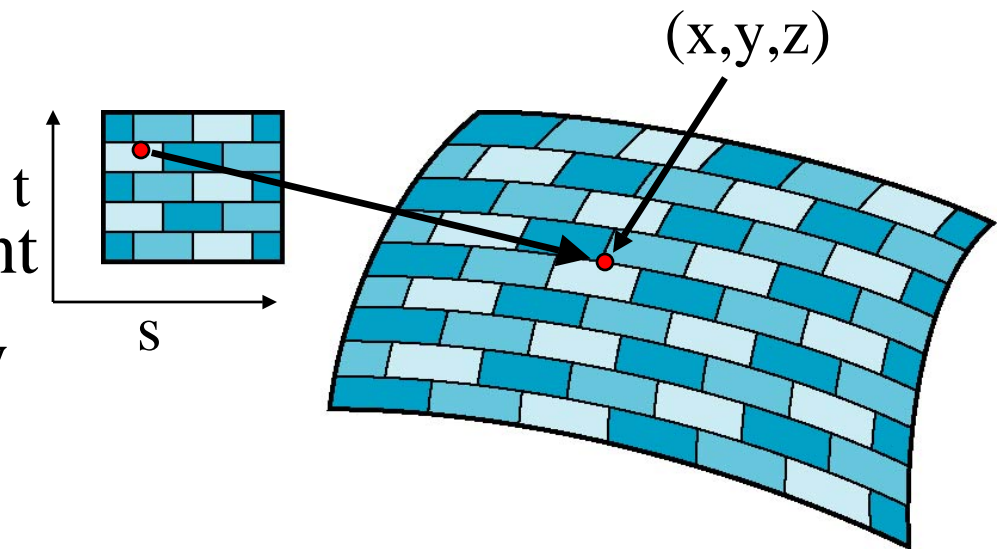
- Basic problem is how to find the maps
- Consider mapping from texture coordinates to a point a surface
- Appear to need three functions

$$x = x(s,t)$$

$$y = y(s,t)$$

$$z = z(s,t)$$

- But we really want to go the other way

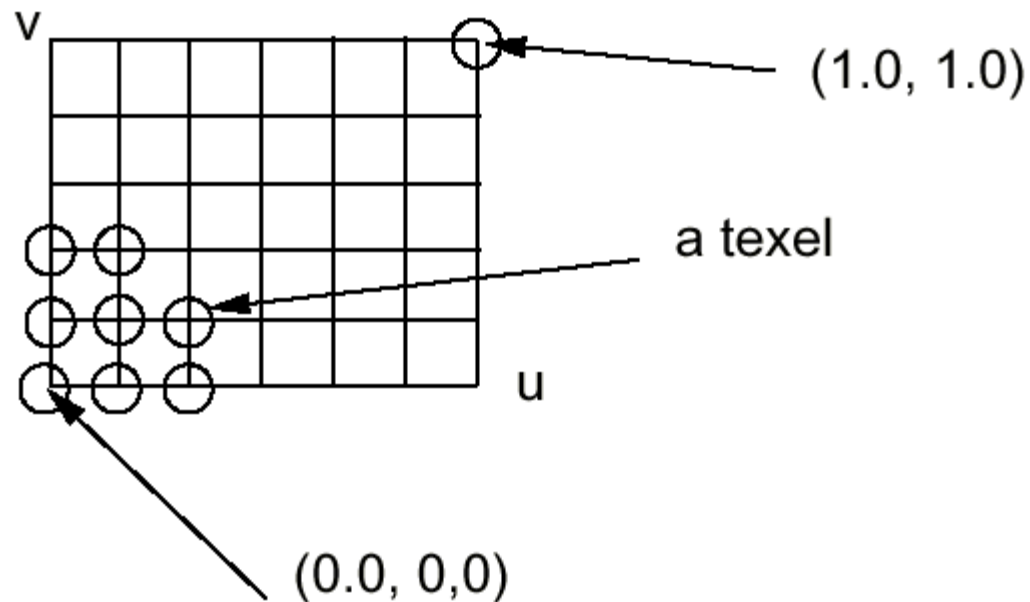


Backward Mapping

- We really want to go backwards
 - Given a pixel, we want to know to which point on an object it corresponds
 - Given a point on an object, we want to know to which point in the texture it corresponds
- Need a map of the form
$$s = s(x,y,z)$$
$$t = t(x,y,z)$$
- Such functions are difficult to find in general

Texture and Texel

- Each Pixel in a Texture map = Texel
- Each Texel has (u,v) 2D Texture Coordinate
- Range of (u,v) is $[0.0,1.0]$ (normalized)



Are there Issues?

2 Problems:

- Which Texel should we use?
- Where Do We Put Texel?

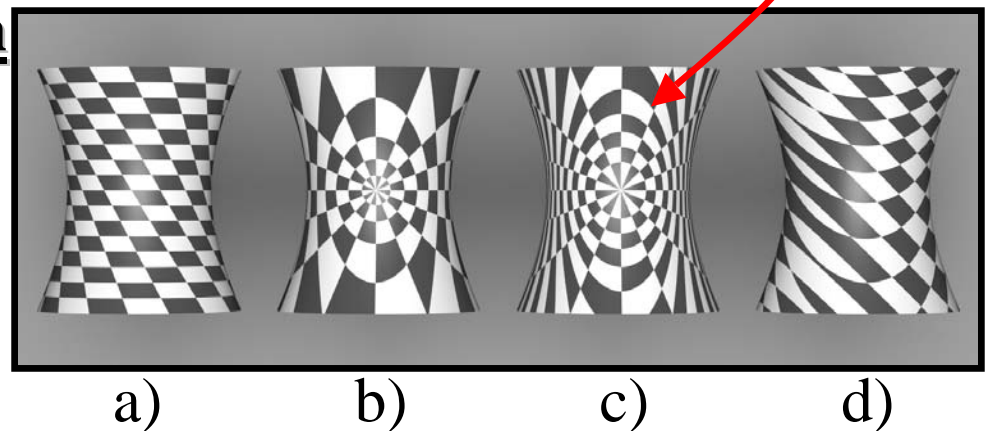
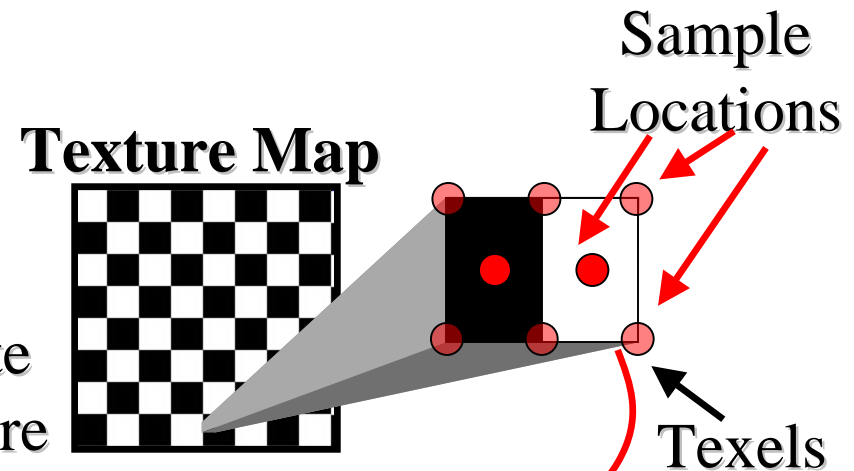
2 Solutions:

Sampling & Filtering

- Map >1 Texel to 1 Coordinate
- Nearest, Interpolation, & More

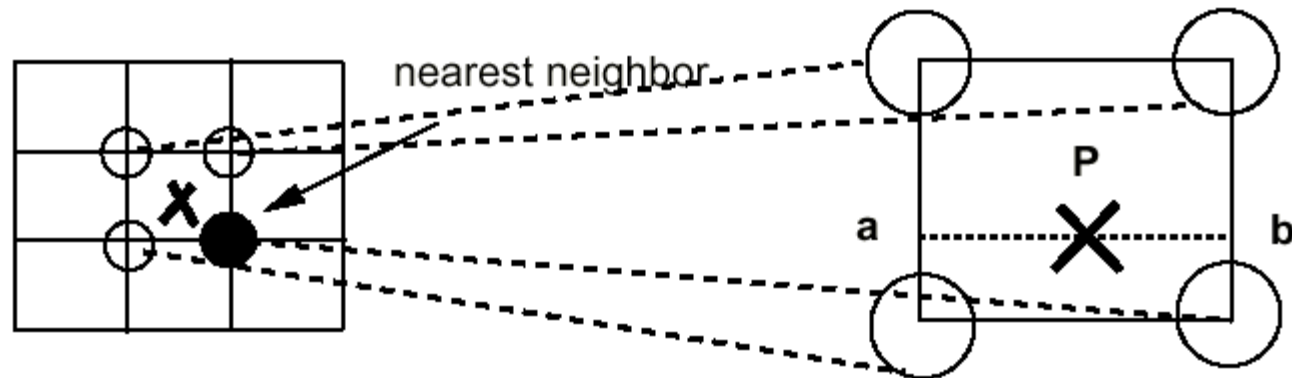
Coordinate Generation

- UV (most common)
- Spherical
- Cylindrical
- Planar



(u,v) tuple

- For any (u,v) in the range of $(0-1, 0-1)$ multiplied by *texture image width and height*, we can find the corresponding value in the texture map



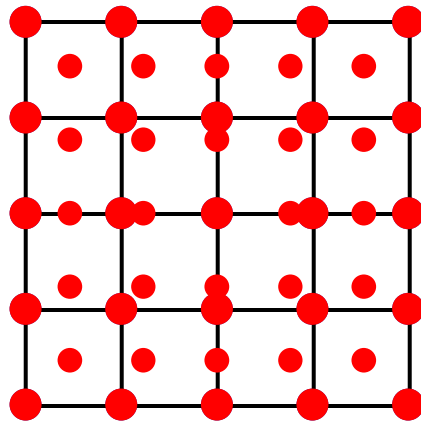
How to get $F(u,v)$?

- We are given a discrete set of values:
 - $F[i,j]$ for $i=0,\dots,N$, $j=0,\dots,M$
- Nearest neighbor:
 - $F(u,v) = F[\text{round}(N*u), \text{round}(M*v)]$
- Linear Interpolation:
 - $i = \text{floor}(N*u)$, $j = \text{floor}(M*v)$
 - interpolate from $F[i,j]$, $F[i+1,j]$, $F[i,j+1]$, $F[i+1,j+1]$
- Filtering in general !

Interpolation



Nearest neighbor



Linear Interpolation



Applying Our Mapping knowledge

Further Realism Improvements:

- **Environment Mapping**
- **Bump Mapping**
- **Displacement Mapping**
- **Illumination Mapping & Others?**

Environment Mapping

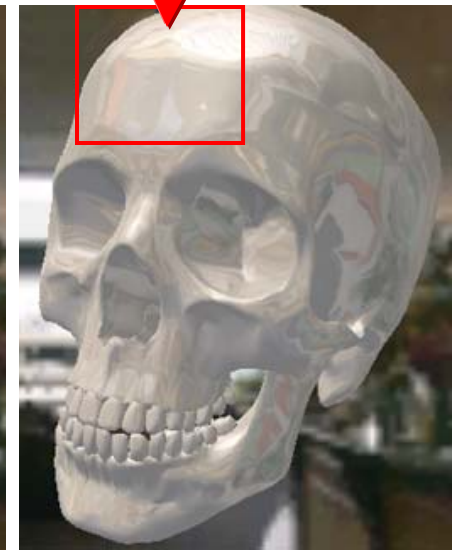
Main idea: "Environment Maps are textures that describe, for all directions, the incoming or out going light at a point in space." [Real Time Shading, pg. 49]"

Three main types:

- Cube Mapping
- Sphere mapping
- Paraboloid Mapping



No Map applied



**Reflections from
Environment**

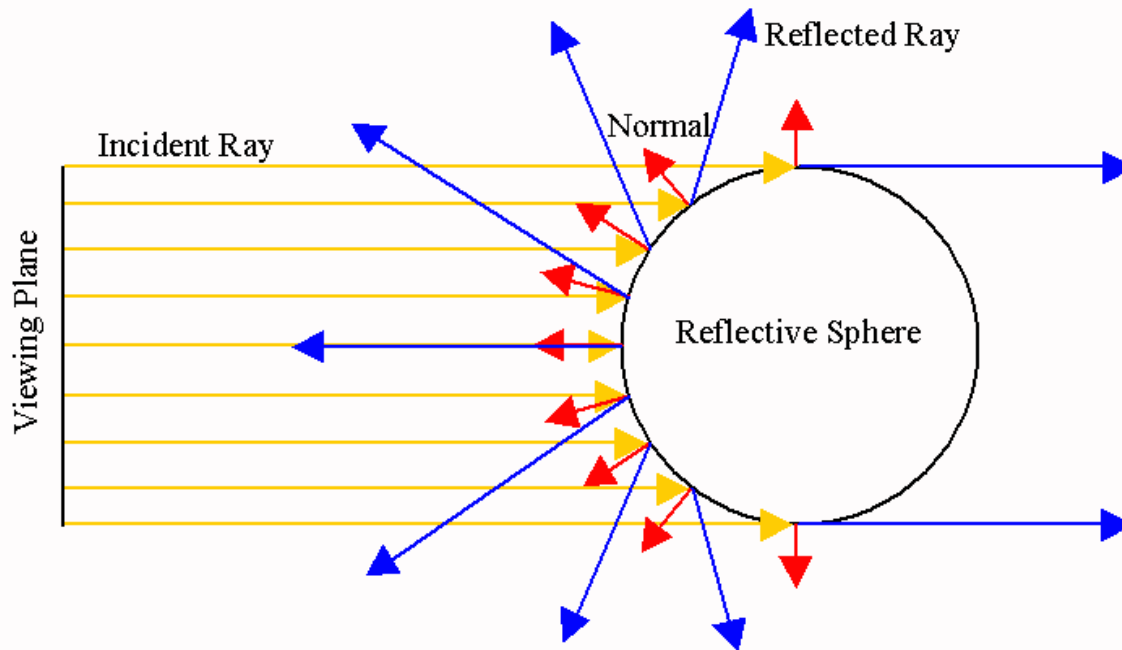
Map Applied

[Images courtesy of Microsoft, msdn.microsoft.com]

Environment Mapping

Sphere Mapping

- Generated from photographing a reflective sphere
- Captures whole environment



Sphere Texture Map

[Diagram and Sphere Map image of a Cafe in Palo Alto, CA, Heidrich]

Environment Mapping

Cons :

- Sphere maps have a singularity of the parameterization of this method, we must fix viewing direction, view-dependent (meaning if you want to change the viewers direction you have to regenerate the Sphere map).
- Paraboloid maps requires 2 passes

Pros:

- Better sampling of the texture environment for Paraboloid mapping, view-independent,
- Cube maps can be fast if implemented in hardware (real-time generation), view independent,

Bump Mapping

Main idea: "Combines per-fragment lighting with surface normal perturbations supplied by a texture, in order to simulate light interactions on a bumpy surface." [Cg Tutorial, pg 199]

Bump Map

**Geometry W/
New Normals**

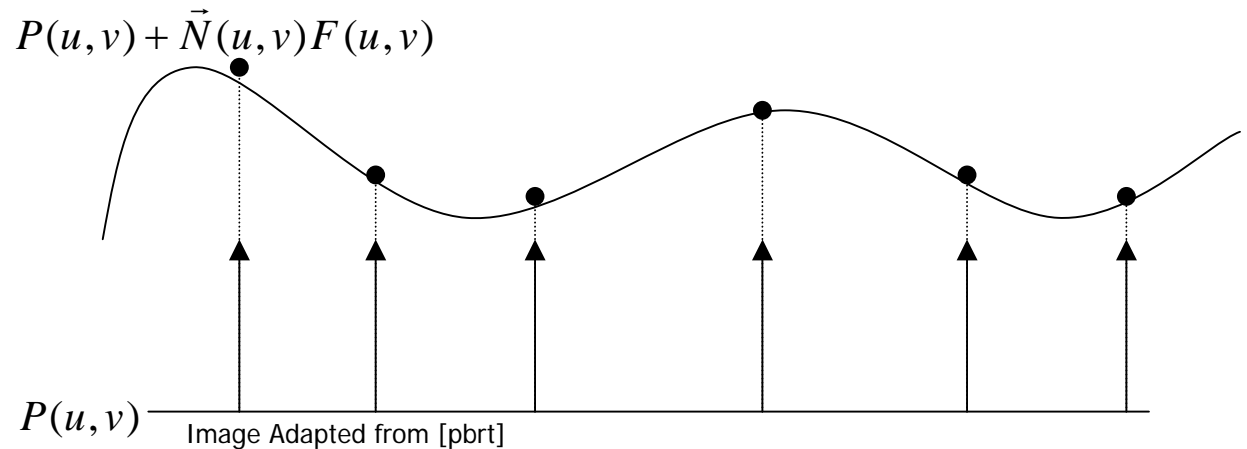
Original Geometry



Bump Mapping

$$P'(u, v) = P(u, v) + \vec{N}(u, v)F(u, v) *$$

- P = original Surface location/height
- N = Surface Normal
- F = Displacement Function
- P' = New Surface location/height



* Assumes \vec{N} is normalized.

Bump Mapping

Bump Map

- The new Normal N' for P' can be calculated from the cross product of it's partial derivatives[Blinn 78].



Differential Math!!!

$$\vec{N}' = \frac{\partial P'}{\partial u} \times \frac{\partial P'}{\partial v} \approx \vec{N} + \frac{\partial F}{\partial u} \left(\vec{N} \times \frac{\partial P}{\partial u} \right) + \frac{\partial F}{\partial v} \left(\vec{N} \times \frac{\partial P}{\partial v} \right)$$

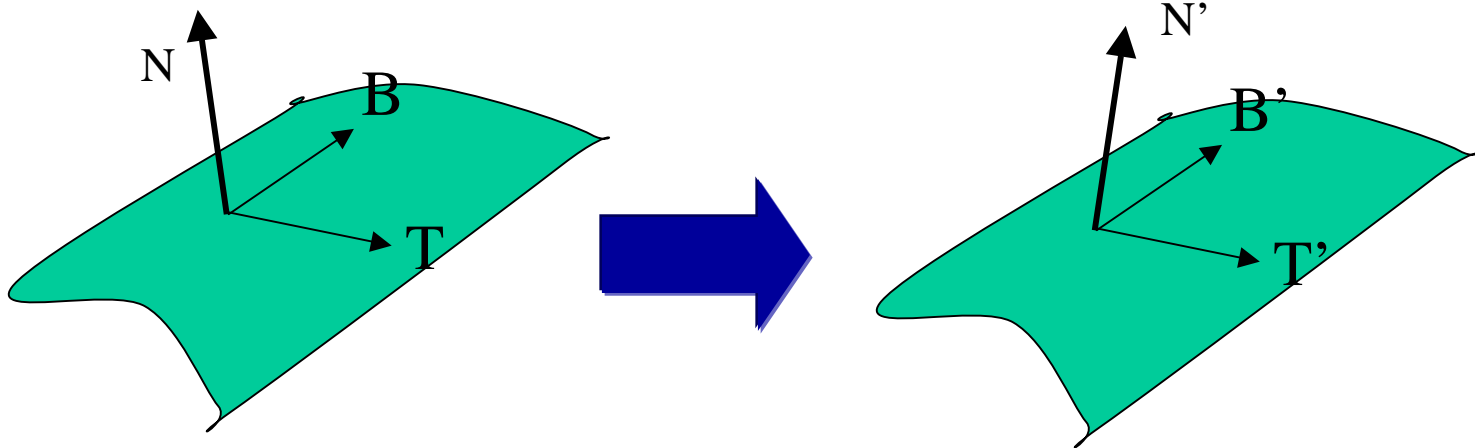
Tangent Space

Calculate Derivatives on the fly is complicated!

Solution:

- We know That our Normal $\mathbf{N} = \mathbf{B} \times \mathbf{T}$
- We Want a Normal \mathbf{N}'

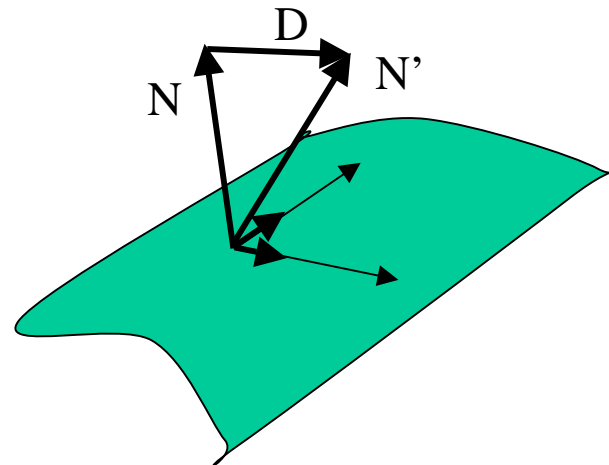
Determine \mathbf{B}' & \mathbf{T}' for \mathbf{P}' to Get \mathbf{N}'



Tangent Space

$$\begin{aligned} \mathbf{N}' &= \mathbf{P}'_u \times \mathbf{P}'_v \\ &= \mathbf{N} + \underbrace{\mathbf{B}(\mathbf{N} \times \mathbf{P}'_v) - \mathbf{T}(\mathbf{N} \times \mathbf{P}'_u)}_{\mathbf{D}} \\ &= \mathbf{N} + \mathbf{D} \end{aligned}$$

\mathbf{D} is just the distance \mathbf{N} has to move to be \mathbf{N}'



Bump Mapping

Optimizations:

- Info Is Known In Advance
- Pre-process & Lookup At Run-time



Normal Mapping

- Use Texture Map To Store N'
- Look up At Run-time
- Translate & Rotate

Used in Games!

- Hardware Texture Optimized
- Most Work Processed Offline

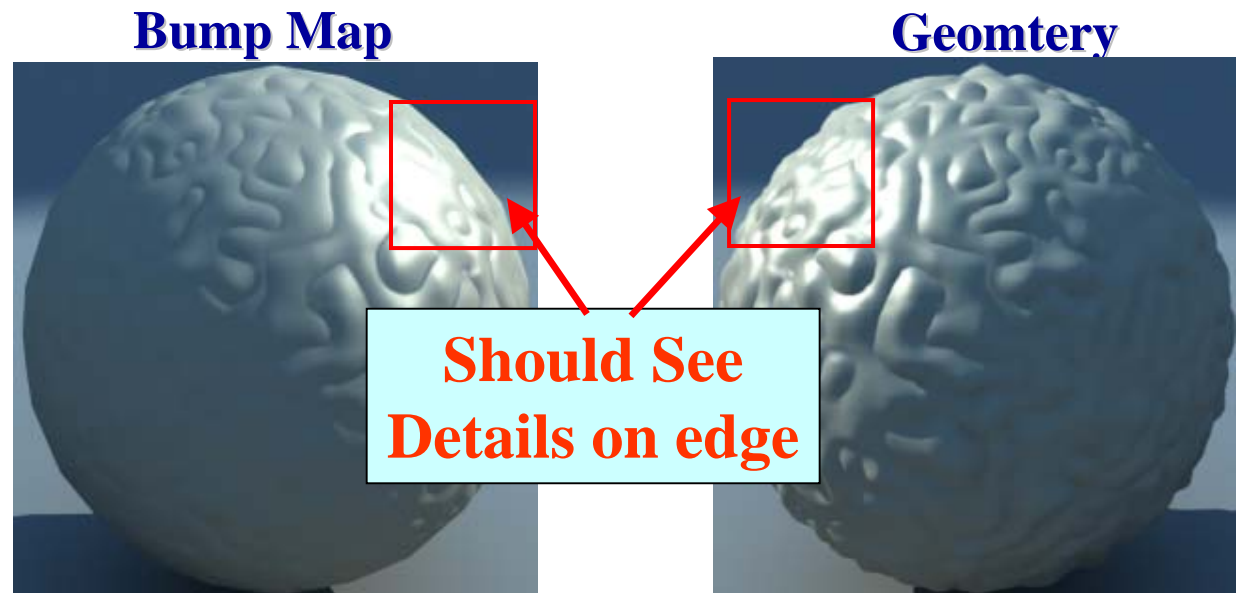
Bump Mapping

Pros:

- Produces the appearance of high detail w/ out cost
- Can be done in hardware

Cons:

- No self shadowing (natively)
- Artifacts on the silhouettes



Displacement Mapping

Main Idea: Use height map texture to displace vertices

- Realistic Perturbations Impossible to Model by Hand
- Actually Displacing Geometry, Not Normals
- No Bump Map Artifacts On Edges

With Displacement



Without Displacement

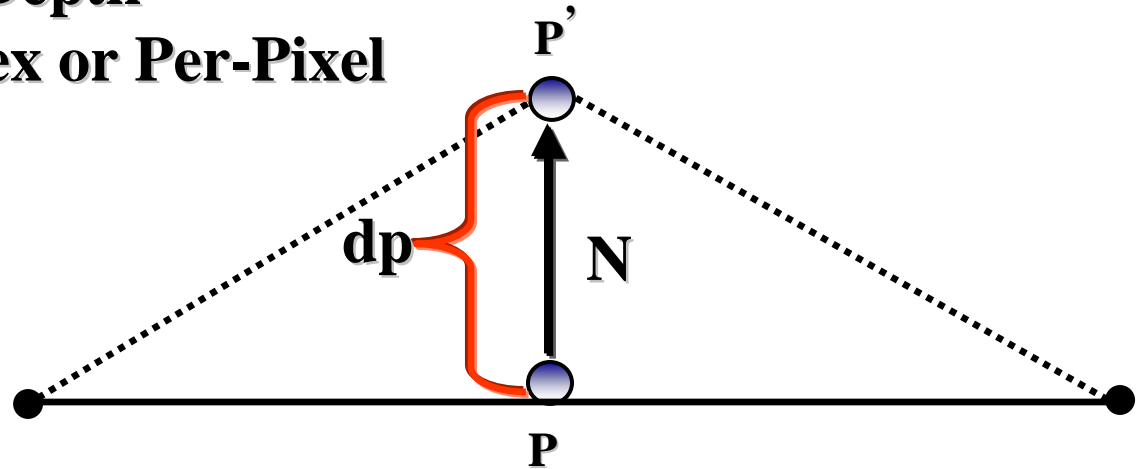


GPU Gems 2: Ch 18, [Using Vertex Texture Displacement for Realistic Water Rendering](#), Screen Captures of *Pacific Fighter* by Ubisoft

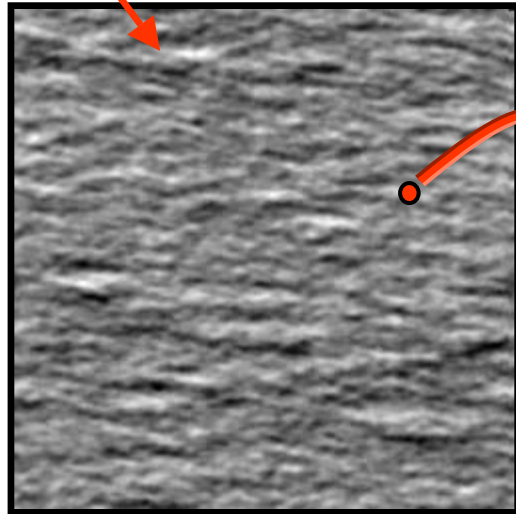
Displacement Mapping

- Gives Geometry Depth
- Can Do Per-Vertex or Per-Pixel

Could be
Heightfield



$$P' = P + (N * dp)$$



$$dp = 0.30 * R + 0.59 * G + 0.11 * B$$

Displacement Mapping Variant

Parallax Mapping:

- Perturb Texture Coordinates
- Based On Viewer Location
- As If Geometry Was Displaced

With Parallax Mapping



Without Parallax Mapping



[Comparison from the [Irrlicht Engine](#)]



Displacement Mapping

Pros:

- Efficient To Implement On GPU
- Good Results With Little Effort

Cons:

- Valid For Smoothly Varying Height fields
- Doesn't Account For Occlusions If Done Per-Pixel



Questions?

Thanks to all who's slides were borrowed and/or modified:

- David Lubke, Nvidia
- Ed Angel, University of New Mexico
- Durand & Cutler, MIT
- Juraj Obert, UCF