





Dice Rolling (1 of 4)

- Have 1d6, sample (i.e., roll 1 die)
- What is probability distribution of values?



Dice Rolling (2 of 4)

- Have 1d6, sample twice and sum (i.e., roll 2 dice)
- What is probability distribution of values?



Dice Rolling (3 of 4)

- Have 1d6, sample thrice and sum (i.e., roll 3 dice)
- What is probability distribution of values?



















Population of 200 game durations Mean µ = 69.637	Sample	Mean	Standard Deviation	Minimum	Median	Maximum	Range
Std Dev $\sigma = 10.411$	1	66.12	9.21	47.20	65.00	87.00	39.80
500 500 600 100011	2	73.30	12.48	52.40	71.10	101.10	48.70
Experiment w/20 samples	3	68.67	10.78	54.00	69.10	85.40	31.40
 Each 15 game durations 	4	69.95	10.57	54.50	68.00	87.80	33.30
(with replacement)	0	/3.2/	13.56	54.40	71.80	101.10	46.70
(with replacement)	0	09.27	10.04	50.10	70.30	85.70	35.60
 Table on right has 20 experiments 	0	00.73	9.38	52.40	67.30	82.60	30.20
	0	72.62	0.07	54.50	08.80	81.50	27.00
Observations?	10	60.25	3.37	50.10	71.90	88.90	38.80
	11	72.56	10.00	60.20	60.10	85.40	39.30
	12	60.69	11.67	49.10	60.40	0770	40.30
	13	64.65	9.71	47.10	64.10	78.50	31.40
	14	68.85	14.42	46.80	69.40	88.10	41.30
	15	67.91	8.34	52.40	69.40	79.60	27.20
	16	66.22	10.18	51.00	66.40	85.40	34.40
	17	68.17	8.18	54.20	66.50	86.10	31.90
	18	68.73	8.50	57.70	66.10	84.40	26.70
	19	68.57	11.08	47.10	70.40	82.60	35.50
	20	75.80	12.49	56.70	77.10	101.10	44.40

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	Sampling Error (1 of 2)													
•	Population of 200 game				State of Lot									
	Mean II = 69 637	Sample	Mean	Standard	Minter									
	(incur µ = 05.057	oumpro	mean	Deviation	winimum	Median	Maximum	Range						
	Std Dev $\sigma = 10.411$	1	66.12	9.21	47.20	65.00	87.00	39.80						
•	Experiment w/20 samples	2	73.30	12.48	52.40	71.10	101.10	48.70						
	Each 1E game durations		00.07 60.0F	10.78	54.00	69.10	85.40	31.40						
	- Each 15 gaille durations		79.95	10.57	54.50	68.00	87.80	33.30						
	(with replacement)	0	13.27	13.56	54.40	71.80	101.10	46.70						
	 Table on right has 20 	7	09.27	10.04	50.10	70.30	85.70	35.60						
	experiments	/	66.75	9.38	52.40	67.30	82.60	30.20						
	Observations?	8	58.72	7.62	54.50	68.80	81.50	27.00						
	Observations	9	12.42	9.97	50.10	/1.90	88.90	38.80						
	 Stats (x̄, s) differ each time! 	10	69.25	10.68	51.10	66.50	85.40	34.30						
		11	72.56	10.60	60.20	69.10	101.10	40.90						
	Canaatina aa biabaa	12	69.48	11.67	49.10	69.40	97.70	48.60						
	 sometimes lower than 	13	64.65	9.71	47.10	64.10	78.50	31.40						
		14	68.85	14.42	46.80	69.40	88.10	41.30						
	population (μ , σ)	15	67.91	8.34	52.40	69.40	79.60	27.20						
	 Sample range varies a lot 	16	66.22	10.18	51.00	66.40	85.40	34.40						
	more than sample	17	68.17	8.18	54.20	66.50	86.10	31.90						
	standard doviation	18	68.73	8.50	57.70	66.10	84.40	26.70						
	standard deviation	19	68.57	11.08	47.10	70.40	82.60	33.50						
	 Population mean (µ) 	20	75.80	12.49	56.70	77.10	101.10	44,40						
	always within sample			Sector rest and	A REAL PROPERTY OF A READ PROPERTY OF A REAL PROPER									
	range		\	1.	1									
	This variation → Sampling error Sampli													
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What Confidence Level to Use (1 of 2)?

- Often see 90% or 95% (or even 99%) used
- Choice based on loss if wrong (population parameter is outside), gain if right (parameter inside)
 - If loss is high compared to gain, use higher confidence
 - If loss is low compared to gain, use lower confidence
 - If loss is negligible, lower is fine
- Example (loss high compared to gain):
 - Hairspray, makes hair straight, but has chemicals
 - Want to be 99.99% confident it doesn't cause cancer
- Example (loss low compared to gain):
 Hairspray, makes hair straight, only uses water
 - Ok to be 75% confident it straightens hair
 - OK to be 75% confident it straightens ha

What Confidence Level to Use (2 of 2)?

- Often see 90% or 95% (or even 99%) used
- Choice based on loss if wrong (population parameter is outside), gain if right (parameter inside)
 - If loss is high compared to gain, use higher confidence
 - If loss is low compared to gain, use lower confidence
 - If loss is negligible, lower is fine
- Example (loss negligible):
 - Lottery ticket \$1, pays \$5 million
 - Chance of winning is 10⁻⁷ (1 in 10 million)
 - To win with 90% confidence, need 9 million tickets
 - No one would buy that many tickets!
 - So, most people happy with 0.01% confidence





Hypothesis Testing Terminology

- Null Hypothesis (H₀) hypothesis that no significance difference between measured value and population parameter (any observed difference due to error)
- e.g., population mean time for Riot to bring up NA servers was 4 hours
 Alternative Hypothesis – hypothesis contrary to null hypothesis
- e.g., population mean time for Riot to bring up NA servers was *not* 4 hours
 Care about alternate, but test null
- If data supports, alternate not true
- If data rejects, alternate may be true
 Why null and alternate?
- Remember, data doesn't "prove hypothesis
- hypothesis
 Can only reject it (at certain significance)
- So, reject Null

- P-value smallest level that can reject H₀
 "If p-value is low, then H₂ must go"
- How "low", consider s"risk" of being wrong
- Riot to



Hypothesis Testing Steps

- 1. State hypothesis (H) and null hypothesis (H₀)
- 2. Evaluate risks of being wrong (based on loss and gain), choosing significance (α) and sample size
- 3. Collect data (sample), compute statistics
- 4. Calculate p-value based on test statistic and compare to $\boldsymbol{\alpha}$
- 5. Make inference
 - Reject ${\rm H_0}$ if p-value less than α
 - Do not reject ${\rm H_0}$ if p-value greater than α

Hypothesis Testing Steps (Example)

- State hypothesis (H) and null hypothesis (H $_{\rm 0})$
 - H: Mario level takes less than 5 minutes to complete
 - H_0 : Mario level takes 5 minutes to complete (H_0 always has =)
- Evaluate risks of being wrong (based on loss and gain), choosing significance (α) and sample size
 - Player may get frustrated, quit game, so $\alpha = 0.01$
 - Note sure of normally distributed, so 30 (Central Limit Theorem)
- Collect data (sample), compute statistics
- 30 people play level, compute average time, compare to 5
- Calculate p-value based on test statistic and compare to α p-value = 0.002, α = 0.01
- Make inference
 - Reject H₀ if p-value less than α (REJECT H₀), so H may be right
 - Do not reject ${\rm H_0}$ if p-value greater than α