

**Homework #2**

**People I worked with and URL's of sites I visited:**

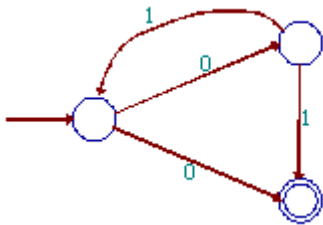
1. Show the following languages are regular by creating finite automata with  $L = L(M)$

- a) Strings over  $\{a,b\}$  that contain 2 consecutive  $a$ 's
- b) Strings over  $\{a,b\}$  that do not contain 2 consecutive  $a$ 's
- c) The set of strings over  $\{0,1\}$  which contain the substring  $00$  and the substring  $11$
- d) The set of strings over  $\{a,b\}$  which do not contain the substring  $ab$ .

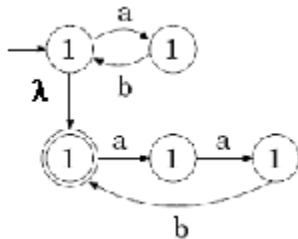
Show your answers in both table and graph form.

#2. Describe  $L(M)$  for the following nfa's: a) in words and b) as a regular expression

a)



b)



#3. Create an NFA (with  $\lambda$  transitions) for all strings over  $\{0, 1, 2\}$  that are missing at least one symbol. For example,  $00010$ ,  $1221$ , and  $222$  are all in  $L$  while  $221012$  is not in  $L$

#4. a) Given an NFA with several final states, show how to convert it into one with exactly one start state and exactly one final state.

b) Suppose an NFA with  $k$  states accepts at least one string. Show that it accepts a string of length  $k-1$  or less.

#5. Let  $L$  be a regular language. Show that the language consisting of all strings not in  $L$  is also regular.

