

Name \_\_\_\_\_

**CS5003  
Homework #7**

**I worked with:**

**I consulted:**

#1. M is the Turing machine:

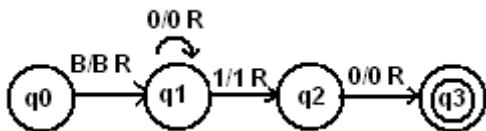
$\delta$	B	a	b	c
$q_0$	$q_1, B, R$			
$q_1$	$q_2, B, L$	$q_1, a, R$	$q_1, c, R$	$q_1, c, R$
$q_2$		$q_2, c, L$		$q_2, b, L$

- a) Trace the computation of  $a a b c a$
- b) Trace the computation of  $b c b c$
- c) Draw the graph for M
- d) What does M do?

#2. Construct a Turing machine with alphabet  $\{a,b\}$  to compute  $f(n) = 2n+3$ . Represent numbers in unary notation; that is, 0 is represented by a  $I$  on the tape, 1 by  $II$ , 2 by  $III$ . (So if  $n = 3$ , you would be left with ten 1's on the tape etc.). Have your Turing machine halt in the configuration:  $q_f B f(n) B$ .

3. Create a Turing machine to accept the language:  $a(a \cup b)^* b$

#4. Given the following Turing machine,



- a) What is  $L(M)$
- b) Show  $R(M)$  using the encodings described in the reading.

#5. Construct a Turing machine in words (i.e., describe its moves without actually writing all the transitions) that determines whether a string over  $\{0,1\}$  is the encoding of a Turing machine.