

Homework #4

#1. (11 Points) Prove that the following is not a regular language: The set of strings of 0's and 1's that are of the form $w w$

#2. (10 Points) Show that the language $L = \{a^p \mid p \text{ is prime}\}$ is not a regular language

#3. (9 Points) Suppose h is the homomorphism from $\{0,1,2\}$ to $\{a,b\}$ defined by $h(0) = a$; $h(1) = ab$; $h(2) = ba$.

- a) What is $h(21120)$
- b) If $L = 01^*2$, what is $h(L)$?
- c) If $L = a(ba)^*$, what is $h^{-1}(L)$?

#4. (20 Points) a) Show that the question: *Does $L = S^*$?* for regular language L is decidable.

- b) Show that the question, *Given a FA M over Σ , does M accept a string of length ≤ 2 ?* is decidable

#5. (Best answers will be posted to the bb) What is a CS or real world application of dfa state minimization?