

Homework #5

1. (5 Points) True or False:

- | | | |
|---|------|-------|
| a) The grammar, $G: E \rightarrow E + E \mid E * E \mid x$ is ambiguous | True | False |
| b) $L(G)$ for the G in part a is ambiguous | True | False |
| c) A grammar is ambiguous if $\exists w$ such that w 's right-most derivation differs from its left-most derivation | True | False |
| d) If r is a regular expression, then $L(r)$ can be generated by a CFG | True | False |
| e) The language described by a^*b^* is context-free | True | False |

2. (10 Points) Given the following grammar, G :

$S \rightarrow S A B \mid \varepsilon$
 $A \rightarrow 0 S 1 \mid C D \mid \varepsilon$
 $B \rightarrow 1 S 0 \mid \varepsilon$
 $C \rightarrow B C \mid A C \mid 0$

Is $0110\varepsilon \in L(G)$? Justify your answer.

Is $001100\varepsilon \in L(G)$? Justify your answer.

#3. (10 Points) a) Create a grammar that generates the language $L = \{a^{2^n}b^{3^n} \mid n \geq 0\}$ Also b) construct a parse tree and c) leftmost derivation of $aabbb$. d) Is your grammar ambiguous? Why or why not?

#4. (10 Points) Consider the following DTD (XML grammar) for songs (from <http://www.cafeconleche.org/slides/sd2004west/xmlfundamentals/22.html> by Rusty Harold):

```
<!ELEMENT SONG (TITLE, COMPOSER+, PRODUCER*, PUBLISHER*,  
                LENGTH?, YEAR?, ARTIST+)>
```

```
<!ELEMENT TITLE (#PCDATA)>
```

```
<!ELEMENT COMPOSER (#PCDATA)>
```

```
<!ELEMENT PRODUCER (#PCDATA)>
```

```
<!ELEMENT PUBLISHER (#PCDATA)>
```

```
<!ELEMENT LENGTH (#PCDATA)>
```

```
<!-- This should be a four digit year like "1999",  
      not a two-digit year like "99" -->
```

```
<!ELEMENT YEAR (#PCDATA)>
```

<!ELEMENT ARTIST (#PCDATA)>

and the following song:

```
<?xml version="1.0"?>
<!DOCTYPE SONG SYSTEM "song.dtd">
<SONG>
  <TITLE>Hot Cop</TITLE>
  <COMPOSER>Jacques Morali</COMPOSER>
  <COMPOSER>Henri Belolo</COMPOSER>
  <COMPOSER>Victor Willis</COMPOSER>
  <PRODUCER>Jacques Morali</PRODUCER>
  <PUBLISHER>PolyGram Records</PUBLISHER>
  <LENGTH>6:20</LENGTH>
  <YEAR>1978</YEAR>
  <ARTIST>Village People</ARTIST>
</SONG>
```

a) Translate the grammar to a standard CFG. You may consider *#PCData* to be terminals (that can contain any character data).

b) Using your grammar, show a parse tree for the song.

#5. (5 Points) For the grammar G:

$$S \rightarrow 0S1 \mid 1S0 \mid \varepsilon$$

What is $L(G)$?

#6. (10 Points) For the grammar G: $S \rightarrow 0S1 \mid \lambda$

a) show that $L(G) \subseteq \{0^n 1^n \mid n \geq 0\} = L$ (You need not do a formal induction)

(Hint 1: show that for all $w \in L(G)$, $w \in \{0^n 1^n \mid n \geq 0\}$ **Hint 2:** $w \in L(G)$ means $S \rightarrow w$)

b) show that $\{0^n 1^n \mid n \geq 0\} \subseteq L(G)$ (You need not do a formal induction)

c) show that $L(G) = \{w \mid w = w^R\}$