

# A Study of Active Queue Management for Congestion Control

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# Outline

- *Introduction*
- *Feedback Control System Background*
- *FCS applied to AQM*
- *Calculating FCS equations*
- *Simulation verifications*
- *RED configuration recommendations*
- *Conclusion*

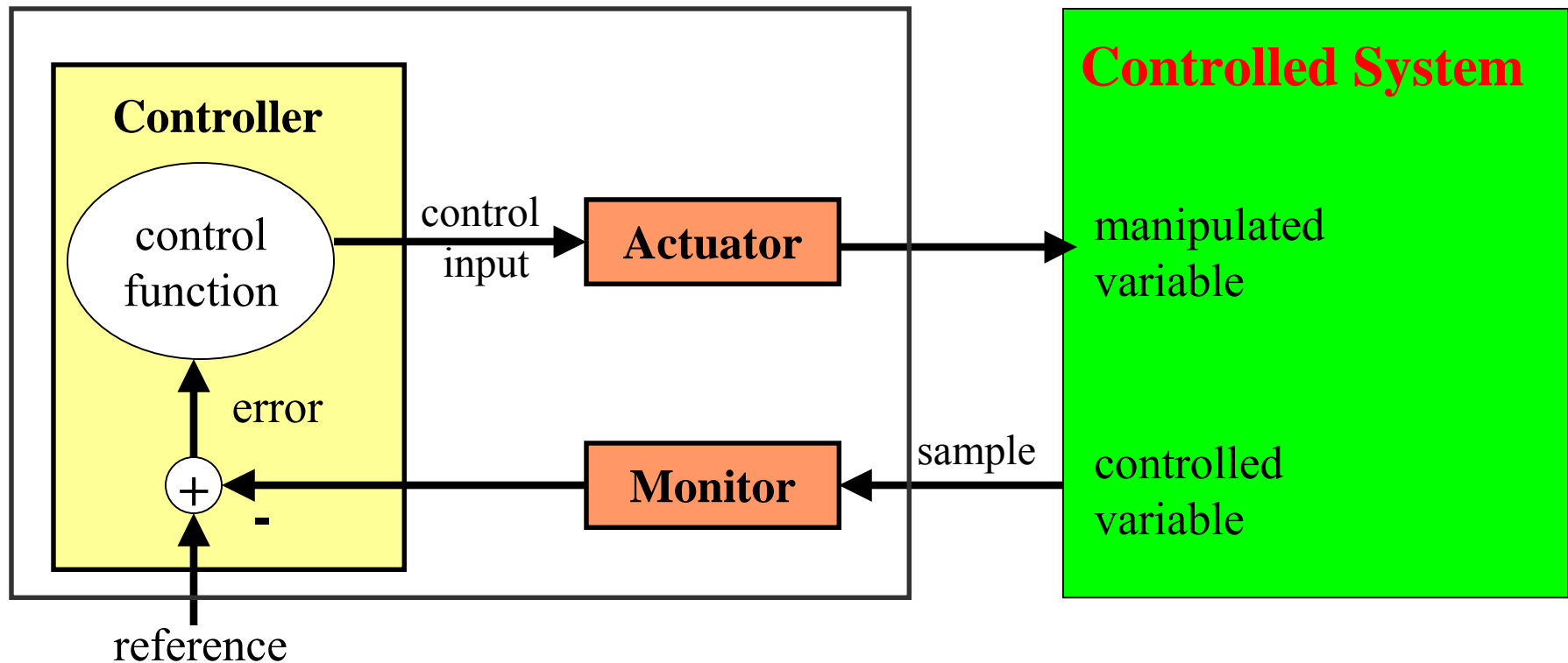
# Introduction

- Goal - Determine “best” RED configuration using systematic approach
- Models - queue vs. feedback control system
- Mathematical analysis and fundamental Laws
- Simulation verification of model
- Recommendations
- Future directions

# Feedback Control systems

- What is it? – Model where a change in input causes system variables to conform to desired values called the reference
- Why this model ? - Can create a stable and efficient system
- Two basic models - Open vs. Closed loop

# Feedback Control (closed loop)



# How to apply FCS to AQM

- Try to get two equations to derive steady state behavior – in our case queue function (avg. length of queue) and control function (dependent upon architecture –RED)

Control theory → stability

- Networks as a feedback system
- Distributed & delayed feedback

# Model TCP Avg. Queue Size

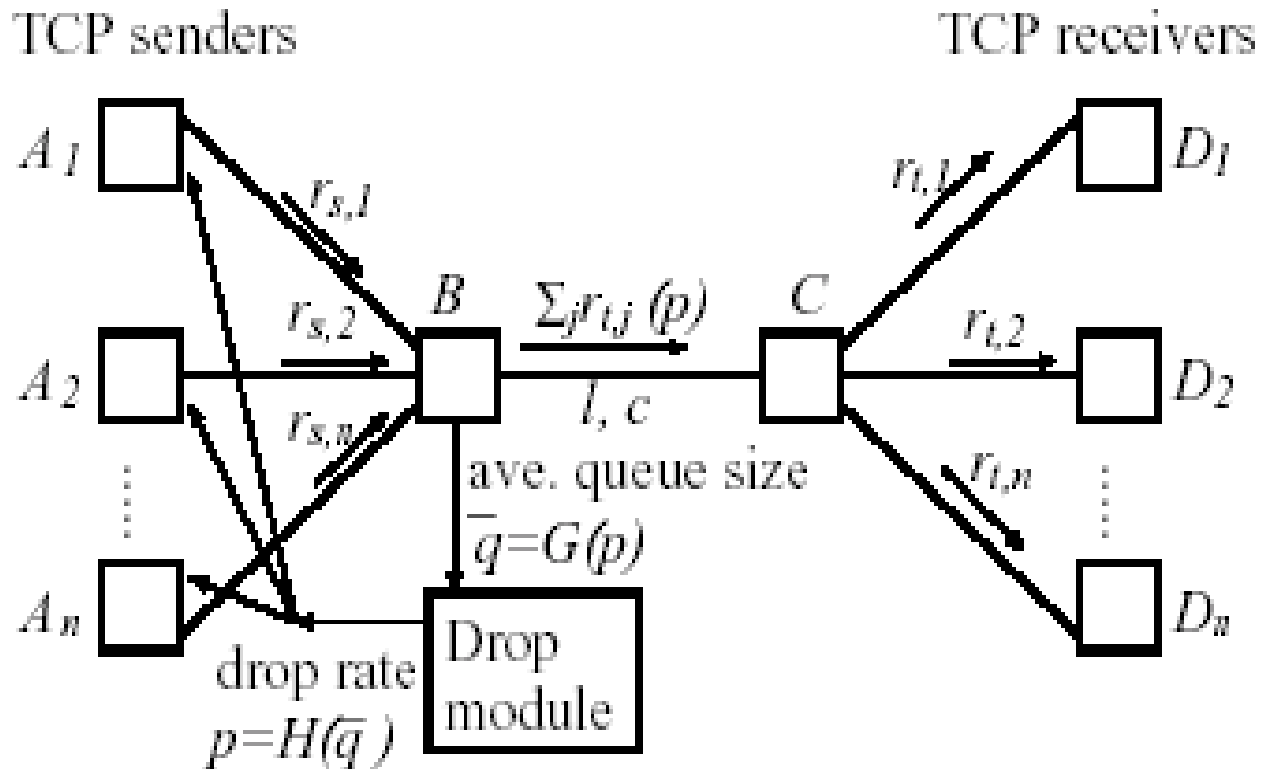


Fig. 1. An  $n$ -flow feedback control system

# Single flow feedback system

$$\sum_{j=1}^n r_{t,j} \leq c$$

$$r_{t,i}(p, R_i) = T(p, R_i)$$

Becomes

$$r_{t,i}(p, R) \leq c/n, 1 \leq i \leq n$$



# Finding the Queue “Law”

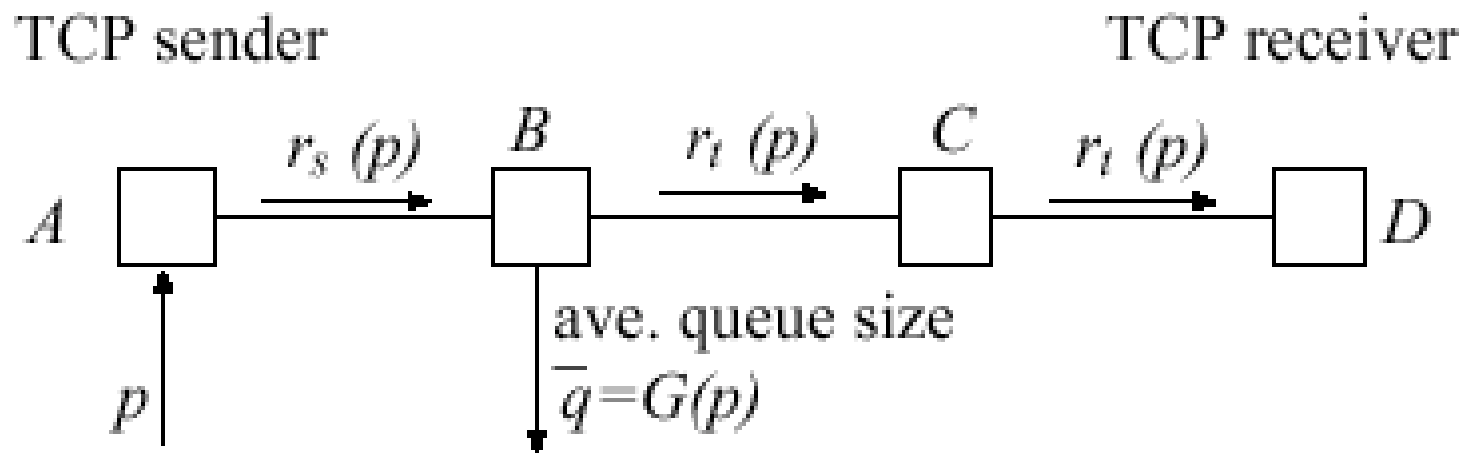


Fig. 3. An open control system with one TCP flow

# Non Feedback Queue “Law”

$$R = R_0 + \bar{q}/c$$
$$p_0 = T_p^{-1}(c/n, R_0)$$

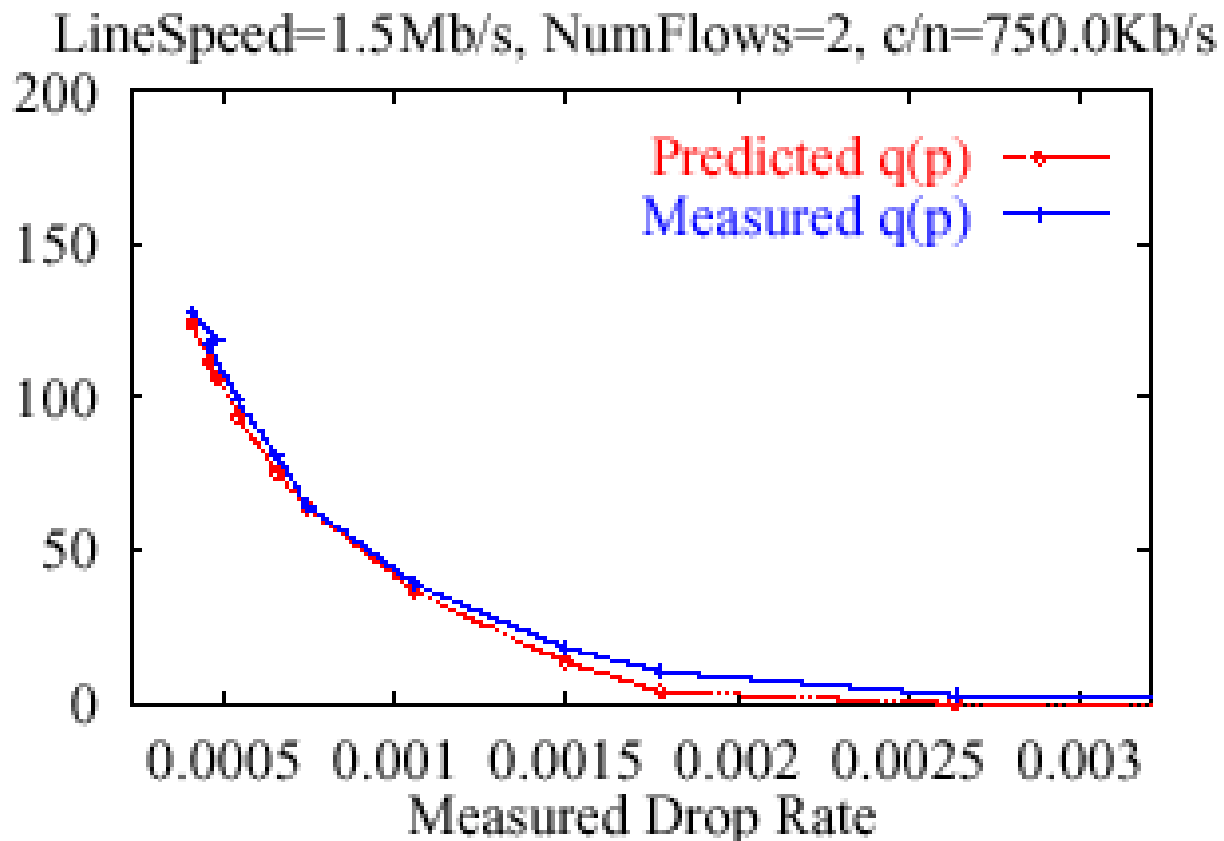
$$\bar{q}(p) = \begin{cases} \max(B, c(T_R^{-1}(p, c/n) - R_0)), & p \leq p_0 \\ \text{Else } 0 \end{cases}$$

$$u(p) = \begin{cases} 1, & p \leq p_0 \\ \text{Else } T(p, R_0) / (c/n) \end{cases}$$

# Verification through simulation

- Using NS run multiple simulations varying link capacity, number of flows, and drop probability  $p$
- Flows are “infinite” FTP sessions with fixed RTT
- Buffer is large enough to prevent packet loss due to overflow
- Graph mathematically predicted average queue size vs. simulation (and do the same with link utilization)

# One Sample Result



# Add in Feedback

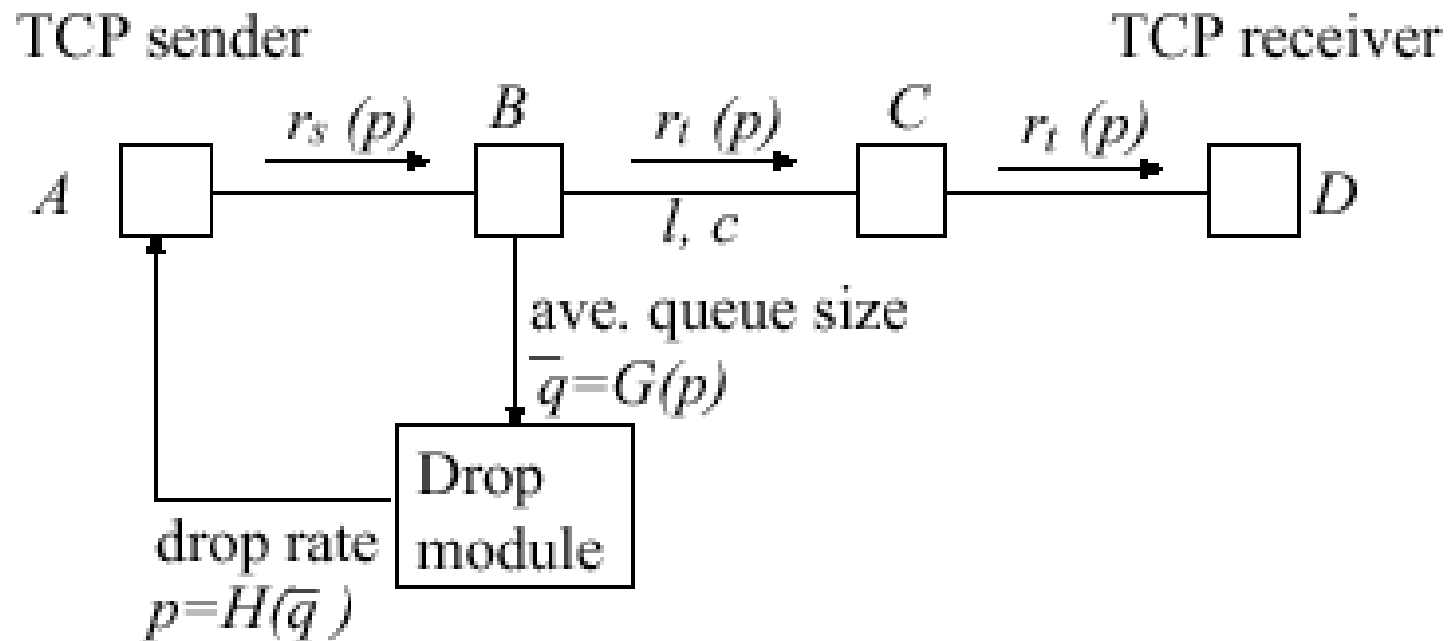
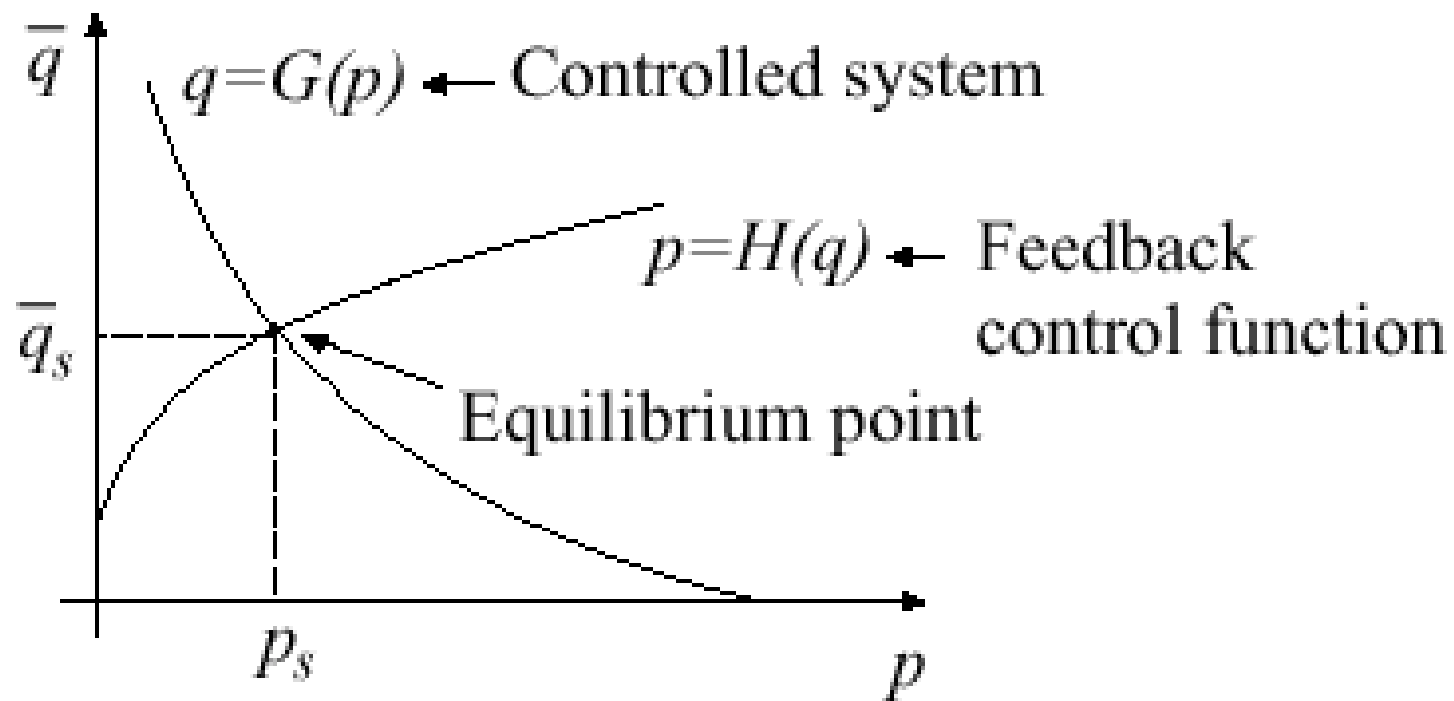


Fig. 2. A single-flow feedback control system

# Feedback Control system Equilibrium point



# RED as a Control Function

$$p = H(\bar{q}_e) = \begin{cases} 0, & 0 \leq \bar{q}_e < q_{min} \\ \frac{\bar{q}_e - q_{min}}{q_{max} - q_{min}} p_{max}, & q_{min} \leq \bar{q}_e < q_{max} \\ 1, & q_{max} \leq \bar{q}_e \leq B \end{cases}$$

# Simulation with $G(p)$ and $H(\bar{q})$

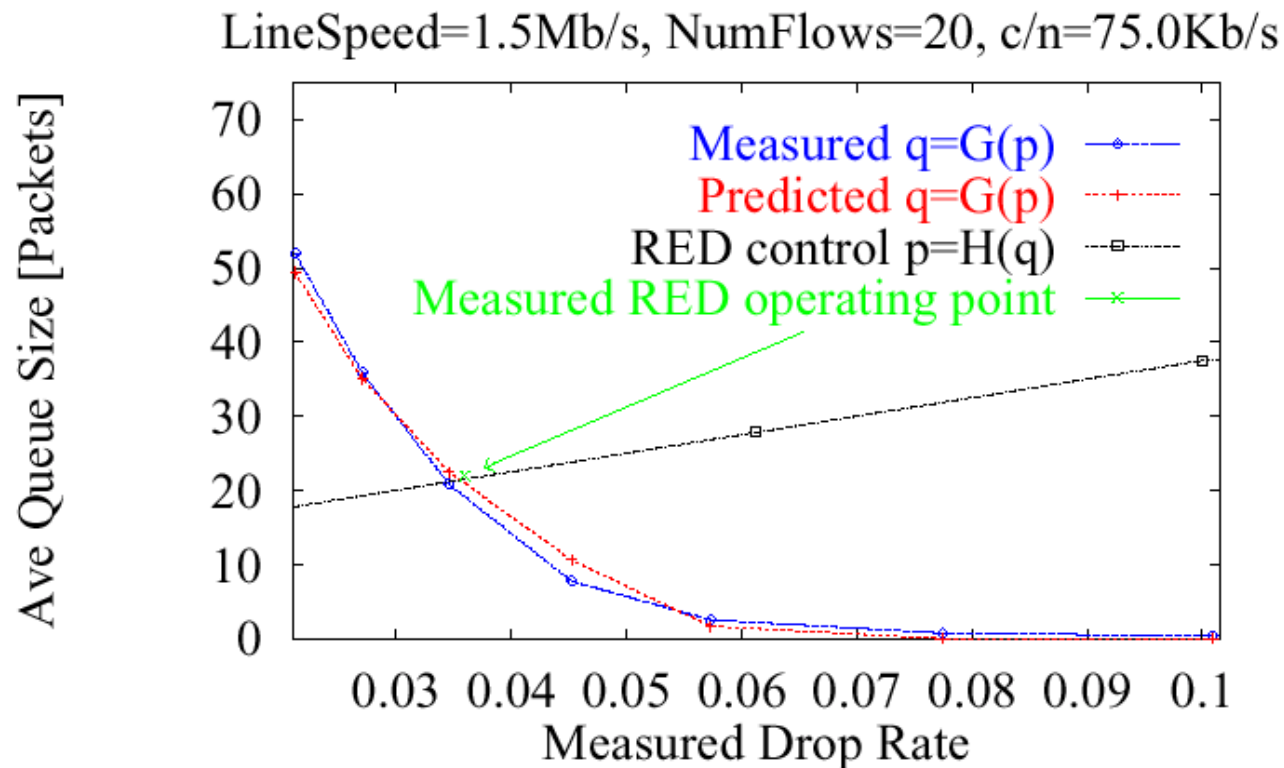
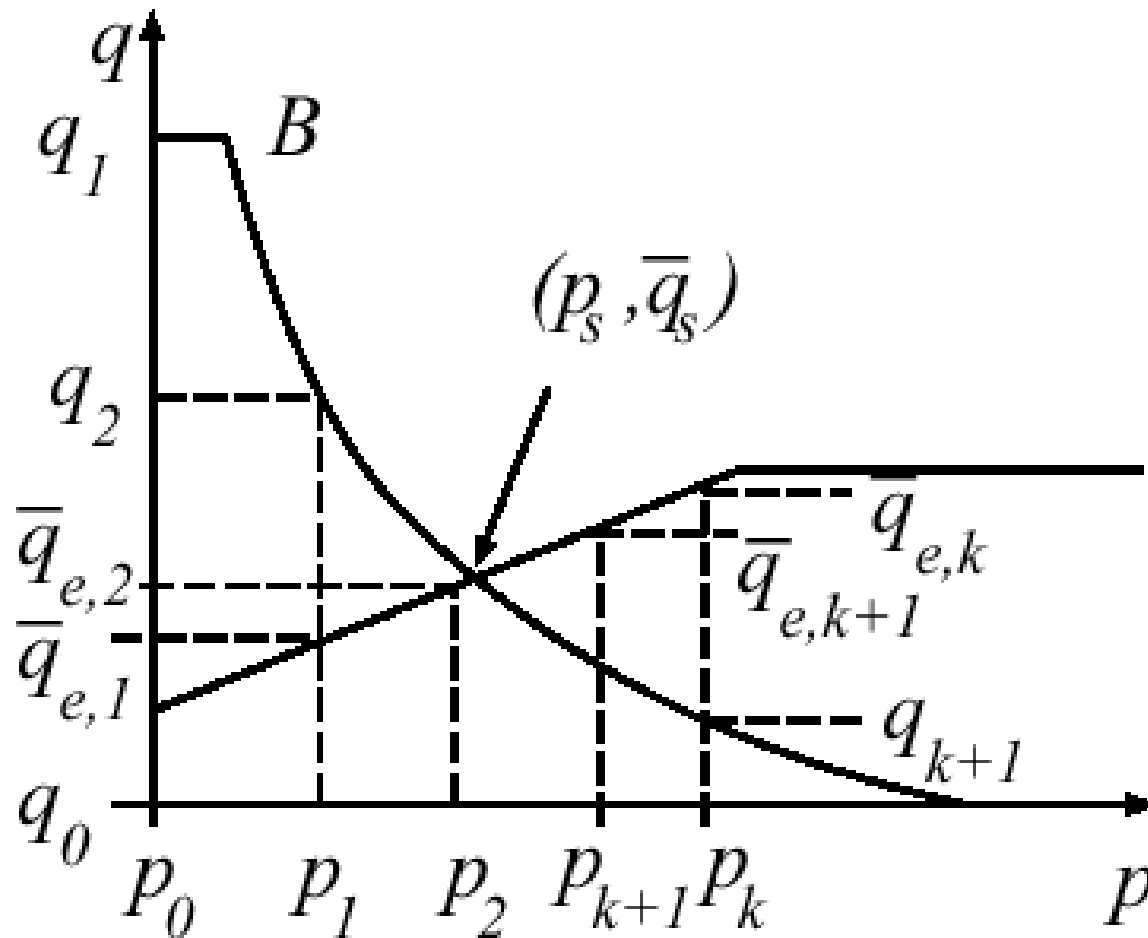


Fig. 8. RED average operating point: measured and predicted



# RED convergence point



# Stable system results

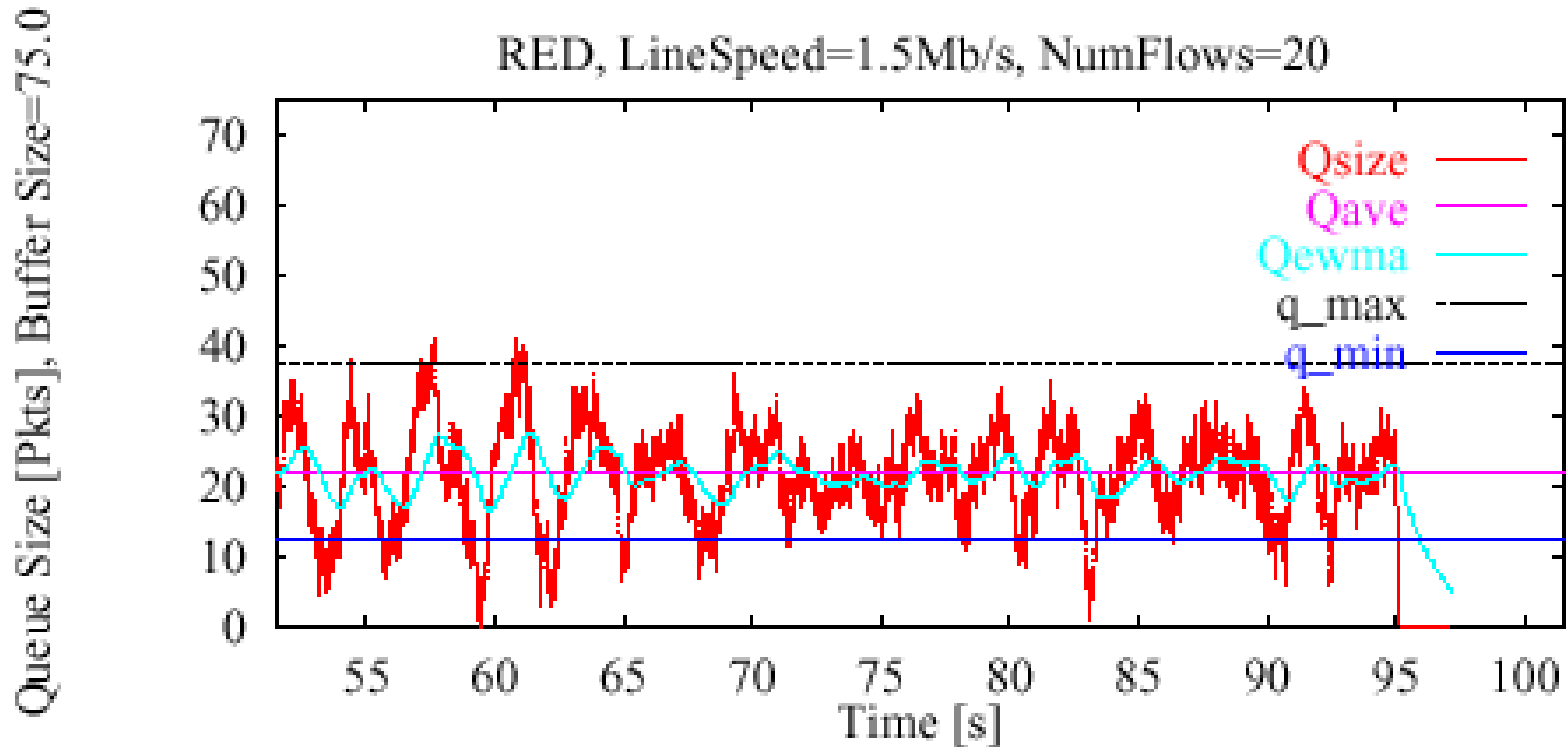


Fig. 10. Instantaneous and average queue size in time, converging case

# Unstable results

LineSpeed=1.5Mb/s, NumFlows=120, c/n=12.5Kb/s

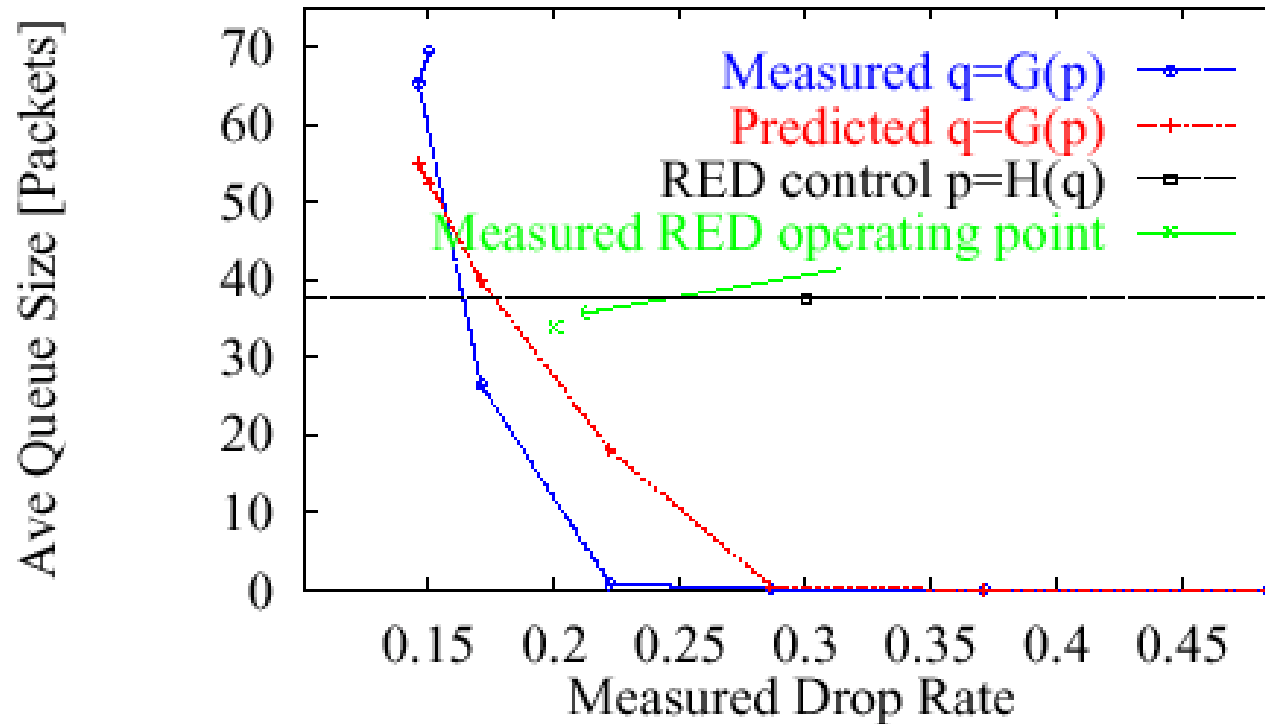


Fig. 11. RED average operating point situated beyond  $p_{\text{thresh}} = 0.1$

# Unstable results part 2

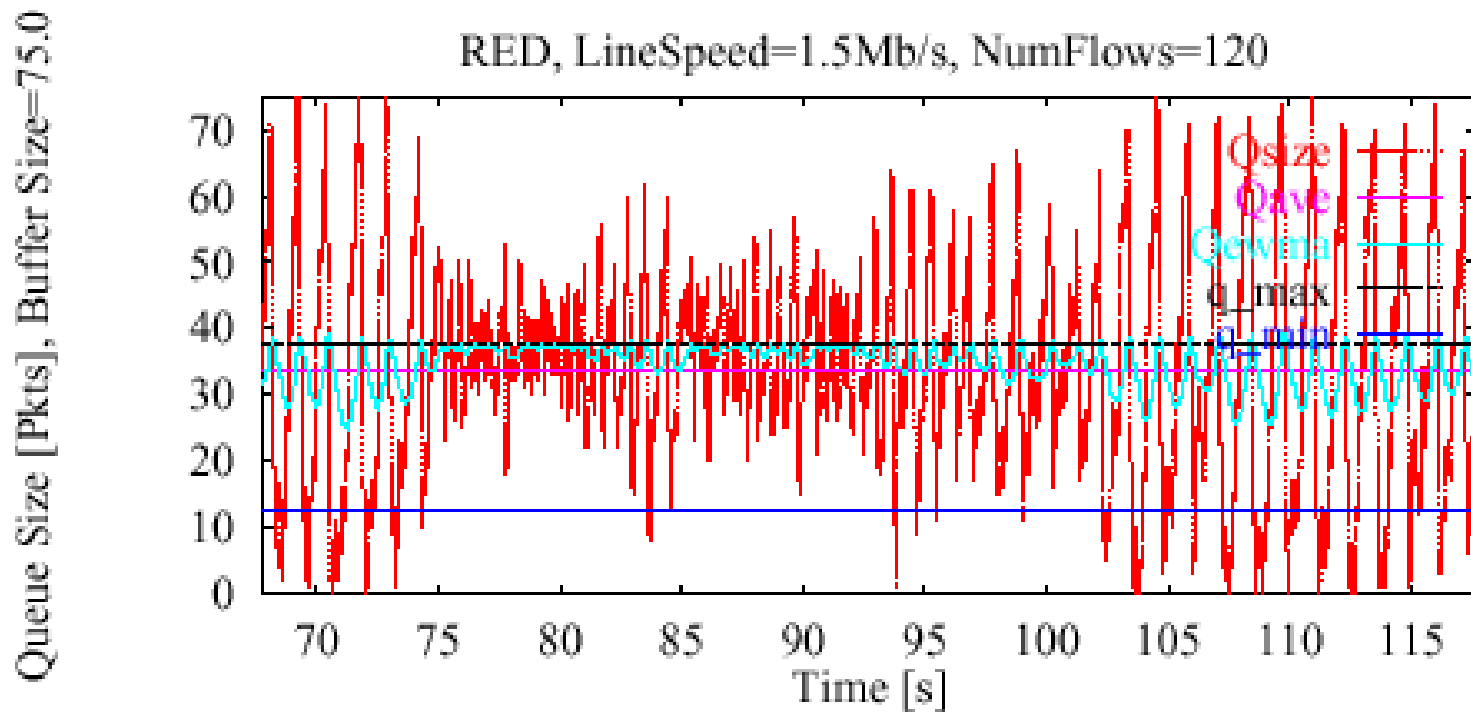
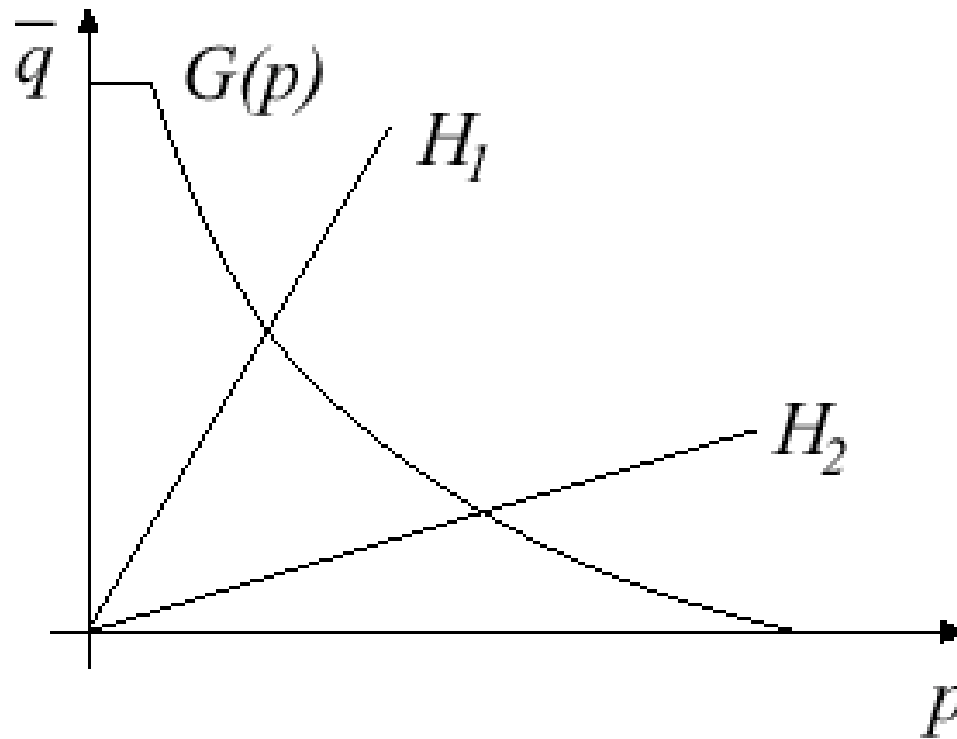


Fig. 13. Instantaneous and average queue size in time, oscillating case

# RED configuration Recommendations

- **drop-conservative policy:** low  $p$ , high  $\bar{q}$
- **delay-conservative policy:** low  $\bar{q}$ , high  $p$
- Need to estimate:
  1. Line speed  $c$
  2. Min and Max throughput per flow  $\tau$  or number of flows  $n$
  3. Min and Max packet size  $M$
  4. Min and Max RRT  $R_0$

# Sample Control Law policy



# Range of Queue Laws

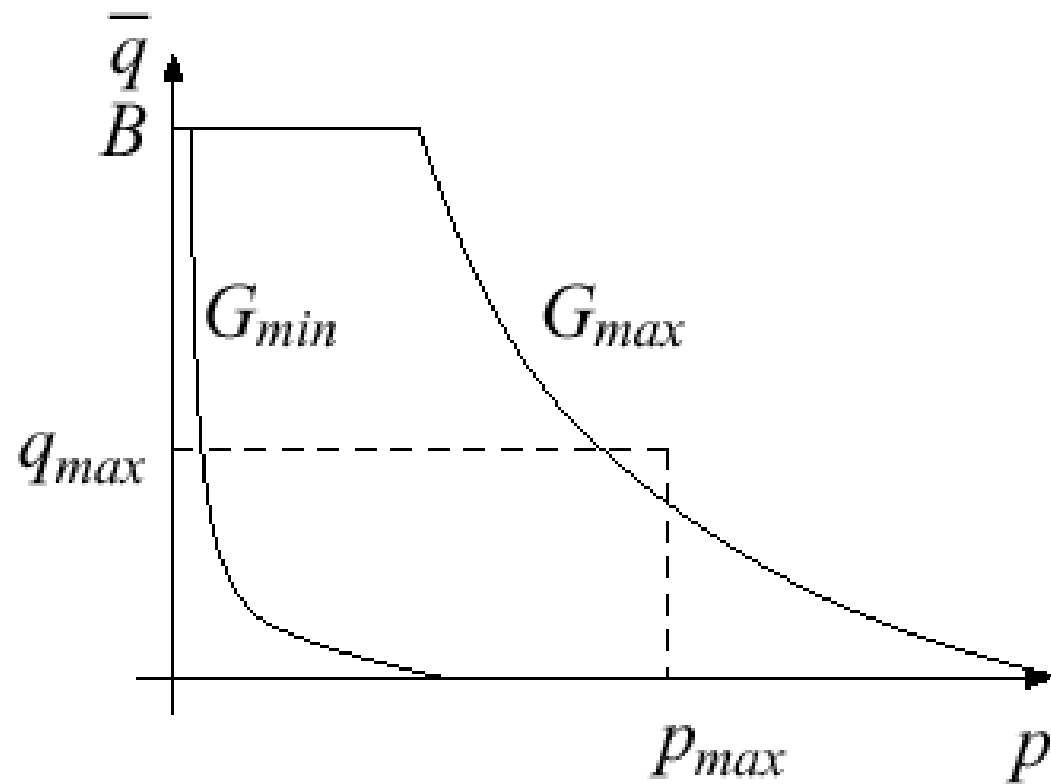


Fig. 15. Range of queue laws for a given queue system

# Configuring Estimator of average queue Size

Consists of :

- Queue averaging algorithms
- Averaging interval
- Sampling the queue size



# Queue Averaging Algorithm

- Low- pass filter on current queue size
- Moving average to filter out bursts
- Exponential weighting decreasing with age
- Estimate is computed over samples from the previous  $I$  time period – recommendations for  $I$  to follow

$$\text{Average weight} = w = 1 - a^{\delta/I}$$

# Averaging Interval I

- Should provide good estimate of long term average assuming number of flows is constant
- Should adapt as fast as possible to change in traffic conditions

# $I = P$ is recommended

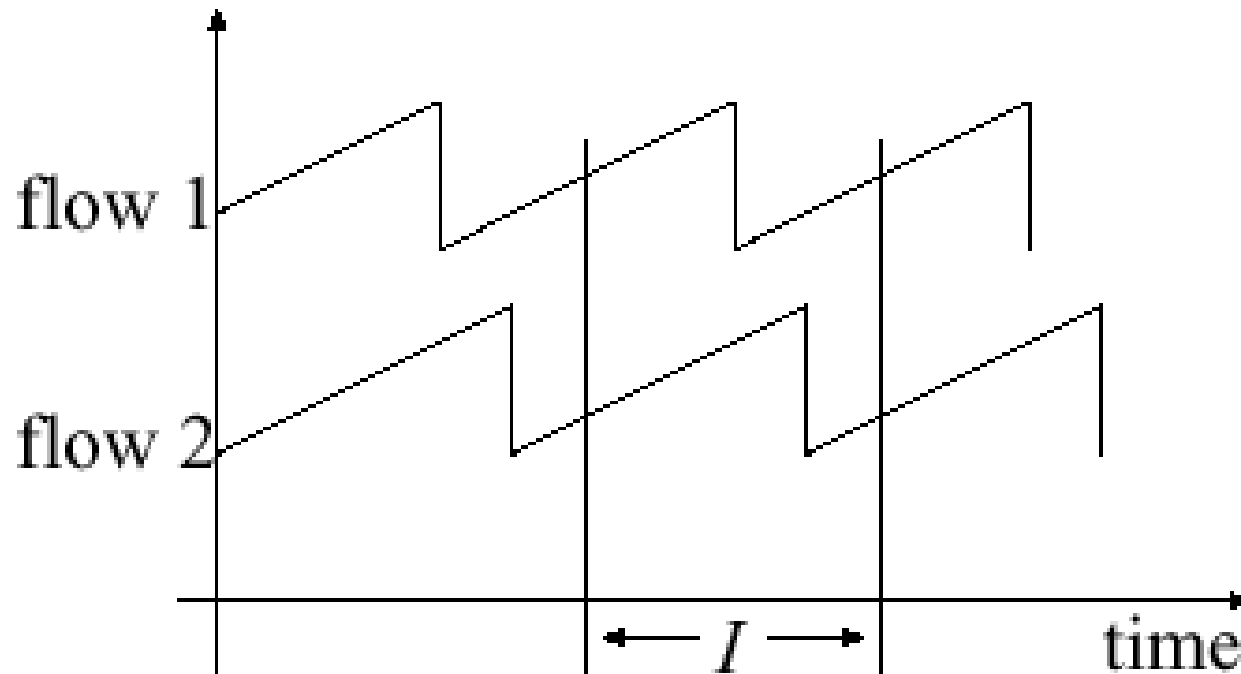


Fig. 18. Averaging two TCP flows

# Sampling the Queue size

- Queue size acts like a step function
- Changes every RTT with adjustments made from information received
- “Ideal” sampling rate is once every RTT
- Recommend sampling = minimum RRT

# Conclusions

- Feedback control model validated through simulations
- Found instability points and recommended settings to avoid them
- Also developed recommended RED queue size estimator settings
- Many issues still to look at in future

# Thoughts

- Nice idea using model from a different discipline to analyze networks
- Good simulations to validate predicted data
- Many assumptions made to make math and model work which may make it invalid
- Limited traffic patterns and type of traffic also make the model's value suspect

# Questions?

